

# **I**HE 2<sup>ND</sup> EDITION **ELECTRONICS COMPANION** Devices and Circuits for

Physicists and Engineers

# A. C. FISCHER-CRIPPS



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# THE 2ND EDITION ELECTRONICS COMPANION

Devices and Circuits for Physicists and Engineers

# **ANTHONY C. FISCHER-CRIPPS**

Fischer-Cripps Laboratories Pty Ltd Sydney, Australia



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This book is dedicated to Robert Winston Cheary.

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## Preface

This book is designed to help you understand the basic principles of electronics. The combination of succinct, but detailed explanations, review questions, and laboratory experiments work together to provide a consistent and logical account of the way in which basic electronics circuits are designed and how they work. The book arose out of a series of lectures that I attended as a student, and then later in life, as the lecturer. I am indebted to the late Robert Cheary, who presented this course for many years at the University of Technology, Sydney. I also express my appreciation to Walter Kalceff and Les Kirkup, my co-presenters, and Anthony Wong, who assisted me in the laboratory with many generations of enthusiastic students.

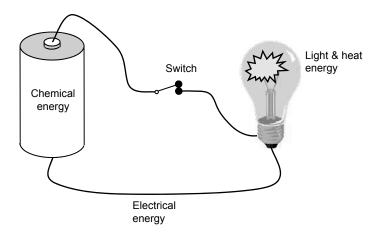
This second edition falls under the auspices of Taylor & Francis. I thank Tom Spicer and John Navas for their sponsorship of the first edition at the Institute of Physics Publishing, and to Francesca McGowan and the publication team at Taylor & Francis for their continued support and very professional approach to the whole publication process.

I hope that you will find this book a useful companion in your study of electronics.

Tony Fischer-Cripps, Killarney Heights, Australia This page intentionally left blank

Summary			
$F = k \frac{q_1 q_2}{d^2}$	Force between two charges where	$k = \frac{1}{4}$	
$F = q_1 E$	Force on a charge a field	in $4\pi \varepsilon_{o}$	
$E = 4\pi k \frac{Q}{A}$	Electric field - point charge	t	
$\overline{E} = k \frac{q\hat{r}}{r^2}$	Electric field - point charge	t	
$\phi = EA$	Electric flux		
$I = A(q_1n_1v_1 +$	$+(-q_2)n_2(-v_2)\Big)$		
$i = \frac{dq}{dt}$	Electric current		
$\frac{W}{q} = Ed$	Electric potential		
$\frac{V}{I} = R$	Ohm's law	$U = \frac{1}{2}CV^2$	Energy - capacitor
$P = VI = I^2 R$	Power - resistor	$U = \frac{1}{2}LI^2$	Energy - inductor
$R = \rho \frac{1}{A}$		$R_{AB} = R_1 + R_2$	Resistors - series
$C = \frac{Q}{V} = \varepsilon_0 \frac{A}{d}$		$\frac{1}{R_{AB}} = \frac{1}{R_1} + \frac{1}{R_2}$	Resistors - parallel
$L = \mu_0 A \frac{N^2}{1}$	Inductance	$R_{AB} = \frac{R_1 R_2}{R_1 + R_2}$	

Consider a circuit in which a battery is connected to a light bulb through a switch.



In this simple electrical system, **chemical energy** is converted into **electrical energy** in the battery. The electrical energy travels along the wires to the light bulb where it is converted into heat and light. The switch is used to interrupt the flow of electrical energy to the light bulb.

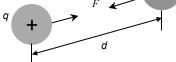
Although such an electrical system may seem commonplace to us now, it was only invented about 100 years ago. For thousands of years before this, light and heat were obtained by burning oil or some other combustible fuel (e.g., wood). Although the concept of electric charge was known to the ancient Greeks, and electricity as we know it was well-studied in the 19th century, it remained a scientific curiosity for many years until it was put to use in an engineering sense.

In the early part of the 20th century, electrical engineering was concerned with motors, generators and generally large scale electrical machines. In the second half of the 20th century, advances in the understanding of the electronic structure of matter led to the emergence of the new field of electronics. Initially, electronic circuits were built around relatively large scale devices such as thermionic valves. Later, the functionality of valves was implemented using solid-state components through the use of semiconductors.

## 1.2 Electric Charge

Electrical (and magnetic) effects are a consequence of a property of matter called electric charge. Experiments show that there are two types of charge that we label positive and negative. Experiments also show that

unlike charges attract and like charges repel.



The force of attraction or repulsion can be calculated using Coulomb's law:

• if F is positive, the charges repel;

• if F is negative, the charges attract.

In vector form, the direction of **F** is

The charge on a body usually refers to its excess or net charge. The smallest unit of charge is that on one electron  $q_e = -1.60219 \times 10^{-19}$ coulombs.

$$F = k \frac{q_1 q_2}{d^2}$$
distance between  
charges
$$k = \frac{1}{4\pi\varepsilon_o} = 9 \times 10^9 \text{ N m}^2 \text{C}^{-2}$$

$$\varepsilon_o = 8.85 \times 10^{-12}$$

determined by the direction of the unit vector **r** and the farads/metre (F m<sup>-1</sup>) sign of the charges. If the charges have the same sign, then the direction of **F** is the same as that of **r**.  $\mathbf{F} = k \frac{q_1 q_2 \hat{\mathbf{r}}}{d^2}$  The purpose of  $\hat{\mathbf{r}}$  is to point a direction; it has a magnitude of 1.

If the two charges are in some substance, e.g., air, then the **Coulomb force** is reduced. Instead of using  $\varepsilon_0$ , we must use  $\varepsilon$ substance. Often, the relative permittivity substance.  $\varepsilon_r$  is specified.  $\varepsilon_r = \frac{\varepsilon}{\varepsilon_0}$ 

- 1. imagine that one of the charges is hidden from view:
- 2. the other charge still experiences the Coulomb force and thus we say it is acted upon by an electric field;
- 3. if a test charge experiences a force when placed in a certain place, then an electric field exists at that place. The direction of the field is taken to be that in which a positive test charge would move in the field.

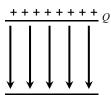
for the Material 
$$\varepsilon_r$$
  
vacuum 1  
water 80  
glass 8  
The units of  $E$  are  
newtons/  
coulomb

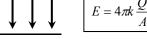
let  $E = k \frac{q_2}{d^2}$ thus  $F = q_1 E$ 

Note: the origin of the  $F = k \frac{q_1 q_2}{d^2}$  field *E* may be due to the presence of many presence of many charges but the magnitude and direction of the resultant field E can be obtained by measuring the force F on a single test charge q.

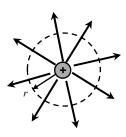
# 1.3 Electric Flux

An electric field may be represented by lines of force. The total number of lines is called the **electric flux**. The number of lines per unit cross-sectional area is the **electric field intensity**, or simply, the magnitude of the electric field.





0



Non-uniform field surrounding a point charge

Uniform electric

field between two

charged parallel

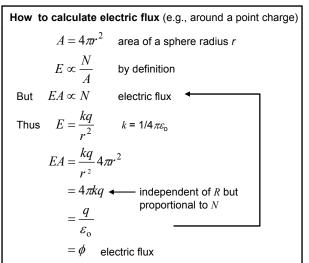
plates

$$E = k \frac{q}{r^2}$$
$$\mathbf{E} = k \frac{q \hat{\mathbf{r}}}{r^2}$$

- Arrows point in the direction of the path taken by a positive test charge placed in the field.
- Number density of lines crossing an area *A* indicates electric field intensity.
- Lines of force start from a positive charge and always terminate on a negative charge (even for an **isolated charge** where the corresponding negative charge may be quite some distance away).

In vector form, the unit vector has a magnitude of 1, but provides direction for the field lines. When q is a positive charge, the electric field E is in the same direction as the unit vector.

Note: for an isolated charge (or charged object) the termination charge is so far away that it contributes little to the field. When the two charges are close together, such as in the parallel plates, both positive and negative charges contribute to the strength of the field. For the plates, O in the formula is the charge on one plate; a factor of 2 has already been included in the formula.



## 1.4 Conductors and Insulators

Atoms consist of a positively charged **nucleus** surrounded by negatively charged **electrons**. Solids consist of a fixed arrangement of atoms usually arranged in a lattice. The position of individual atoms within a solid remains constant because **chemical bonds** hold the atoms in place. The behaviour of the outer electrons of atoms is responsible for the formation of chemical bonds. These outer shell electrons are called **valence electrons**.

#### 1. Conductors

Valence electrons are weakly bound to the atomic lattice and are free to move about from atom to atom.

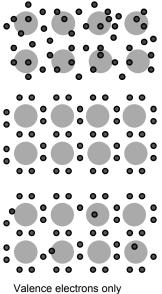
#### 2. Insulators

Valence electrons are tightly bound to the atomic lattice and are fixed in position.

#### 3. Semiconductors

In **semiconductors**, valence electrons within the crystal structure of the material are not as strongly bound to the atomic lattice and, if given enough energy, may become mobile and free to move just as in a conductor.

valence electrons



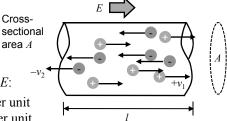
shown in these figures

Electrons, especially in conductors, are **mobile charge carriers** (they have a charge, and they are mobile within the atomic lattice).

## 1.5 Electric Current

**Mobile charge carriers** may be either positively charged (e.g., positive ions in solution) or negatively charged (e.g., negative ions, loosely bound

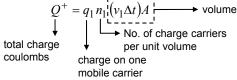
valence electrons). Consider the movement during a time  $\Delta t$  of positive and negative charge carriers in a **conductor** of cross-sectional area A and length l placed in an electric field E:



Let there be  $n_1$  positive carriers per unit volume and  $n_2$  negative carriers per unit

volume. Charge carriers move with drift velocities  $v_1$  and  $-v_2$ . In time  $\Delta t$ , each particle moves a distance  $l = v_1 \Delta t$  and  $l = v_2 \Delta t$ .

The total positive charge exiting from the right (and entering from the left) during  $\Delta t$  is thus:



The total negative charge exiting from the left is:  $Q^- = (-q_2)n_2(-v_2\Delta t)A$ The total net movement of charge during  $\Delta t$  is thus:

 $Q^{+} + Q^{-} = q_1 n_1 v_1 A \Delta t + (-q_2) n_2 (-v_2) A \Delta t$ 

The total charge passing any given point in coulombs per second is called electric current:  $Q^+ + Q^-$ 

$$\frac{Q^{+} + Q}{\Delta t} = q_1 n_1 v_1 A + (-q_2) n_2 (-v_2) A$$
  
of  $\longrightarrow I = A(q_1 n_1 v_1 + (-q_2) n_2 (-v_2))$ 

1 amp is the rate of flow of electric charge when one coulomb of electric charge passes a given point in an electric circuit in one second.

Current density J = I/Aamps m<sup>-2</sup> or coulombs m<sup>-2</sup> s<sup>-1</sup>

In general,

$$i = \frac{dq}{dt}$$

Lower case quantities refer to instantaneous values. Upper case refers to steady-state or DC values. In metallic conductors, the mobile charge carriers are negatively charged electrons; hence  $n_1 = 0$ .

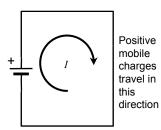
Note that the **amp** is a measure of quantity of charge per second and on its own provides no information about the net drift <u>velocity</u> of the charge carriers ( $\approx 0.1 \text{ mm s}^{-1}$ ).

# 1.6 Conventional Current

Electric current involves the net flow of electrical charge carriers, which, in a metallic conductor, are negatively charged electrons. Often in circuit analysis, the physical nature of the actual flow of charge is not important whether it be the flow of free electrons in a wire or the movement of positive ions in a solution.

> But, in the 1830s, no one had heard of the **electron**. At that time, Faraday noticed that when current flowed through a wire connected to a chemical cell, one electrode, the **anode**, lost weight and the other electrode, the **cathode**, gained weight. Hence it was concluded that charge carriers, whatever they were, flowed through the wire from the anode to the cathode. The anode was therefore thought to be positively charged with electricity and these electric charges went from the anode to the cathode through the wire.

We now know that the gain and loss of weight at each electrode is due to movement of both positive and negative ions in the solution of the cell rather than movement of charge carriers in the wire and in fact, negatively charged electrons flow from the anode to the cathode along the wire. The anode is charged with electricity all right, but the electric charges there are negative and flow towards the cathode.

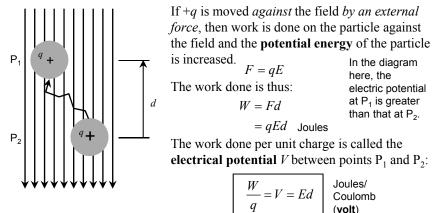


For historical reasons, all laws and rules for electric circuits are based on the direction that would be taken by positive charge carriers if they were present, and mobile, in the wire. Thus, in all circuit analysis, *imagine* that current flows due to the motion of positive charge carriers. Current then travels from positive to negative. This is called **conventional current**.

If we need to refer to the actual *physical process* of conduction, then we refer to the specific charge carriers appropriate to the conductor being considered.

#### 1.7 Potential Difference

When a particle carrying an electric charge is moved from one point  $P_1$  to another  $P_2$  in an electric field, its potential energy is changed since this movement involved a force *F* moving through a distance *d*.



If a charged particle is released in

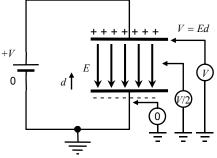
the field, then work is done by the field on the particle and it acquires **kinetic** energy (= $1/2mv^2$  where v is the velocity acquired after travelling a distance d) and loses potential energy. The force acting on the particle is proportional to the field strength E. The stronger the field, the larger the force – the greater the acceleration and the greater the velocity at distance d.

A uniform electric field E exists between two parallel charged plates since a positive test charge placed anywhere within this region will experience a downwards force of the same value. The electric field also represents a

#### potential gradient.

If the negative side of the circuit is grounded (where we set our reference potential to be zero), then the electrical potential at the negative plate is zero and increases uniformly through the space between the plates to the top plate, where it is +V.

The potential gradient (in volts per metre) is numerically equal to the **electric field strength** (newtons per coulomb) but is opposite in direction.

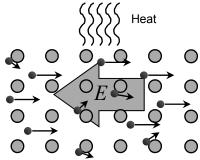


In a *uniform* electric field, the potential decreases uniformly along the field lines and is a potential gradient.

#### 1.8 Resistance

A voltage source, utilising chemical or mechanical means, raises the electrical potential of mobile charge carriers (usually electrons) within it. There is a net build up of charge at the terminals of a voltage source. This net charge results in an **electric field** which is channelled through the conductor. Mobile electrons within the conductor thus experience an electric force and are accelerated.

However, as soon as these electrons move through the conductor, they suffer collisions with other electrons and fixed atoms and lose velocity and thus some of their kinetic energy. Some of the fixed atoms correspondingly acquire **internal energy** (vibrational motion) and the **temperature** of the conductor rises. After collision, electrons are accelerated once more and again suffer more collisions.



Note: negatively charged electrons move in the opposite direction to that of electric field *E*.

Alternate accelerations and decelerations result in a net average velocity of the mobile electrons (called the **drift velocity**) which constitutes an electric current. **Electrical potential energy** is converted into **heat** within the **conductor**. The opposition to the free flow of electrons is called electrical **resistance**.

Experiments show that, for a particular specimen of material, when the applied voltage is increased, the current increases. For most materials, doubling the voltage results in a doubling of the current. That is, the current is directly proportional to the voltage:  $I \propto V$ 

$$\boxed{\frac{V}{I} = R}$$
 Ohm's law

Units: **ohm**  $\Omega$ 

$$P = VI$$
  
but 
$$V = IR$$
  
thus 
$$P = I^2 R$$

The constant of proportionality is called the **resistance**. Resistance limits the current flow through a material for a particular applied voltage. The rate at which electrical potential energy is converted into heat is the **power** dissipated by the resistor. Since electrical potential is in joules/coulomb, and current is measured in coulombs/second, then the product of voltage and current gives joules/second, which is **power** (in **watts**).

# 1.9 Resistivity

Experiments show that the **resistance** of a particular specimen of material (at a constant temperature) depends on three things:

- the length of the conductor, *l*
- the cross-sectional area of the conductor, A
- the type of material,  $\rho$

The material property which characterises the ability of a particular material to conduct electricity is called the **resistivity**  $\rho$ (the inverse of which is the **conductivity**  $\sigma$ ).

<b>Material</b>	$\rho$ Ω m @ 20 °C
silver	1.64 × 10 <sup>-8</sup>
copper	1.72 × 10 <sup>-8</sup>
aluminium	2.83 × 10 <sup>-8</sup>
tungsten	$5.5 imes10^{-8}$

The resistance R (in ohms) of a particular length l of material

of cross-sectional area A is given by:

 $\frac{V}{I} = \rho \frac{I}{A}$  The quantity

but  $E = \frac{V}{I}$  the current density J.

I/A is called

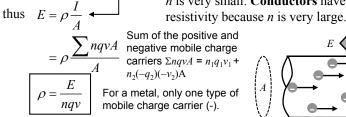
Now, V = IR

hence  $=I\frac{\rho l}{\Lambda}$ 

$$R = \rho \frac{l}{A}$$
 The units of  $\rho$  are  $\Omega$  m, the units of  $\sigma$  are S m<sup>-1</sup>.

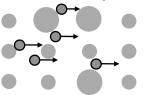
The number density of mobile charge carriers *n* depends on the material. If the

number density is large, then, if E (and hence v) is held constant, the **resistivity** must be small. Thus, the resistivity depends inversely on n. **Insulators** have a high resistivity since n is very small. **Conductors** have a low resistivity because n is very large.



For a particular specimen of material, n, q, A and l are constants. Increasing the applied field E results in an increase in the **drift velocity** v and hence an increase in current I.

The **resistivity** of a pure substance is lower than that of one containing impurities because the mobile electrons are more likely to travel further and acquire a larger velocity when there is a regular array of stationary atoms in the conductor.



Presence of impurity atoms decreases the average drift velocity.

# 1.10 Variation of Resistance

Consider an applied voltage which generates an electric field E within a conductor of resistance R and of length l and area A.

#### 1. Variation with area

Evidently, if the area A is increased, there will be more mobile charge carriers available to move past a given point during a time  $\Delta t$  under the influence of the field and the current I increases. Thus, for a particular specimen, the resistance decreases with increasing cross-sectional area.

#### 2. Variation with length

Now, the field E acts over a length *l*.

$$V = El$$

If the applied voltage is kept constant, then it is evident that if l is increased, E must decrease. The drift velocity depends on E so that if E decreases, then so does v, and hence so does the current.

#### 3. Variation with temperature

Increasing the **temperature** increases

the random thermal motion of the atoms in the conductor thus increasing the chance of collision with a mobile electron and reducing the average drift velocity and increasing the resistivity. Different materials respond to temperature according to the **temperature coefficient of resistivity**  $\alpha$ .

$$\rho_T = \rho_0 \left[ 1 + \alpha (T - T_0) \right]$$

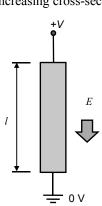
$$R_T = R_0 \left[ 1 + \alpha (T - T_0) \right]$$

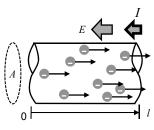
$$R_T = \text{resistance at } T$$

$$R_0 = \text{resistance at } T_0 \text{ (usually 0 °C)}$$
This formula applies to a conductor, not a semi-conductor.  

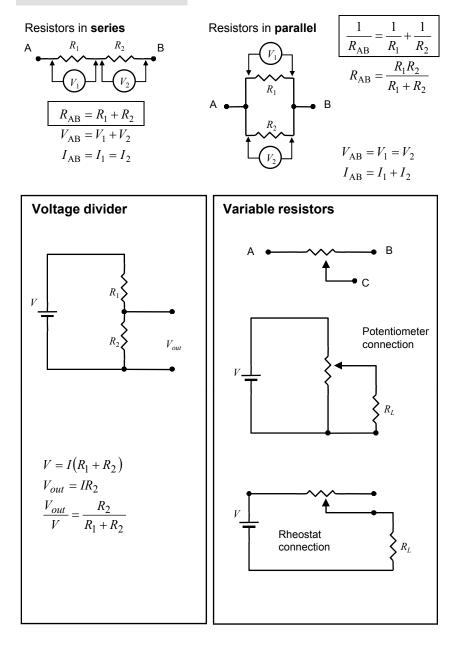
$$Material \qquad \alpha (C^{-1} \Omega^{-1})$$

$$U = \frac{1}{2} \sum_{\alpha \in \mathbb{Z}^{n-1}} \frac{1}{2} \sum_{\alpha \in \mathbb{Z}^{n$$

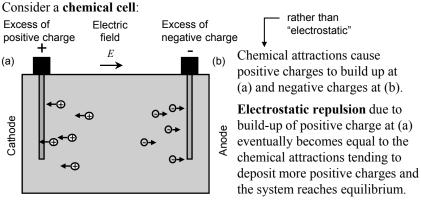




# 1.11 Resistor Circuits



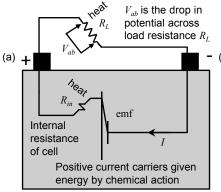
# 1.12 Electromotive Force



The emf (electromotive force) is defined as the amount of energy expended by the cell in moving 1 coulomb of charge from (b) to (a) within the cell. "Force" is a poor choice of At open-circuit,  $emf = V_{ab}$ 

words since emf is really "energy" (joules per coulomb).

Now connect an external load  $R_L$  across (a) and (b). The terminal voltage  $V_{ab}$  is now reduced.



The circuit has been drawn to emphasise where potential drops and rises occur.

Loss of positive charge from (a) reduces the accumulated charge at (a) and hence

(b) chemical reactions proceed and more positive charges are shifted from (b) to (a) within the cell to make up for those leaving through the external circuit. Thus, there is a steady flow of positive charge through the cell and through the wire. Assume positive carriers -

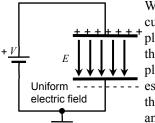
conventional current flow.

But, the continuous conversion of chemical potential energy to electrical energy is not 100% efficient. Charge moving within the cell encounters internal resistance, which, in the presence of a current *I*, means a voltage drop so that:

At closed-circuit,  $emf = V_{ab} + IR_{in}$ 

## 1.13 Capacitance

Consider two **parallel plates** across which is placed a voltage V.



When a voltage V is connected across the plates, current begins to flow as charge builds up on each plate. In the diagram, **negative charge** builds up on the lower plate and **positive charge** on the upper plate. The accumulated charge on the two plates establishes an electric field between them. Since there is an electric field between the plates, there is an electrical potential difference between them.

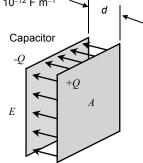
For a **point charge** in space, *E* depends on the distance r away from the charge:  $E = \frac{1}{4\pi\varepsilon_0} \frac{q}{r^2}$ But, for parallel plates holding a total charge O on each plate, calculations show that the electric field *E* in the region between the plates is proportional to the magnitude of the charge *Q* and inversely proportional to the area A of the plates. For a given accumulated charge +O and -Q on each plate, the field E is independent of the distance between the plates.

$$E = \frac{Q}{\varepsilon_0 A}$$
Now,  $V = Ed$ 
thus  $V = \frac{Q}{\varepsilon_0 A}d$ 

*Q* in these formulas refers to the charge on ONE plate. Both positive and negative charges contribute to the field E. A factor of 2 has already been included in these formulas.



permittivity of free space = 8.85 × 10<sup>-12</sup> F m<sup>-1</sup>



A charged particle released between the plates will experience an accelerating force.

Capacitance is defined as the ratio of the magnitude of the charge on each plate (+O or -O) to the potential difference between them.

A large capacitor will C =store more charge for every volt across it than a small capacitor.

$$= \frac{Q}{V} \quad \text{but } V =$$

$$= Q \frac{\varepsilon_0 A}{Q d} \quad \text{if the with a set of the se$$

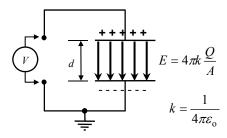
Units: farads

but 
$$V = \frac{Q}{\varepsilon A}d$$

space between the plates is filled a dielectric, then capacitance is increased by a factor  $\varepsilon_r$ . A dielectric is an insulator whose atoms become polarised in the electric field. This adds to the storage capacity of the capacitor.  $C = \mathcal{E}_r \mathcal{E}_0 \frac{A}{d}$ 

#### 1.14 Capacitors

If a capacitor is charged and the voltage source V is then disconnected from it, the accumulated charge remains on the plates of the capacitor.



Since the charges on each plate are opposite, there is an **electrostatic** force of attraction between them but the charges are kept apart by the gap between the plates. In this condition, the capacitor is said to be  $k = \frac{1}{4\pi\varepsilon_0}$  charged. A voltmeter placed across the terminals would read the voltage V used to charge the capacitor.

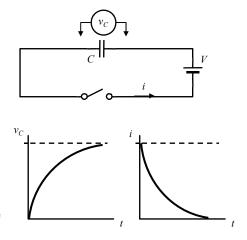
When a **dielectric** is inserted in a capacitor, the molecules of the dielectric align themselves with the applied field. This alignment causes a field of opposite sign to exist within the material, thus reducing the overall net field. For a given applied voltage, the total net field within the material is small for a material with a high **permittivity**  $\varepsilon$ . The permittivity is thus a measure of how easily the charges within a material line up in the presence of an applied external field. In a conductor, charge carriers not only align but

If the plates are separated by a dielectric, then the field *E* is reduced. Instead of using  $\varepsilon_o$ , we must use  $\varepsilon$  for the substance. Often, the **relative permittivity**  $\varepsilon_r$  is specified.

$\varepsilon_r = \frac{\varepsilon}{\varepsilon_0}$	<b>Material</b> Vacuum Water Glass	<i>ɛ</i> , 1 80 8
0	Glass	8

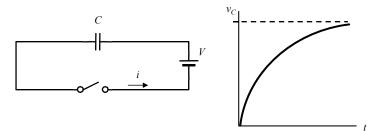
When a capacitor is connected across a voltage source, the current in the circuit is initially very large and then decreases as the capacitor charges. The voltage across the capacitor is initially zero and then rises as the capacitor charges.

In a conductor, charge carriers not only align but actually move under the influence of an applied field. This movement of charge carriers completely cancels the external field. The net electric field within a conductor placed in an external electric field is zero!



# 1.15 Energy Stored in a Capacitor

**Energy** is required to charge a capacitor. When a capacitor is connected across a voltage source, the current in the circuit is initially very large and then decreases as the capacitor charges. The voltage across the capacitor is initially zero and then rises as the capacitor charges.



Energy is expended by the voltage source as it forces charge onto the plates of the capacitor. When fully charged, and disconnected from the voltage source, the voltage across the capacitor remains. The stored electric potential energy within the charged capacitor may be released when desired by discharging the capacitor.

Power 
$$P = vi$$
  
 $i = \frac{dq}{dt}$   
 $Pdt = vdq = dU$   
 $U = \int_{0}^{Q} vdq$  Energy  
 $= \int_{0}^{Q} \frac{q}{C}dq$   $C = \frac{q}{v}$   
 $= \frac{1}{2}\frac{Q^{2}}{C}$   $C = \frac{Q}{V}$   
Energy stored  
in a capacitor  $U = \frac{1}{2}CV^{2}$ 

# 1.16 Capacitor Circuits

#### Capacitors in series

$$Q = Q_1 = Q_2 = Q_3$$

$$V = V_1 + V_2 + V_3$$

$$C_{total} = \frac{Q}{V} \quad \text{charge on one plate}$$

$$V_1 = \frac{Q}{C_1}; V_2 = \frac{Q}{C_2}; V_3 = \frac{Q}{C_3}$$

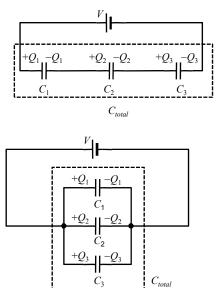
$$V = Q \left(\frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}\right)$$

$$\frac{1}{C_{total}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

Capacitors in parallel

$$\begin{aligned} +Q &= Q_1 + Q_2 + Q_3 \\ V &= V_1 = V_2 = V_3 \\ C_{total} &= \frac{Q}{V} \\ V_1 &= \frac{Q_1}{C_1}; V_2 = \frac{Q_2}{C_2}; V_3 = \frac{Q_3}{C_3} \\ Q &= V_1 C_1 + V_2 C_2 + V_3 C_3 \\ &= V (C_1 + C_2 + C_3) \\ \frac{Q}{V} &= C_1 + C_2 + C_3 \\ &= C_{total} \end{aligned}$$

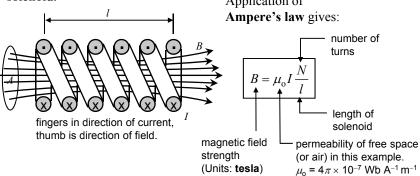
The combination of capacitors behaves like one large capacitor  $C_{total}$  with charge  $+Q_1$  on one end and  $-Q_3$  at the other end and so  $+Q_1 = +Q_2...$ 



In this case, the same voltage is applied across all capacitors and since C = Q/V, Q must distribute itself according to C for each capacitor.

# 1.17 Inductance

In a conductor carrying a steady electric current, there is a magnetic field around the conductor. The magnetic field of a current-carrying conductor may be concentrated by winding the conductor around a tube to form a **solenoid**. Application of



When the current in the coil changes, the resulting change in **magnetic flux** induces an emf in the coil (**Faraday's law**).

emf = 
$$-\frac{d\Phi}{dt}$$
 magnetic flux  
=  $-\mu_0 A \frac{N}{l} \frac{di}{dt}$  where  $B = \frac{\Phi}{A} = \mu_0 I \frac{N}{l}$   
magnetic field cross-sectional area of coil

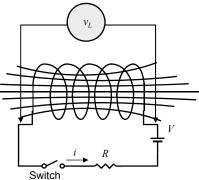
But, this is the emf induced in *each loop* of the coil. Each loop lies within a field *B* and experiences the changing current. The *total* emf induced between the two ends of the coil is thus *N* times that for one loop:

emf = 
$$-\left[\mu_0 A \frac{N^2}{l}\right] \frac{di}{dt}$$
 The induced emf tends to oppose the change in current (Lenz's law).  
Inductance:  $L = \mu_0 A \frac{N^2}{l}$  determines the magnitude of the emf induced within the coil for a given rate of change of current.

# 1.18 Inductors

In a circuit with an inductor, when the **switch** closes, a changing current results in a changing magnetic field around the coil. This *changing* magnetic field induces a voltage (emf) in the loops (Faraday's law) which tends to oppose the applied voltage (Lenz's law). Because of the self-induced opposing emf, the current in the circuit does not rise to its final value at the instant the circuit is closed, but grows at a rate which depends on the **inductance** (in **henrys**, L) and resistance (R) of the circuit. As the current increases, the *rate of change* of current decreases and the magnitude of the opposing voltage decreases. The current reaches a maximum value I when the opposing voltage drops to zero and all the voltage appears across the resistance R.

voltage induced by



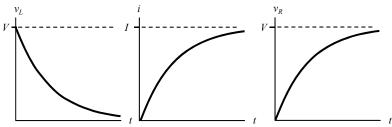
When the switch is closed, the rate of change of current is controlled by the value of *L* and *R*. Calculations show that the voltage across the inductor is given by: Rt

$$v_I = V e^{-L}$$

the changing current  $v_L = -L \frac{di}{dt}$ The minus sign indicates that if the current is decreasing (*dildt*) rate of change of current through the inductor

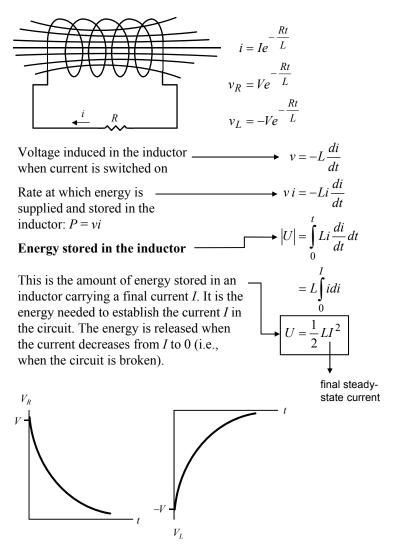
the current is decreasing (di/dt is negative) then the voltage  $v_L$  induced in the coil is positive (i.e., same direction as V).





## 1.19 Discharge and Stored Energy

Establishing a current in an inductor requires energy which is stored in the **magnetic field**. When an inductor is discharged, this energy is released. If the inductor is discharged through a resistor as shown, then the rate of decrease in current in the circuit is given by:

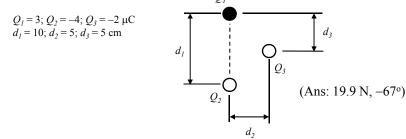


#### 1. Electricity

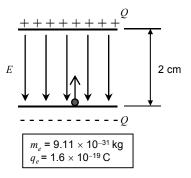
## 1.20 Review Questions

 A negative charge of -0.1 μC exerts an attractive force of 0.5 N on an unknown charge at a distance of 0.5 m. Determine the magnitude (and sign) of the unknown charge. (Ans: 138.9 μC)

2. Three electrically charged billiard balls are placed at positions as shown in the diagram. Determine the magnitude and direction of the resulting forces on the black ball.  $Q_I$ 



3. A uniform electric field exists between two oppositely charged parallel plates. An electron is released from rest at the surface of the negatively charged plate and strikes the surface of the positively Echarged plate. The distance between the plates is 2 cm and it takes  $1.5 \times 10^{-8}$ seconds for the electron to travel from one plate to the other. (a) Find the electric field strength, and (b) the velocity of the electron as it strikes the positively charged plate.



(Ans: 1012 NC<sup>-1</sup>,  $2.67 \times 10^{6} \text{ ms}^{-1}$ )

4. A steady current of 6 A is maintained in a metallic conductor. What charge (in coulombs) is transferred through it in 1 minute?

(Ans: 360 C)

Two parallel plates are 1 cm apart and are connected to a 500 V source. What force will be exerted on a single electron half way between the plates? (Ans: 8 × 10<sup>-15</sup> N)

6. Calculate the resistance of 100 m of copper wire which has a diameter of 0.6 mm.

(Ans:  $6.08 \Omega$ )

- 7. A steady voltage source V = 1 V is connected to a coil which consists of a 50 m length of copper wire of radius 0.01 mm. Given that the number density of mobile electrons in copper is  $8.5 \times 10^{22}$  cm<sup>-3</sup> and  $\rho = 1.72 \times 10^{-8} \Omega$  m, calculate:
  - (a) the electric field *E* which acts on the mobile electrons in the coil.
  - (b) the drift velocity v of the mobile electrons.
  - (c) the resistance *R* of the coil.
  - (d) the steady DC current *I* in the coil.

(Ans:  $0.02 \text{ V m}^{-1}$ ;  $8.6 \times 10^{-5} \text{ m s}^{-1}$ ; 2738 W; 0.36 mA)

8. A fuse in a motor vehicle electrical system has a resistance of  $0.05 \Omega$ . It is designed to blow when the power dissipation exceeds 50 W. What is the current rating of the fuse?

(Ans: 31.6 A)

9. A 12 volt battery in a motor vehicle is capable of supplying the starter motor with 150 A. It is noticed that the terminal voltage of the battery drops to 10 V when the engine is cranked over with the starter motor. Determine the internal resistance of the 12 volt battery.

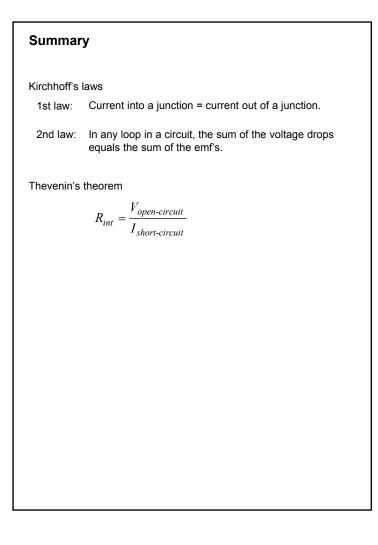
(Ans:  $0.013 \Omega$ )

- 10. A capacitor consists of two parallel plates each of area 200 cm<sup>2</sup> separated by an air gap of 0.4 mm thickness. 500 V is applied. Calculate:
  - (a) capacitance of this capacitor;
  - (b) charge on each plate;
  - (c) energy stored in the capacitor;
  - (d) electric field strength between the plates.

(Ans: 442 pF,  $2.24 \times 10^{-7}\,C,\, 5.6 \times 10^{-5}\,J,\, 1.25 \times 10^{6}\,V\,m^{-1})$ 

A coil has an inductance of 5 H and a resistance of 20 Ω. If a DC voltage of 100 V is applied to the coil, find the energy stored in the coil when a steady maximum current has been reached. (Ans: 62.5 J)

# 2. DC Circuits



60 Ω

**20** Ω

9 V

## 2.1 Superposition

In a circuit containing several sources of emf, the current flowing in any branch of the circuit will be equal to the sum of the **current components** that would flow in the branch if each source of emf were to be acting alone.

6 V

Example:

Find the current in the 20  $\Omega$  resistor in the circuit shown.

Solution:

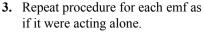
We proceed as follows: replace all sources with their **internal** 

**resistances** except one and calculate the current component flowing in the branch of interest by combining resistors in serial or parallel as required.

1. Combine 60 and  $20 \Omega$  into one resistance.

2. Analyse for unknown current *component*.

$$R_{60,20} = \left(\frac{1}{20} + \frac{1}{60}\right)^{-1}$$
  
= 15 \Omega  
$$R_T = 15 + 30$$
  
= 45  
$$I_1 = \frac{6}{45}$$
  
= 0.133 \A  
$$V_{ab} = (0.133)(15)$$
  
= 1.995 \V  
$$I_2 = \frac{1.995}{20}$$
  
= 0.1 \A



3 V

**30** Ω

$$R_{60,30} = 20 \Omega$$

$$R_T = 20 + 20$$

$$= 40 \Omega$$

$$I_2 = \frac{3}{40}$$

$$= 0.075 \text{ A}$$

$$R_{30,20} = 12 \Omega$$

$$R_T = 72 \Omega$$

$$I_3 = \frac{9}{72}$$

$$= 0.125 \text{ A}$$

$$V_{ab} = 0.125(12)$$

$$= 1.5 \text{ V}$$

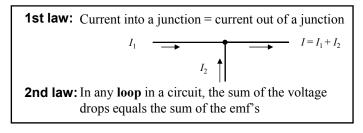
$$I_2 = \frac{1.5}{20}$$

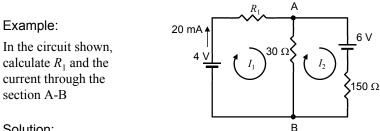
$$= 0.075 \text{ A}$$
4. Add current components together for final answer.

$$I_{total} = 0.1 + 0.075 + 0.075$$
$$= 0.25 \text{ A}$$

#### 2. DC Circuits

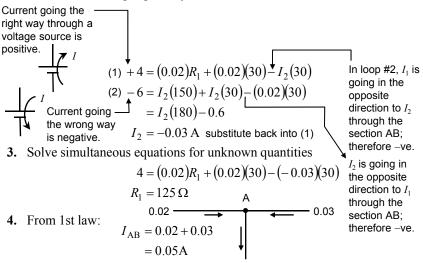
### 2.2 Kirchhoff's Laws





Solution:

- 1. Divide the circuit up into **current loops** and draw an arrow which indicates the direction of current assigned to each loop (the direction you choose need not be the correct one. If you guess wrongly, then the current will simply come out negative in the calculations).
- 2. Consider each loop separately:



## 2.3 Kirchhoff's Laws Example

Determine the current in the two 1  $\Omega$  resistors in the following circuit.

0

0

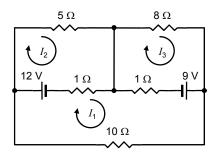
1

0

0

1

0



(1) 
$$-12 + 9 = I_1(10 + 1 + 1) + -I_2(1) - I_3(1)$$
  
 $-3 = 12I_1 - I_2 - I_3$   
(2)  $12 = I_2(5+1) - I_1(1)$ 

(3)  $-9 = I_3(8+1) - I_1(1)$ 

Three simultaneous equations. Solve by matrix method to give:

$$I_1 = -0.170 \text{ A}$$
  
 $I_2 = 1.972 \text{ A}$   
 $I_3 = -1.019 \text{ A}$ 

Thus:

$$I_2 - I_1 = 1.972 - 0.170$$
  
= 2.142 A  $\leftarrow$   
 $I_1 - I_3 = -0.170 - -1.019$   
= 0.849 A  $\rightarrow$ 

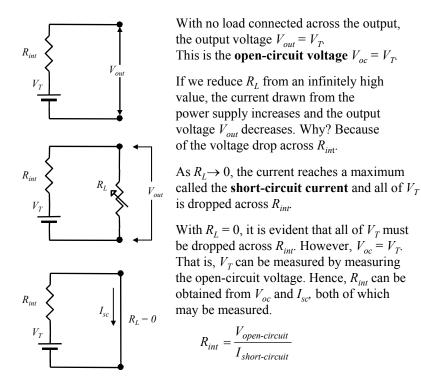
The minus signs indicate that the currents  $I_1$  and  $I_3$  are opposite in direction to that shown in the diagram above.

Arrange coefficients in this format. The aim is to obtain a pattern of 0's and 12 -1 -1 -3 1's on the left to give the 0 12 -1 6 value of the unknown -1 0 9 -9 values on the right by manipulating rows (R). 1 0 | -12 |-6 Swap R1, R2 and multiply 12 -1| -3-1 new R1 by -1 -1 0 9 -9 0 - 121 -6 Add  $-12 \times R1$  to R2 71 -1 141 Add R1 to R3 -6 9 -21 -6 0 -12 Divide R2 by 71 -0.014 1.986 1 -21 -6 9 0 -0.084 -0.084 Add  $6 \times R2$  to R1 1 -0.014 1.986 Add  $6 \times R2$  to R3 0 0 8.916 -9.084  $|1 \quad 0 \quad 0 \quad |-0.170| \longleftarrow I_1$  Divide R3 by 8.916 0 1 0 1.972 🗲  $-I_2$  Add 0.014  $\times$  R3 to R2  $-I_3$  Add 0.084 × R3 to R1 0 0 1 -1.019

### 2. DC Circuits

# 2.4 Thevenin's Theorem

Consider a voltage source  $V_T$  with internal resistance  $R_{int}$ .

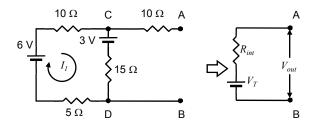


 $V_T$  and  $R_{int}$  are useful tools for reducing a complicated power supply circuit to a simpler circuit. This is Thevenin's theorem. That is, any **two-terminal voltage source**, no matter how complicated, can be represented by  $V_T$  and  $R_{inr}$ 

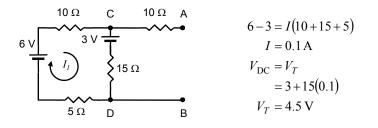
Analysis	Measurement	
1. Calculate open-circuit voltage $V_T$ using Kirchhoff or superposition	<ol> <li>Or, measure short-circuit current and open-circuit</li> </ol>	
2. Determine $R_{int}$ by replacing all internal voltage sources with their internal resistances and analysing resistance network	voltage with multimeter to obtain <i>R<sub>int</sub></i>	

### 2.5 Thevenin's Theorem Example

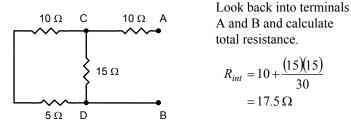
Reduce this circuit to a single voltage source  $V_T$  and internal resistance  $R_{int}$ .



(1) Determine  $V_T$  by calculating **open-circuit voltage** using Kirchhoff or superposition.



(2) Determine  $R_{int}$  by replacing all emf's with their **internal resistances** (zero in this example).



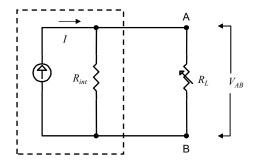
(3) Calculate short-circuit current if desired.

$$I_{sc} = \frac{V_{oc}}{R_{int}} = \frac{4.5}{17.5} = 257 \text{ mA}$$

#### 2. DC Circuits

### 2.6 Norton's Theorem

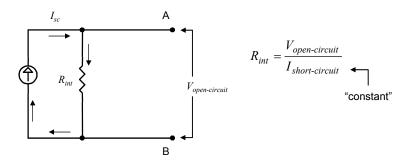
Imagine a black box contains a special generator that produces a completely variable voltage but always produces a **constant current** *I* (equal to the **short-circuit current**).



*I* is a constant.  $V_{AB}$  varies as  $R_L$  varies.

 $R_{int}$  must be in parallel with the power source so that *I* remains constant when  $R_L \rightarrow$  infinity. When  $R_L = 0$ ,  $I = I_{sc} =$ constant.

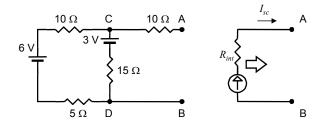
Consider open-circuit conditions:



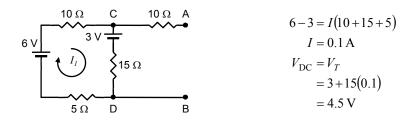
Circuits (or parts thereof) may be reduced to **equivalent circuits** in terms of either **constant voltage** (Thevenin) or **constant current** (Norton) sources with an internal resistance. We shall see shortly that Thevenin and Norton equivalent circuits are exactly the same thing from the point of view of the voltage and current seen by an external load.

## 2.7 Norton's Theorem Example

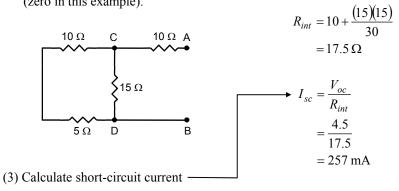
Reduce this circuit to a constant current source  $I_{sc}$  with a parallel internal resistance  $R_{inr}$ 



(1) Determine the open-circuit voltage by Kirchhoff or superposition.



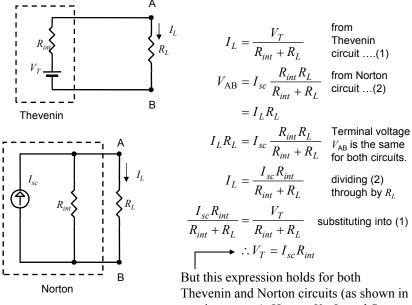
(2) Determine  $R_{int}$  by replacing all emf's with their internal resistances (zero in this example).



#### 2. DC Circuits

### 2.8 Equivalence of Norton and Thevenin

Consider these two representations of a **two-terminal power supply**. If both of these can replace the actual circuitry of the power supply and appear to be the same from the point of view of whatever is connected to the output terminals A and B, then the terminal voltage  $V_{AB}$  and load current  $I_L$  must be the same for each circuit.



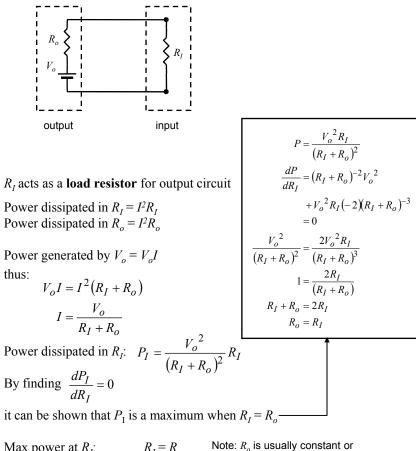
previous pages). Hence,  $V_T$ ,  $I_{sc}$  and  $R_{int}$  are exactly the same for each circuit.

#### Equivalence of Norton and Thevenin

Thevenin and Norton equivalent circuits are two different ways of representing a complicated circuit, either as a simple series or a simple parallel circuit. Which one do we use? It depends on the circuit being analysed. For transistor circuits, the Norton equivalent circuit is better and leads to a simpler analysis because transistors are mostly current controlling devices.

## 2.9 Maximum Power Transfer

Transfer from an output device (e.g., amplifier) to an input device (e.g., loudspeaker)



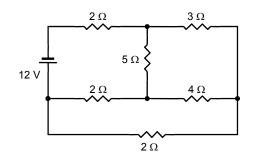
Max power at  $R_I$ : $R_I = R_o$ Max voltage drop  $R_I$ : $R_I >> R_o$ Max current at  $R_I$ : $R_I << R_o$ 

Note:  $R_o$  is usually constant o fixed by the apparatus.

### 2. DC Circuits

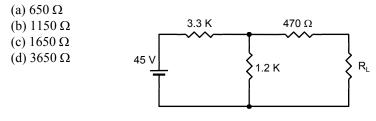
# 2.10 Review Questions

1. Using Kirchhoff's laws, find the current in the 4  $\Omega$  resistor in the network below:



(Ans: 0.122 A)

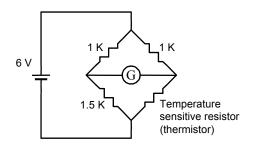
2. Find the current through the load resistor  $R_L$  when it takes the following values:



Hint: use Thevenin's theorem.

(Ans: 6, 4.8, 4, 2.4 mA)

3. A Wheatstone's bridge is used to measure temperature with the aid of a temperature sensitive resistor (a thermistor). If the meter (G) across the bridge has a resistance of 1200  $\Omega$ , and the resistance of the thermistor changes from 1500  $\Omega$  to 1600  $\Omega$  for a change in temperature of 60 °C to 61 °C, determine the change in current through the meter.

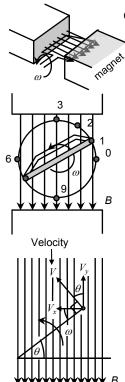


(Ans: 0.038 mA)

# 3. AC Circuits

Summary			
$v = V_p \sin(\omega t)$	Instantaneous voltage		
$V_{rms} = \frac{V_p}{\sqrt{2}} = 0.707 V_p$	rms voltage		
$I_{rms} = \frac{I_p}{\sqrt{2}} = 0.707 I_p$	rms current		
$X_C = \frac{1}{\omega C}$	Capacitive reactance		
$X_L = \omega L$	Inductive reactance		
$P_R = V_{rms} I_{rms}$	Reactive power		
$P_{av} = V_{rms} I_{rms} \cos \phi$	Average (active) power		
$S = V_{rms}I_{rms}$	Apparent power		
$ Z  = \sqrt{R^2 + (X_L - X_C)}$ $\tan \phi = \left[\frac{X_L - X_C}{R}\right]$	$\overline{\big)^2} \qquad Z = R + j \big( X_L - X_C \big)$ Impedance $= R + j \bigg( \omega L - \frac{1}{\omega C} \bigg)$		
$\frac{V_{out}}{V_{in}} = \frac{1}{\sqrt{1 + R^2 \omega^2 C^2}}$	Low-pass filter		
$\frac{V_{out}}{V_{in}} = \frac{R\omega C}{\sqrt{R^2 \omega^2 C^2 + 1}}$	High-pass filter		
$R\omega C = 1$	3 dB point		

# 3.1 AC Voltage



Consider a conductor at constant angular speed ( $\omega$ ):

- at (0) motion of conductor is parallel to *B*, hence induced voltage = 0;
- at (1), conductor has begun to cut magnetic field lines *B*, hence some voltage is induced;
- at (2), conductor cuts magnetic field lines at a greater rate than (1) and thus a greater voltage is induced;
- at (3), conductor cuts magnetic field lines at maximum rate, thus maximum voltage is induced;
- from (3) to (6), the rate of cutting becomes less;
- at (6), conductor moves parallel to B and v = 0;
- from (6) to (9), conductor begins to cut field lines again but in the opposite direction, hence induced voltage is reversed in polarity.

The **induced voltage** is directly proportional to the rate at which the conductor cuts across the magnetic field lines. Thus, the induced voltage is proportional to the velocity of the conductor in the x direction ( $V_x = V \sin q\theta$ ). The velocity component  $V_y$  is parallel to the field lines and thus does not contribute to the rate of "cutting."

Right-hand rule: • fingers: direction of field

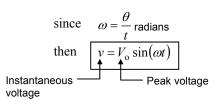
- thumb: direction of  $V_x$
- palm: force on *positive* charge carriers
- Thus, current is coming out from the page.

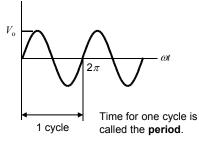
 $v_{induced} = V_{o} \sin \theta$ 

 $\rightarrow$  maximum (peak) voltage  $V_0$  induced at  $\theta = \pi/2$ 

 $V_{o}$  depends on:

- total number of flux lines through which the conductor passes
- angular velocity of loop
- no. turns of conductor in loop





### 3.2 Resistance

The **instantaneous voltage** across the resistor is:  $v_r = V_p \sin \omega t$ Maximum value of V The **instantaneous**  $i = \frac{v}{R}$ current in the resistor is: The maximum current in the resistor is when sin  $\omega t = 1$  thus:  $V_p \sin \omega t$  $I_p = \frac{V_p}{R}$  $\therefore i = I_p \sin \omega t$ 

#### Instantaneous power:

$$p = vi$$

$$= i^{2}R$$

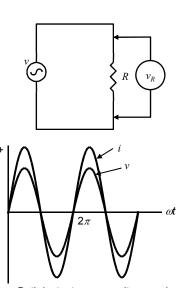
$$= (I_{p} \sin \omega t)^{2}R$$

$$= I_{p}^{2}R \sin^{2} \omega t$$

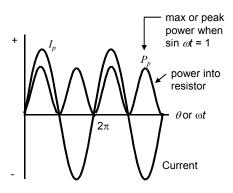
$$P_{p} = I_{p}^{2}R$$

$$p = P_{p} \sin^{2} \omega t$$

- power is a function of  $\sin^2 \omega t$
- power is sinusoidal in nature with a frequency of twice the instantaneous current and voltage and is always positive, indicating power continuously supplied to the resistor.



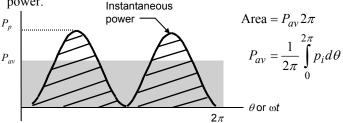
Both instantaneous voltage and current are functions of ( $\omega t$ ). Thus, they are "in-phase."



**Resistance** is the opposition to alternating current due to the motion of charge carriers within the resistor. The opposition tendered depends upon the magnitude of voltage across the resistor.

### 3.3 rms Voltage and Current

The area under the power vs time function is energy. Thus, it is possible to calculate an average power level which, over one voltage cycle, is associated with the amount of energy carried in two cycles of instantaneous power.



This energy would be that given by an equivalent DC, or steady-state, voltage and current over a certain time period compared to that from an alternating current and voltage for the same time period.

Average power:  $2\pi$ 

 $=\frac{1}{2\pi}\int_{0}^{2\pi}i^{2}Rd\theta$ 

 $=\frac{R}{2\pi}\int_{0}^{2\pi}i^{2}d\theta$ 

 $=\frac{I_p^2 R}{2\pi} \int_{0}^{2\pi} \sin^2 \theta d\theta$ 

 $=\frac{{I_p}^2 R}{2}$  this integral evaluates

 $P_{av} = \frac{\int_{0}^{\infty} p_i d\theta}{2\pi}$ 

Now: 
$$P_{av} = \frac{I_p^2}{2}R$$

What equivalent steady-state current and voltage would give the same average power as an alternating current and voltage?

Let:	$I_{rms} = \frac{I_p}{\sqrt{2}}$	This result is only for sinusoidal signals.

Thus:  $P_{av} = I_{rms}^2 R$  For resistor circuit only. See later for LCR series circuit.

 $I_{rms}$  and  $V_{rms}$  are  $= \frac{R}{2\pi} \int_{0}^{2\pi} I_p^2 \sin^2 \theta d\theta = \frac{I_p}{\sqrt{2}} \int_{0}^{2\pi} \frac{I_{rms} V_{rms}}{\sqrt{2}} = \frac{V_p}{\sqrt{2}}$   $= \frac{I_p^2 R}{2\pi} \int_{0}^{2\pi} \sin^2 \theta d\theta = 0.707 I_p = \frac{V_p}{\sqrt{2}}$   $= 0.707 V_p$   $= 0.707 V_p$ 

general:  

$$V_{rms} = \sqrt{\frac{1}{T} \int_{0}^{T} v^2(t) dt} \qquad I_{rms} = \sqrt{\frac{1}{T} \int_{0}^{T} i^2(t) dt}$$

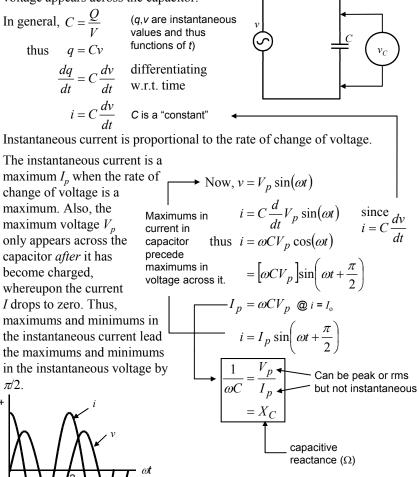
In AC circuits, V and I without subscripts indicate rms values unless stated otherwise.

### 3.4 Capacitive Reactance

 $v = V_p \sin(\omega t)$ 

 $i = I_p \sin\left(\omega t + \frac{\pi}{2}\right)$ 

The AC source supplies an alternating voltage *v*. This voltage appears across the capacitor.

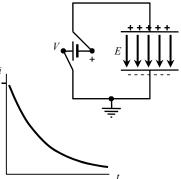


**Capacitive reactance** is the opposition to alternating current by capacitance. The opposition tendered depends upon the rate of change of <u>voltage</u> across the capacitor.

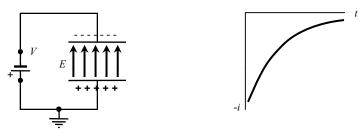
What is capacitive reactance? How can a capacitor offer a **resistance** to alternating current?

Consider a capacitor connected to a DC supply so that the polarity of the applied voltage can be reversed by a switch.

When the switch is first closed, it takes time for the charge Q to accumulate on each plate. Charge accumulation proceeds until the voltage across the capacitor is equal to the voltage of the source. During this time, current flows in the circuit.



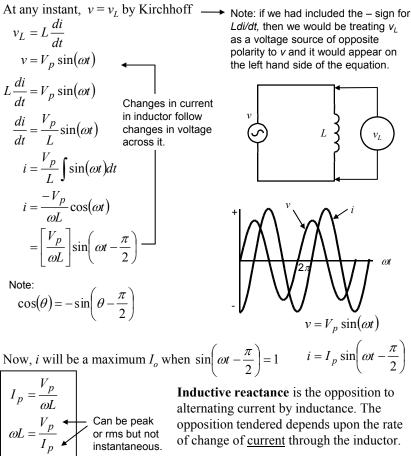
When the polarity is reversed, the capacitor initially discharges and then charges to the opposite polarity. Current flows in the opposite direction while reverse charging takes place until the voltage across the capacitor becomes equal to the supply voltage, whereupon current flow ceases.



Now, if the switch were to be operated very quickly, then, upon charging, the current would not have time to drop to zero before the polarity of the supply voltage was reversed. Similarly, on reverse charging, the reverse current would not have time to reach zero before the polarity of the source was reversed. Thus, the current would only proceed a short distance along the curves as shown and a continuous alternating current would result. The faster the switch over of polarity, the greater the average or rms AC current. Thus, the "resistance" to AC current is greater at lower frequencies and lower at high frequencies.

### 3.5 Inductive Reactance

Let the inductor have no resistance. Thus, any voltage that appears across the terminals of the inductor must be due to the self-induced voltage in the coil by a changing current through it (self-inductance).

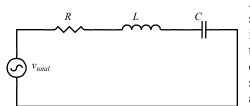


=  $X_I$   $\leftarrow$  inductive reactance ( $\Omega$ )

opposition tendered depends upon the rate of change of current through the inductor.

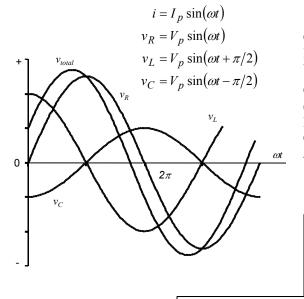
For high frequencies, the magnitude of the induced back emf is large and this restricts the maximum current that can flow before the polarity of the supply voltage changes over. Thus, the reactance increases with increasing frequency.

### 3.6 LCR Series Circuit



A varying voltage  $v_{total}$  from the source will cause a varying instantaneous current *i* to flow in the circuit. Because it is a series circuit, the current must be the same in each part of the circuit at any particular time *t*.

- For the resistance, changes in  $v_R$  are in phase with those of *i*
- For the inductor, changes in  $v_L$  are ahead of those of *i* by  $\pi/2$
- For the capacitor, changes in  $v_c$  follow those of *i* by  $\pi/2$



CAN ONLY ADD INSTANTANEOUS VALUES

CANNOT ADD PEAK (OR RMS) VALUES BECAUSE THEY ARE OUT OF PHASE

- Except for a resistive circuit.

Note: we can put  $v_L$  on the right hand side of this equation as long as we remember that there is a change of sign of Ldi/dt.

From Kirchhoff,  $v_{total} = v_R + v_L^{\dagger} + v_C$  at any instant. Note that each of these voltages do not reach their peak values when  $v_{total}$  reaches a maximum, thus  $|V_{ptotal}| \Leftrightarrow |V_{pR}| + |V_{pL}| + |V_{pC}|$ . Also, since the rms value of any voltage = 0.707  $V_p$ , then  $|Vrms_{total}| \Leftrightarrow |Vrms_R| + |Vrms_L| + |Vrms_C|$ 

Algebraic addition generally only applies to instantaneous quantities (can only be applied to other quantities, e.g., peak or rms, if current and voltage are in phase – such as resistor circuit).

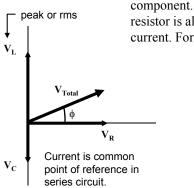
Note also that the resultant of the addition of sine waves of the same frequency is another sine wave of the same frequency.

# 3.7 LCR circuit – Peak and rms Voltage

In an LCR series circuit, how then may the total or <u>resultant</u> peak (or rms) values of voltage and current across the series components be determined from the individual peak (or rms) voltages across each component?

A VECTOR approach is needed (can use **complex numbers**).

Consider the axes below which indicate either peak (or rms) voltages  $V_R$ ,  $V_C$  and  $V_L$ .



In a *series* circuit, the current is the same in each component. The instantaneous voltage across the resistor is always in phase with the instantaneous current. For the inductor and the capacitor:

- $v_L$  precedes  $v_R$  by  $\pi/2$ , therefore peak or rms values of  $V_L$  precede  $V_R$ by  $\pi/2$  and  $V_L$  is drawn upwards on the vertical axis.
- $v_C$  follows  $v_R$  by  $\pi/2$ , therefore peak or rms values of  $V_C$  always follow  $V_R$  by  $\pi/2$  and  $V_C$  is downwards on the vertical axis.

The resultant peak or rms voltage  $V_T$  is the <u>vector</u> sum of  $V_R + V_L + V_C$ 

For an AC series circuit:

- · same current flows in all components
- vector sum of rms or peak voltages must equal the applied rms or peak voltage  $V_T = V_R + V_L + V_C$
- algebraic sum of instantaneous voltages equals the applied instantaneous voltage  $v_{total} = v_R + v_L + v_C$

The angle  $\phi$  is the **phase angle** of the resultant peak (or rms) voltage w.r.t. the peak (or rms) common current and is found from:

$$\tan\phi = \frac{V_L - V_C}{V_R}$$

Magnitudes of the peak or rms voltages

In complex number form:

$$V_T = V_R + j \big( V_L - V_C \big)$$

Complex numbers are a convenient mathematical way to keep track of directions or "phases" of quantities.

I

# 3.8 Impedance

The total opposition to current in an AC circuit is called impedance. For a series circuit, the impedance is the vector sum of the resistances and the reactances within the circuit.

Now, from a consideration of the voltages:

$$|V_{T}| = \sqrt{|V_{R}|^{2} + |V_{L} - V_{C}|^{2}}$$

$$\frac{|V_{T}|}{|I|} = \sqrt{\frac{|V_{R}|^{2}}{|I|^{2}} + \frac{|V_{L} - V_{C}|^{2}}{I}}$$
Dividing through by I
$$= \sqrt{R^{2} + |X_{L} - X_{C}|^{2}}$$
since  $R = \frac{V_{R}}{I}$ 

$$= |Z|$$

$$|Z| = \frac{|V|}{|I|}$$
Can multiply and divide magnitudes but must add as vectors
$$X_{L} = \frac{V_{L}}{I}$$

$$|Z| = \sqrt{R^{2} + (X_{L} - X_{C})^{2}}$$

$$tan \phi = \left[\frac{X_{L} - X_{C}}{R}\right]$$
For an RC series circuit:
$$tan \phi = \left[\frac{-X_{C}}{R}\right]$$

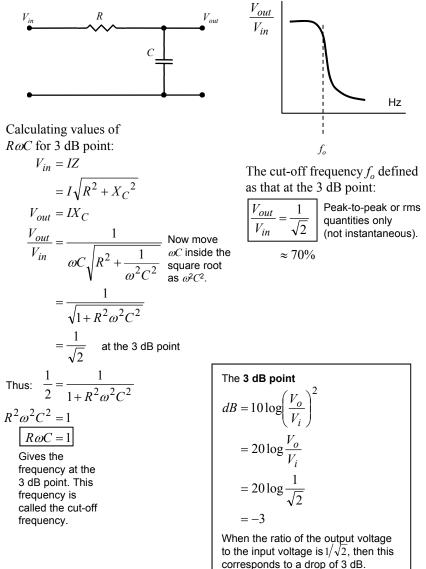
$$tan \phi = \left[\frac{X_{L}}{R}\right]$$

= -R

If  $X_C > X_L$ , circuit is **capacitively reactive**. If  $X_C < X_L$ , circuit is inductively reactive. If  $X_C = X_L$ , circuit is **resonant**.

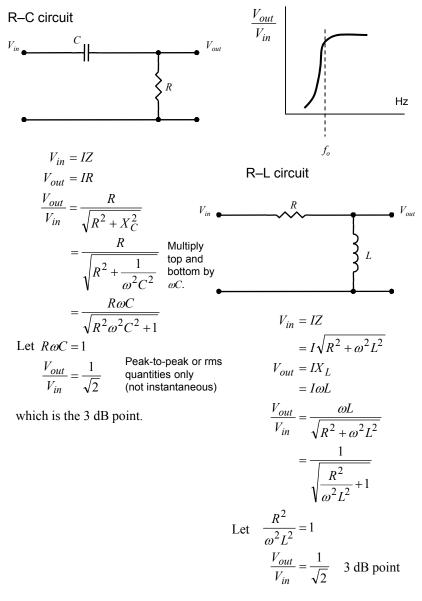
### 3. 9 Low-Pass Filter

In a low-pass filter, low frequencies are let through; high frequencies are attenuated.



### 3.10 High-Pass Filter

In a high-pass filter, high frequencies are let through; low frequencies are attenuated.



### 3. AC Circuits

# 3.11 Complex Impedance (Series)

For a series circuit, the **impedance** is the vector sum of the resistances and the reactances within the circuit.

$$Z = \frac{V}{I} \text{ by definition}$$

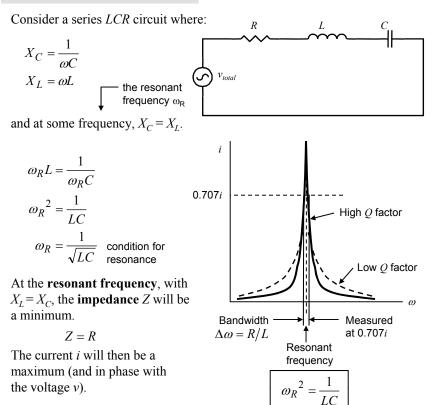
$$V = V_R + j(V_L - V_C)$$

$$\frac{V}{I} = \frac{V_R}{I} + j\frac{(V_L - V_C)}{I}$$
thus
$$Z = R + j\left(\omega L - \frac{1}{\omega C}\right)$$
Note:
$$|Z| = \frac{|V|}{|I|}$$
Magnitudes of the peaks  
or ms voltages. For  
series or parallel circuits,  
cannot simply add peak  
or ms values.
If  $X_C > X_L$ , circuit is **capacitively reactive**.  
If  $X_C > X_L$ , circuit is **inductively reactive**.  
If  $X_C = X_L$  - then **resonant**.
$$X_L$$

$$X_L = \frac{V_L}{I}$$
Modulus of Z
$$|Z| = \sqrt{R^2 + (X_L - X_C)^2}$$
e.g. for an  $RC$  for an  $RL$  series  
circuit,  $\tan \phi = \left[\frac{X_L - X_C}{R}\right]$ 
Phase difference between the  
current and the voltage
$$= \frac{-1}{R\omega C}$$

$$= \frac{\omega L}{R}$$

# 3.12 Resonance (Series)



The Q factor is an indication of the sharpness of the peak. High Q indicates sharp peak, low Q broad peak.

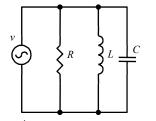
$$Q = \frac{\omega_R L}{R} = \frac{1}{R\omega_R C}$$
$$= \frac{1}{R} \sqrt{\frac{L}{C}}$$

The Q factor describes the **selectivity** of the circuit as well as the magnification of the voltage across the inductor and the capacitor. At resonance,  $V_C = QV$ ,  $V_L = QV$ 

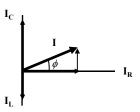
Note: this is resonance for an *LCR* series circuit. *L*, *C* and *R* must be present for resonance to occur. If R = 0, then the resonance peak is infinitely high.

### 3.13 Impedance (Parallel)

A parallel circuit is one in which the same voltage appears across all components. For parallel circuits, the voltage is the common point of reference (rather than the current as was the case in series circuits).



peak or rms



In complex number form:

1	1	. ( 1	1)
$\overline{Z}$	R	$-J\left(\frac{1}{X_C}\right)$	$\overline{X_L}$

Y = 1/Z is admittance (units: siemens).

At resonance,  $X_C = X_L$  and total current i is a minimum since Z is a maximum.

$$\omega_R^2 = \frac{1}{LC}$$

Parallel circuits exhibit high impedance at resonance.

In a parallel circuit, the instantaneous current across the resistor is always in phase with the instantaneous voltage; thus, for the capacitor and the inductor:

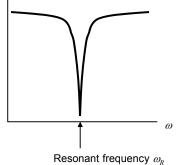
- $I_C$  always precedes  $I_R$  by  $\pi/2$  thus  $I_C$ is upwards on the vertical axis;
- $I_L$  always follows  $I_R$  by  $\pi/2$  thus  $I_L$  is downwards on the vertical axis.

Voltage is the common point of reference for a parallel circuit:

- same voltage across all components;
- vector sum of rms or peak currents must equal the rms or peak current;
- · algebraic sum of instantaneous currents equals the total instantaneous current.

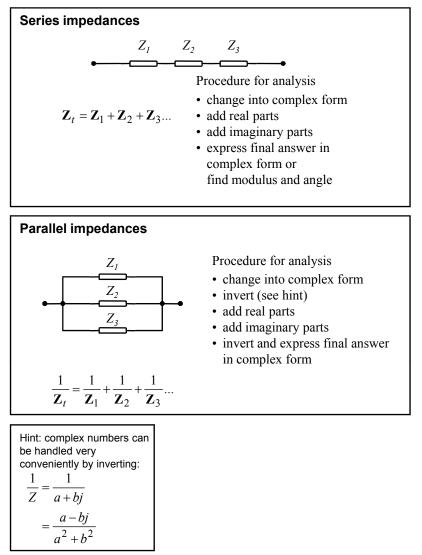
Note: this formula is consistent with addition of parallel impedances Z. The "i" has been moved to the numerator by multiplying through by *i/i* and remembering that  $j^2 = -1$  (hence positions of  $X_L$  and  $X_C$  reversed).

i



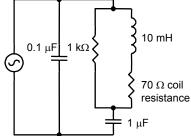
# 3.14 Impedances (Series and Parallel)

Impedances must always be added as vectors.



# 3.15 Impedances (Example)

Determine the **total impedance** of this circuit at a frequency f = 3 kHz ( $\omega = 18850$  rad s<sup>-1</sup>)



1. Express each component in complex form.

0.1 
$$\mu$$
F Z = 0 +  $j(-18850(0.1 \times 10^{-6}))^{-1}$   
= 0 + -530  $j$   
1  $\mu$ F Z = 0 +  $j(-18850(1 \times 10^{-6}))^{-1}$   
= 0 + -53  $j$   
10 mH Z = 70 +  $j(18850)(10 \times 10^{-3})$   
= 70 + 188.5  $j$ 

- $1 \text{ k}\Omega \qquad Z = 1000 + j(0)$
- 2. Combine inductor and resistor

$$\frac{1}{Z} = \frac{1}{1000} + \frac{1}{70 + 188.5j}$$

$$= \frac{1}{1000} + \frac{70 - 188.5j}{(70 + 188.5j)(70 - 188.5j)}$$

$$= \frac{1}{1000} + \frac{70 - 188.5j}{4900 + 35532}$$

$$= 2.73 \times 10^{-3} - 4.7 \times 10^{-3} j$$

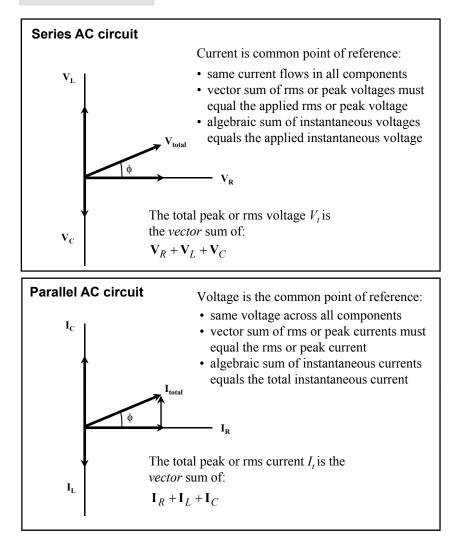
$$Z = \frac{2.73 \times 10^{-3} + 4.7 \times 10^{-3} j}{(2.73 \times 10^{-3})^2 + (4.7 \times 10^{-3})^2}$$

$$= 92.4 + 159 j$$

- 3. Combine with capacitor in series Z = 92.4 + (159 - 53)j= 92.4 + 106 j
- 4. Combine with capacitor in parallel

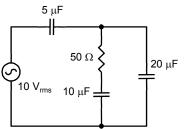
$$\frac{1}{Z} = \frac{1}{-530j} + \frac{1}{92.4 + 106j}$$
$$= \frac{530j}{280900} + \frac{92.4 - 106j}{19773}$$
$$= 4.67 \times 10^{-3} - 3.46 \times 10^{-3} j$$
$$Z = \frac{4.67 \times 10^{-3} + 3.46 \times 10^{-3} j}{3.38 \times 10^{-5}}$$
$$= 138 + 102.4 j \Omega$$
$$Z = 171.8 \Omega, 36.6^{\circ}$$

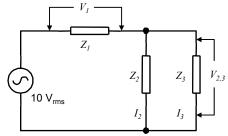
# 3.16 AC Circuits



# 3.17 AC Circuits (Example)

Calculate the **impedance** of the network shown at  $\omega = 1000$  rad s<sup>-1</sup> and also the current in the 20 µF capacitor.





1. By methods of the previous 2. Then apply Kirchhoff's laws: example, determine total impedance:

$$Z_{1} = 0 - 200 j$$
  

$$Z_{2} = 50 - 100 j$$
  

$$Z_{3} = 0 - 50 j$$
  

$$Z_{2} \parallel Z_{3} = 5 - 35 j$$
  

$$Z_{T} = 5 - 235 j$$
  

$$V = IZ$$
  

$$I = \frac{10}{5 - 235 j}$$
  

$$= 9 \times 10^{-4} + 0.0425 j$$

Note: all quantities are vectors.

$$V_{1} = (9 \times 10^{-4} + 0.0425 j)(0 - 200 j)$$
  
= 8.5 - 0.181 j  
$$V_{2,3} = (9 \times 10^{-4} + 0.0425 j)(5 - 35 j)$$
  
= 1.488 + 0.181 j  
$$|V_{3}| = 1.5$$
$$V_{1} + V_{2,3} = 10 + 0 j$$
$$V_{3} = I_{3}Z_{3}$$
$$I_{3} = \frac{1.488 + 0.181 j}{0 - 50 j}$$
  
= -3.62 \times 10^{-3} + 0.02976 j  
$$|I_{3}| = 0.03A$$
  
or  
$$1.5 = I_{rms} |Z_{3}|$$
$$I_{rms} = 0.03 A$$

Note: can do multiplication with magnitudes but not additions.

;)

# 3.18 Filters: Complex Form

low-pass filter

$$V_{in} = IZ$$
  
=  $I(R - X_C j)$   
=  $I\left(R - \frac{1}{\omega C}j\right)$   
 $V_{out} = I\left(-X_C j\right)$   
=  $I\left(-\frac{1}{\omega C}j\right)$   
 $\frac{V_{out}}{V_{in}} = \frac{\frac{-1}{\omega C}j}{R - \frac{1}{\omega C}j}$   
=  $\frac{1 - R\omega Cj}{1 + R^2 \omega^2 C^2}$   
=  $\frac{1}{1 + R\omega Cj}$   
 $\left|\frac{V_{out}}{V_{in}}\right| = \frac{1}{\sqrt{1^2 + R^2 \omega^2 C^2}}$ 

### high-pass filter

Peak, peak-to-peak  
or rms quantities  
only  
$$V_{in} = I(R + -X_C j)$$
$$V_{out} = IR$$
$$\frac{V_{out}}{V_{in}} = \frac{R}{R - X_C j}$$
$$\frac{R}{R - \frac{1}{\omega C} j} = \frac{R}{\sqrt{R^2 + \frac{1}{\omega^2 C^2}}}$$
$$\left|\frac{V_{out}}{V_{in}}\right| = \frac{R\omega C}{\sqrt{R^2 \omega^2 C^2 + 1}}$$
Let  $R\omega C = 1$ 
$$\frac{V_{out}}{V_{in}} = \frac{1}{\sqrt{2}}$$
 which is the  
3 dB point

Let  $R\omega C = 1$ 

$$\frac{V_{out}}{V_{in}} = \frac{1}{\sqrt{2}}$$
 which is the  
3 dB point

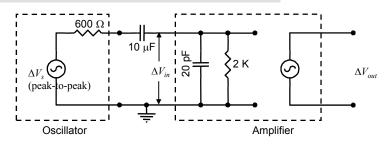
For a fixed *R* and *C*, the frequency at the 3 dB point is called the **cut-off frequency**  $f_0$  at

which point:

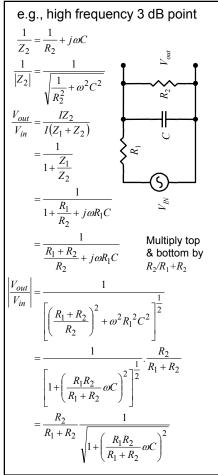
 $V_{out} = \frac{V_{in}}{\sqrt{2}}$ 

Peak, peak-to-peak or rms quantities only (not instantaneous)

# 3.19 Signal Generator and Oscilloscope

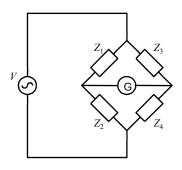


The input and output impedances of signal generating and measuring devices have a marked effect on the attenuation of voltage signals that may be produced or measured. For example, an oscillator with an output impedance of 600  $\Omega$  may be connected to the input of an oscilloscope with an input resistance of 2 k $\Omega$  and a series capacitance of 10 µF (on the AC setting of the oscilloscope). The capacitance of the signal leads shunts the input of the oscilloscope and may be around 20 pF. At low frequencies, the shunt capacitance may be ignored. At high frequencies, the series capacitance may be ignored. In the midfrequency range, we may assume that both capacitances have a negligible effect on the signal. By determining the 3 dB points for the equivalent high and low frequency circuits, two frequencies  $f_{lo}$  and  $f_{hi}$  can be found at which the input voltage  $\Delta V_{in}$  drops by 3 dB relative to its mid-frequency value (assuming that  $\Delta V_s$  is constant at all frequencies).



# 3.20 AC Bridge

For the galvanometer to read zero, the voltage across its terminals must be zero. Thus, the voltage across  $Z_1$  and  $Z_3$  must be equal in magnitude and phase.

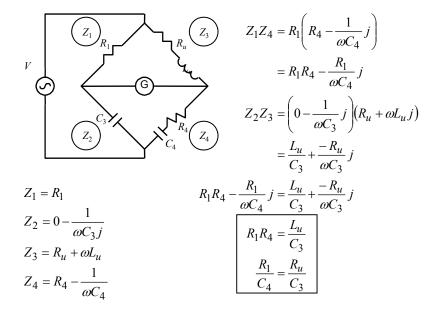


$$V_1 = V_3$$
$$I_1 Z_1 = I_3 Z_3$$

At balance condition, no current flows through the galvanometer.

Thus 
$$V = I_1(Z_1 + Z_2)$$
  
 $= I_3(Z_3 + Z_4)$   
 $I_1 = \frac{V}{Z_1 + Z_2}; I_3 = \frac{V}{Z_3 + Z_4}$   
 $I_1Z_1 = \frac{Z_1V}{Z_1 + Z_2}; I_3Z_3 = \frac{Z_3V}{Z_3 + Z_4}$   
 $\frac{Z_3V}{Z_3 + Z_4} = \frac{Z_1V}{Z_1 + Z_2}$   
 $\boxed{Z_1Z_4 = Z_2Z_3}$   
General bridge  
equation at  
balance condition

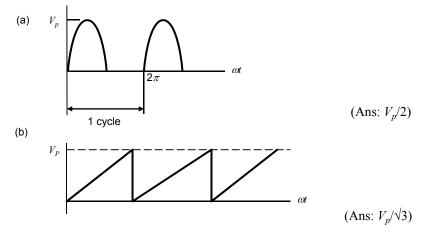
Example



#### 3. AC Circuits

# 3.21 Review Questions

1. Determine the rms voltages of the waveforms shown below from first principles. In both cases, assume that the circuits are resistive (voltage and current are in phase).



2. The average (i.e., rms) power of a soldering iron is 55 W and the iron has a resistance of 250  $\Omega$ . Calculate the (a) rms current, (b) rms voltage and (c) peak voltage. If the power supply in is 240 V rms, determine the peak voltage  $V_{pr}$ .

(Ans: 469 mA, 117.25 V, 166 V, 340 V)

3. An electric toaster draws 3 A rms from a 240 V, 50 Hz source. Calculate the average power and the peak value of the instantaneous power to the toaster.

(Ans: 720 W, 1440 W)

4. What is the capacitive reactance of a 47 pF capacitor when the frequency is (a) 5 MHz, (b) 1 kHz?

(Ans: 676.9 Ω, 3.39 MΩ)

5. What value of capacitor is needed to limit the rms current through it to 3 mA when it is connected across a 50 V, 500 Hz AC source?

(Ans: 19 nF)

- The inductance of an ignition coil in a motor vehicle is 0.005 H. The resistance of its windings is 1.5 Ω. Determine the impedance of the coil when the current in the circuit turns on and off 1000 times per second. (Ans: 1.59 Ω)
- 7. Determine the impedance of a 200 pF capacitor connected in series with a  $1.2 \text{ k}\Omega$  resistor when the frequency is 5 MHz.

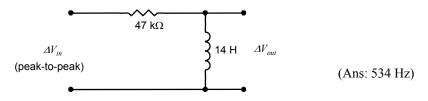
(Ans: 1210 Ω)

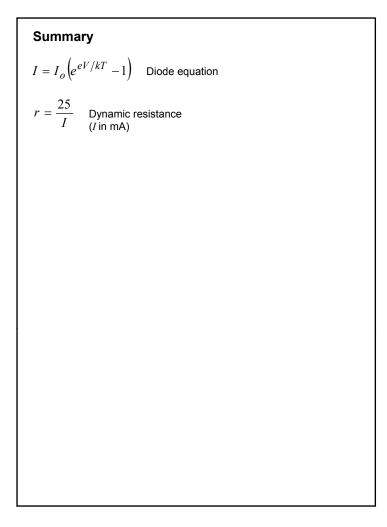
- 8. Find the magnitude and phase with respect to *V* of each of the following for the circuit shown below:
  - (a) current; (b) voltage across R; (c) voltage across L; (d) average power supplied by source.  $V_{rms} = 250 V$   $f = 100/\pi Hz$

9. Three impedances  $Z_1$ ,  $Z_2$  and  $Z_3$  are connected in series. Calculate the total impedance.

$$Z_1 = 240 \,\Omega, +10^\circ$$
  
 $Z_2 = 40 \,\Omega, +40^\circ$   
 $Z_3 = 1000 \,\Omega, -10^\circ$  (Ans: 1256  $\Omega, -4.85^\circ$ )

- 10. Determine the value of capacitor which must be connected in series with a 600  $\Omega$  resistor to limit its power dissipation to 5 W when connected to a 240 V, 50 Hz source. (Ans: 276 nF)
- 11. In the circuit shown, determine the frequency corresponding to the
  - 3 dB point.





# 4.1 Semiconductors

There are three classes of materials:

#### 1. Conductors

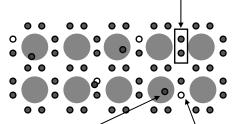
Valence electrons are weakly bound to the atomic lattice and are free to move about from atom to atom.

#### 2. Insulators

Valence electrons are tightly bound to the atomic lattice and are fixed in position.

#### 3. Semiconductors

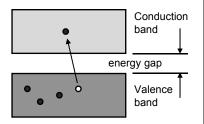
In **semiconductors**, thermal vibration of atoms in a crystal causes electrons to break away and become free. The solid then becomes weakly "conducting":



e.g., these two electrons shared equally between neighbouring atoms i.e., a covalent bond

Conductivity increases with increasing temperature.

Electrons which have broken away enter what is called the **conduction band** and have a higher energy than those left behind in the **valence band**.



Intrinsic semiconductor

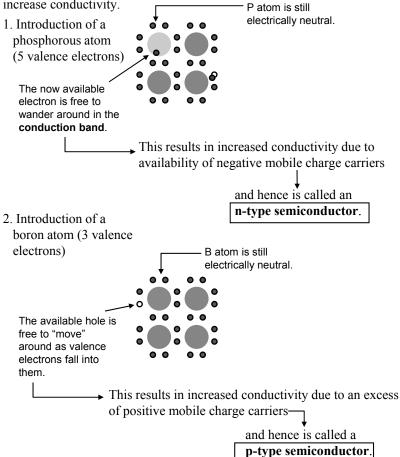
The place left vacant by such an electron is called a **hole**.

#### What is an energy band?

A popular model of the atom describes the structure of atoms in terms of a series of electron energy levels (1s, 2s, 2p, etc). In a solid (as distinct from a single atom), the effects of neighbouring atoms give rise to the condition that each electron energy level splits into a number of closely spaced sub-levels. In a solid, there are many neighbouring atoms to any one atom and the total effect is for the sub-levels to become continuous and thus the energy level is more correctly called an energy band. In a metal, the valence band overlaps with the conduction band. In an insulator, there is a considerable energy gap. In a semiconductor, some electrons escape from the valence band across a small energy gap into the conduction band.

# 4.2 P- and N-Type Semiconductors

The addition of certain impurities (doping) to the silicon lattice can increase conductivity.



In both types of semiconductor, the increased conductivity arises due to the deliberate increase in the number of *mobile* charge carriers - all still electrically neutral material.

- The **majority carriers** in an n-type material are electrons, the majority carriers in a p-type material are holes.
- Both types have thermally generated electrons and holes which are called **minority carriers**.

# 4.3 Response in an Electric Field

n-type (majority carriers: electrons)

1. Electrons, attracted by positive charge of battery, enter wire from conduction 2. Electrons from band. wire enter 3. A few (intrinsic) conduction ~0 holes drift towards band negative. o ക് or may fall Small current flows into a hole, but since Note: In these types of solid state diagrams, the electron current not many will be shown, not conventional current. Conventional current will holes be assumed for regular circuit diagrams. Here we are interested (minority in events on the atomic scale, hence our need to show the carriers) in movement of electrons (and also holes). n-type small effect. p-type (majority carriers: holes) Electrons jump from atom 1. Electrons, attracted by 2. Electrons from to atom, causing hole to battery positive enter wire

wire enter into appear to move to right. from valence band, holes that leaving a hole. arrive here and 3. A few (intrinsic) become **\_\_\_\_** conduction band electrons valence move towards positive. < CO electrons. 0  $\rightarrow$ < CO→ Small current flows

# 4.4 P-N Junction

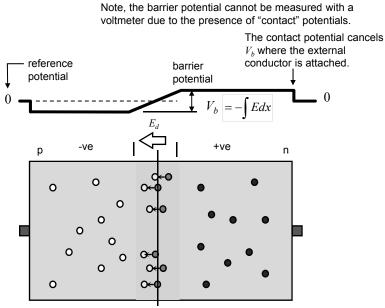
1. Near the junction, free electrons from the n side **diffuse** across the junction and fall into holes on the p side, becoming valence electrons.

Thermal energy causes free electrons to have "random motion." Excess of free electrons on the n side constitutes a "concentration gradient." These two conditions permit a net transfer of free electrons from the n side to the p side by "diffusion" ... and vice versa on the p side.

2. The resulting build-up of negative charge on the p side and positive charge on the n side establishes an increasing electric field  $E_d$  across the junction, leading to what is called the **barrier potential**  $V_b$ .

 $V_b$  = 0.7 V (Si) @ 25 °C, decreasing with increasing temperature.

**3.** Balance between diffusion process and electrostatic repulsion due to field is quickly established; no more net movement of charge carriers.



The area near the junction becomes free of majority carriers (and is therefore an insulator) and is called the **depletion region**. Any thermally generated minority carriers within the depletion region are swept across it by field  $E_d$ . Accumulation of charge is reduced somewhat and diffusion then reestablishes equilibrium and  $E_d$  resumes its former value.

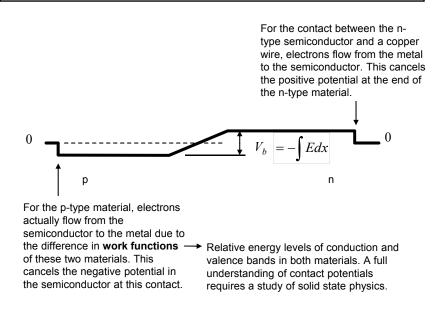
# 4.5 Contact Potential

When a metal is placed in contact with a semiconductor (or even another metal), the difference between the density of free electrons on either side of the contact, or junction, causes a **concentration gradient** which results in **diffusion** of electrons across the contact junction.

Whether or not electrons diffuse from the metal to the semiconductor or from the semiconductor to the metal depends upon whether the semiconductor is p- or n-type and the nature of the metal.

The "nature" of the metal and the contact is beyond the scope of our discussion. It is connected with the energy levels of the conduction electrons in each of the materials and how they compare with each other.

This movement of electrons across the contact gives rise to an electric **contact potential**. Because of contact potentials, you cannot measure the barrier potential of a p-n junction by connecting a voltmeter across it.



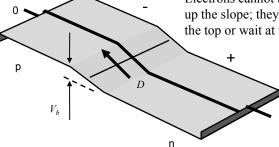
# 4.6 Potential Diagram

In this type of diagram, electrons are like marbles or round beads. Electrons are given a boost upwards by emfs or voltage sources. Electrons may only move if there is a downhill path or slope. If the slope is frictionless (i.e., an electric field), then electrons gain "kinetic" energy. If the slope has friction (i.e., resistor), then energy is converted to heat.

#### p-n junction

Diffusion acts like a "force" *D* to push electrons from the n side to the p side. As electrons accumulate on the p side, the slope becomes steeper and steeper until it is too difficult for the diffusion force (which remains constant) to transfer any more electrons from p to n.

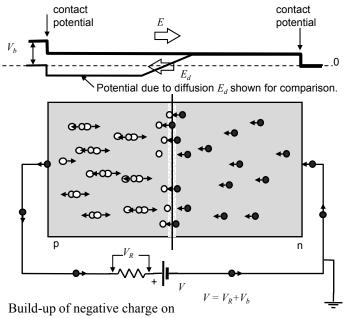
The slope (**barrier potential**) arises due to the accumulation of charge on either side of the junction. Diffusion acts to transfer electrons up the slope. If the slope is too steep, then no electrons are transferred. Electrons cannot be transferred part-way up the slope; they are either transferred to the top or wait at the bottom.



If an **electron-hole pair** should appear on the slope (via thermal agitation) then the electron rolls downhill to the n side. This electron cancels some of the +ve charge on the n side, thus reducing the steepness of the slope slightly. Diffusion can then transfer one more electron to the p side whereupon the steepness of the slope resumes its previous value and diffusion is not strong enough to transfer any further electrons.

# 4.7 Forward Bias

1. Battery voltage V causes an external field E across the depletion layer to cancel the internal field  $E_{d}$ . Majority carriers in both materials can cross the junction because the applied emf overcomes the barrier potential. The depletion region disappears.

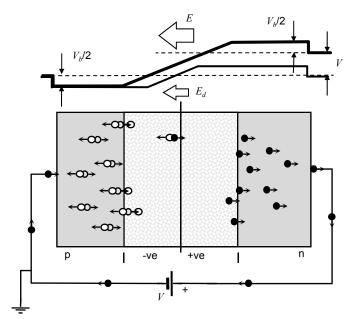


- 2. Build-up of negative charge on the p side is prevented as electrons drain away to the battery positive terminal.
  - 3. Continuous flow of electrons on the n side and holes on the p side constitute electric current, the magnitude of which is given by  $I = (V-V_b)/R$ .

Note, from now on in these diagrams, we shall refer voltages (i.e., potentials) to the (-) or "earth" side of the applied emf.

# 4.8 Reverse Bias

1. Free electrons on the n side are attracted to the battery positive, causing them to move away from the junction, causing additional build-up of positive charge near the junction. The depletion region widens.



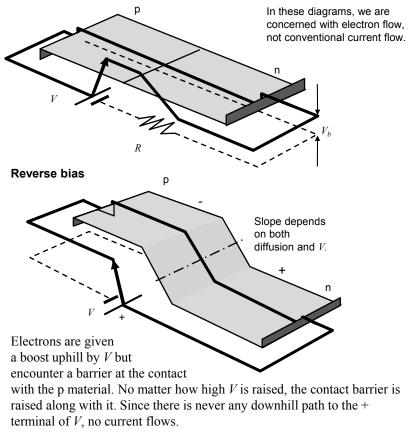
- 2. Holes on the p side are attracted towards the battery negative, causing additional negative charge near the junction.
  - **3.** After a very short period, equilibrium is established where the attraction of mobile carriers to the externally applied voltage source is balanced by a build-up of charge on either side of the junction. Movement of majority carriers ceases; no current flows.

Thermally generated minority carriers in the depletion layer may be swept cross junction by the field. This is called **leakage current**.

## 4.9 Potential Diagrams

#### **Forward bias**

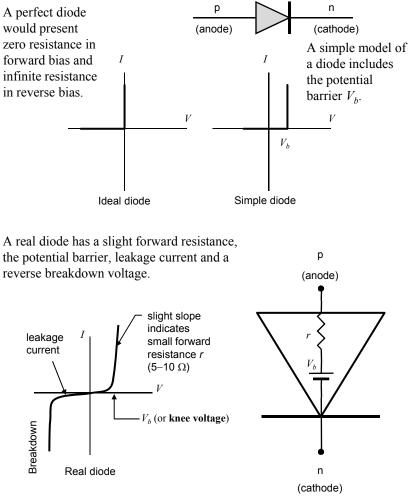
After being given an initial boost uphill by the voltage source V, electrons (now with potential energy) have a downhill run all the way around the circuit. Potential energy is lost after going through the resistor (heat), and then again through the contact potentials (overcoming diffusion "force").



If an electron appears on the slope (i.e., thermally generated within the depletion region), then the electron immediately rolls downhill to the n side, acquiring sufficient "kinetic energy" to overcome the contact barrier and thus be transported around to the emf and given a boost uphill. This is reverse bias leakage current.

# 4.10 Diode

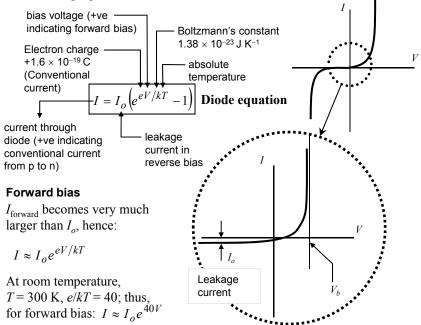
A p-n junction will conduct current in forward bias and act as an open circuit in reverse bias. Such an action is called **rectification** and the device as a whole is called a **diode**.



Equivalent circuit

# 4.11 Diode Equation

**Maxwell–Boltzmann statistics** applied to the diffusion of charge carriers can predict current density across the junction in forward and reverse bias. The resulting equation is:



For a linear resistor, V/I = R, but here, the relationship between V and I is not a constant, but is exponential. Hence, the slope of the line at any point gives the "resistance" of the forward bias junction.

$$\frac{dI}{dV} = 40 I_o e^{40V}$$
$$= 40 I$$

Hence,

$$\frac{dV}{dI} = \frac{1}{40I}$$
$$= r$$
$$r = \frac{25}{I}$$

**Dynamic resistance** of forward biased junction

when I is expressed in mA

#### **Reverse bias**

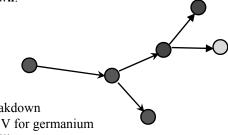
*V* is negative and hence the exponential term is very small; thus:

 $I \approx -I_o$ 

Leakage current is typically a few  $\mu$ A. Note, the diode equation says nothing about the possibility of breakdown.

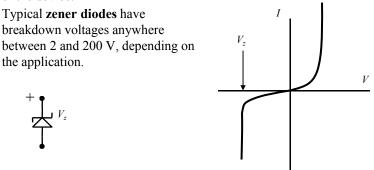
#### 4.12 Reverse Bias Breakdown

As the magnitude of the reverse bias voltage is increased, the current remains at  $I_0$  but eventually the reverse bias field is so strong that thermally generated electrons (or holes) acquire enough kinetic energy to ionise atoms within the crystal structure. These in turn ionise other atoms, leading to a very swift multiplication effect and a large current. This is called **avalanche breakdown**.



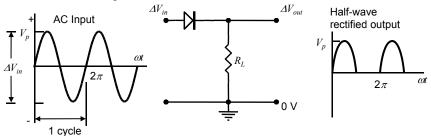
The reverse bias breakdown voltage is about 500 V for germanium and about 1 kV for silicon.

If the impurity doping density is high enough, then the depletion region is narrow enough (even in reverse bias) to allow the electric field across the region to be very high. The high accelerating field and narrow depletion region allow electrons to tunnel through. This is called **zener breakdown**. Zener diodes are designed to break down in reverse bias. They can withstand a relatively large reverse current without damage. The reverse bias voltage leading to zener breakdown is adjustable during manufacture of the device.

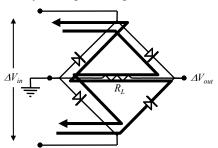


#### 4.13 Rectification

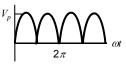
One very common application of diodes is in **rectification** of an AC signal, that is, the conversion of AC into DC. In many cases, mains AC voltage has to be converted into a low DC voltage. The conversion from high voltage to low voltage is usually accomplished by a **transformer**, the output of which is a low voltage AC signal. This then has to be converted to a stable, DC output.



Full-wave rectification involves a clever arrangement of diodes to produce a DC signal but with a large ripple. This may be smoothed to give a fairly steady DC signal using various methods.

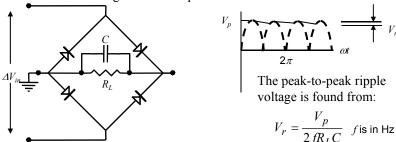


Full-wave rectified output



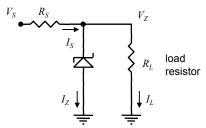
Note:  $\Delta V$  means peak-to-peak voltage where  $V_p$  means the amplitude of the sine wave signal.

A steady "DC" output can be obtained by filtering the full-wave rectified signal with a capacitor.



# 4.14 Regulation

**Zener diodes** find special application as voltage regulators. They have a very sharp reverse bias breakdown characteristic. In a **voltage regulator**, the supply voltage can change significantly but the zener diode voltage  $V_Z$  does not change.



 $V_L = V_Z$  and  $I_S$  is thus fixed and independent of  $R_L$ . If  $R_L$  increases, the zener passes more current to keep  $V_L = V_Z$ . When  $R_L$  is infinite,  $I_Z = I_S$ . Care must be taken to ensure that the maximum current through the zener diode does not cause overheating. Maximum current in the zener occurs at open-circuit conditions (no  $R_L$  connected).

Example:

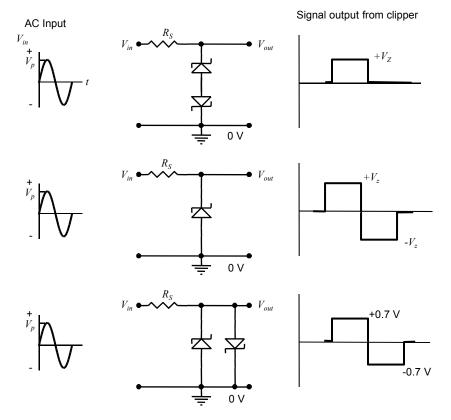
What resistor  $R_S$  is required to limit the power dissipation in the 4.8 V zener diode shown in the diagram above to 25 mW if  $V_S$  is 10 V?

Solution:

$$25 \text{ mW} = 4.8I$$
$$I = 5.2 \text{ mA}$$
$$10 - 4.8 = 5.2 \times 10^{-3} R_s$$
$$R_s = 1 \text{ k}\Omega$$

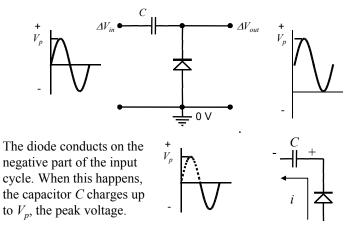
# 4.15 Clipper

A diode clipping circuit is useful for signal shaping. For example, in a Geiger counter, a click is heard when an ionizing particle strikes the detector. Now, the detector itself does not produce voltage pulses of equal magnitude, but instead, an irregularly shaped signal. For the measurement of radiation, we simply require the rate at which pulses are produced and we are not concerned with the amplitude or shape of the pulse. A diode clipper can be used to produce a squared-up waveform which can then be fed into an audio amplifier or digital counter. The clipper ensures that the pulses fed to the counting circuit are uniform and that the counting circuit needs to only display the count rate.



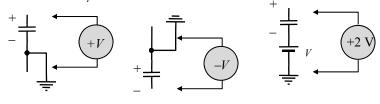
## 4.16 Clamp

The diode clamp is used for changing the reference voltage of an AC input signal.

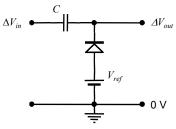


The potential of the right hand side of the capacitor with respect to the left hand side is  $+V_p$ . That is, when  $\Delta V_{in}$  is at  $-V_p$ , the potential of the right hand side of the capacitor is 0 V. When the input  $V_{in}$  reaches 0 V,  $\Delta V_{out} = +V_p$  since the capacitor remains charged – the diode does not allow the capacitor to discharge.

On the positive half cycle, the left hand side of the capacitor is brought to a potential of  $+V_p$ . The right hand side of the capacitor must now be at a potential of  $+2V_p$  with respect to 0 V.

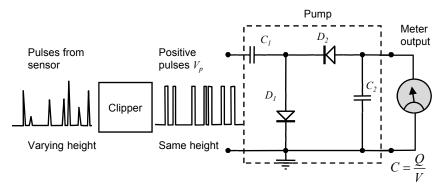


Thus, the output swings between 0 V and  $+2V_p$ . If a voltage source  $V_{ref}$  is inserted "beneath" the diode, then the reference voltage is held at  $V_{ref}$ and the output swings between  $V_{ref}$  and  $V_{ref} + 2V_p$ .



# 4.17 Pump

A diode pump is a circuit which produces a steady DC signal whose magnitude is proportional to the rate of arrival of voltage pulses at the input. We have seen how a clipper may be used to square up irregularly shaped pulses, now we shall see how to convert the train of pulses into a "rate" (i.e., an output voltage which is proportional to the number of pulses per second). The diode pump is how a tachometer works. Pulses from the ignition system are received and converted into a steady DC voltage whose magnitude thus depends on engine rpm. The DC voltage then drives a moving coil meter which is calibrated to read rpm.

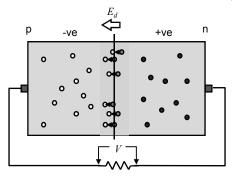


A positive pulse  $V_p$  charges capacitor  $C_1$  via  $D_1$ . The value of  $C_1$  is such that it can charge fully during the positive value of the input pulse (small time constant). Thus, a single pulse fully charges  $C_1$ . The right hand side of  $C_1$  is negative w.r.t. the left hand side. When the left hand side returns to 0 V, the right hand side of  $C_1$  is negative w.r.t. the top side of  $C_2$ . The negative charge is now distributed between  $C_1$  and  $C_2$  since  $D_2$  is now conducting. Most of the charge on  $C_1$  is transferred to  $C_2$  (capacitors in parallel – voltage across each is the same, charge on each depends on C and here,  $C_2 >> C_1$ ).

Now, if another pulse  $V_p$  arrives at the input,  $D_1$  turns on as  $C_1$  charges up and  $D_2$  turns off. This leaves most of the original -ve charge on the "top" plate of  $C_2$ .  $C_1$  accepts more charge from the input pulse and this is again transferred to  $C_2$  on the next fall to 0 V at the input. The current through the meter depends upon the amount of accumulated charge on  $C_2$ . The faster the rate of input pulse, the greater the accumulation of charge on  $C_2$ . In order to indicate pulse rate, it is important that the peak voltage of the input pulses are all the same. The shape or width of them then does not matter.

### 4.18 Photodiode

A photodiode employs the **photovoltaic** effect to produce an electric current which is a measure of the intensity of incident radiation.



Diffusion of electrons and holes across the junction lead to the formation of a **barrier potential** leading to field  $E_d$  and a **depletion region**. When a photon creates an **electron-hole pair** in the depletion region, the resulting free electron is swept across the junction towards the n side (opposite direction of  $E_d$ ). Current will flow in the external circuit as long as photons of sufficient energy strike the material in the depletion region.

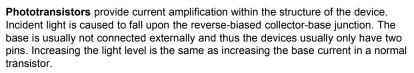
dark

illuminated

Even though the photodiode generates a signal in the absence of any external power supply, it is usually operated with a small reverse bias voltage. The incident photons thus cause an increase in the **reverse bias leakage current**  $I_{o}$ .

The reverse bias leakage current is directly proportional to the luminous intensity. Responsivity is on the order of  $0.5 \text{ A W}^{-1}$ .

Avalanche photodiodes operate in reverse bias at a voltage near to the breakdown voltage. Thus, a large number of electron-hole pairs are produced for one incident photon in the depletion region (internal ionisation).

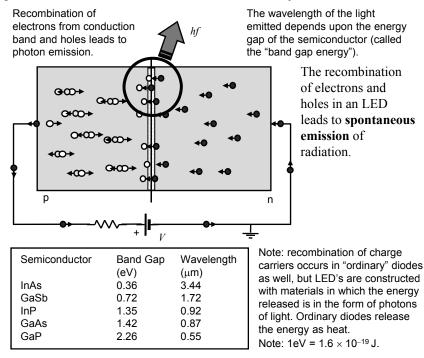


**Schottky photodiodes** use electrons freed by incident light at a metal-semiconductor junction. A thin film is evaporated onto a semiconductor substrate. The action is similar to a normal photodiode but the metal film used may be constructed so as to respond to short wavelength blue or ultraviolet light only since only relatively high energy photons can penetrate the metal film and affect the junction.

A **PIN photodiode** is a p-n junction with a narrow region of intrinsic semiconductor sandwiched between the p- and n-type material. This insertion widens the depletion layer, thus reducing the junction capacitance and the time constant of the device – important for digital signal transmission via optical cable.

# 4.19 LED

The light-emitting diode (LED) operates in forward bias and generates a photon when electrons and holes recombine near the junction.



In a **laser diode**, photons arising from spontaneous emission are reflected back and forth between the polished faces of the device. These photons are absorbed within the crystal, releasing an electron into the conduction band. However, simultaneously with this absorption, electrons in the conduction band also fall back into the valence band and a photon of the same frequency is emitted. This is **stimulated emission**.

Absorption and stimulated emission occur simultaneously and with equal probability. However, in a laser diode, the geometry of the mirrored faces and the doping of the crystal ensure that when the current through the device is sufficient, there are more electrons in the conduction band than in the valence band (**population inversion**) and the stimulated emission of photons has a greater chance of occurring than absorption. The emitted photons all have the same phase and frequency and are emitted as laser light out through one of the partially mirrored sides of the device.

#### 4.20 Review Questions

- 1. Briefly describe the essential features of an electrical insulator, semiconductor and a conductor.
- 2. Explain the origin of leakage current in a reverse-biased p-n junction.
- 3. It can be shown that the barrier potential of a p-n junction can be calculated from:

$$V_B = \frac{kT}{e} \ln \left( \frac{N_A N_D}{n_i^2} \right)$$

Assuming that for germanium the  $N_A$  is  $5 \times 10^{16}$  cm<sup>-3</sup> and  $N_D$  is  $1 \times 10^{18}$  cm<sup>-3</sup>, calculate the value of the barrier potential  $V_B$  at T = 300 K. Assume  $n_i = 1 \times 10^{15}$  cm<sup>-3</sup>.

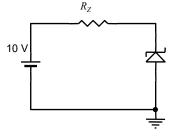
(Ans: 0.28 V)

4. Calculate the apparent resistance of a forward-biased p-n junction at room temperature (300 K) when the current through the junction is 5 mA.

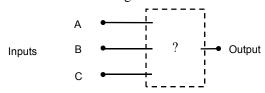
(Ans:  $5 \Omega$ )

5. In the circuit below, calculate the value of  $R_Z$  required so that the power dissipated by the 4.8 V zener diode does not exceed 25 mW.

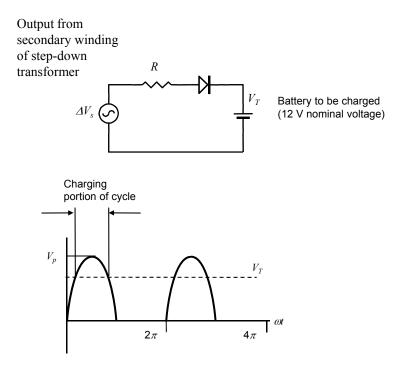
(Ans:  $1 k\Omega$ )



6. In a logic gate which implements the logic "OR" function, a steady 5 V DC signal is produced at the output when either one of 3 inputs is at 5 V. Implement this circuit using diodes.



7. A motor vehicle battery charger consists of a step-down transformer, a resistor and a diode. The transformer supplies a peak-to-peak voltage  $\Delta V_s$  to the diode and resistor as shown.



The battery voltage  $V_T$  rises as charging progresses. The peak charging voltage is 14 V. At low charge conditions, ( $V_T$  is low), we require maximum charging current (6 amps rms).

- (a) Determine a value for the resistance *R*. Hint: when the battery is completely flat, the charging current is a maximum; further, the rms current for a half sine wave is  $I_p/2$ .
- (b) Determine the maximum reverse voltage applied to the diode.
- (c) Calculate the peak value of the charging current when the battery voltage reaches 12 V.
- (d) Determine the rms current when the battery terminal voltage reaches 12 V (hint: this is NOT  $I_p/2$ ).

(Ans: 1.17 Ω, 26 V, 1.7 A, 0.67 A)

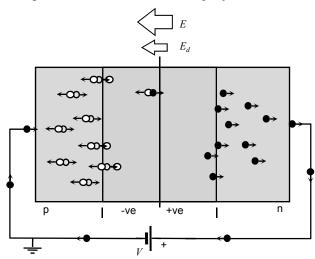
# 5. Bipolar Junction Transistor

Summary
$\frac{I_c}{I_b} = h_{fe}$ Current gain
$I_c = -\frac{1}{R_c}V_{ce} + \frac{V_{cc}}{R_c}  \text{Load line (simple bias)}$
$V_b = I_b R_b + V_{be}$ Simple bias
$V_{cc} = I_c R_c + V_{ce}$
$I_c = -\frac{1}{R_c + R_e} V_{ce} + \frac{V_{cc}}{R_c + R_e}  \text{Load line (emitter bias)}$
$\frac{\Delta V_{out}}{\Delta V_{in}} = A_v  \text{Voltage gain}$

# 5.1 Bipolar Junction Transistor - Construction

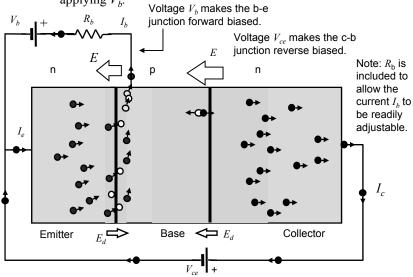
How does it work?

Step 1. Start with a reverse-biased p-n junction.



Note: the field  $E + E_d$ only exists across the depletion region. Thus. once equilibrium is established, the electrical potential between the p- and the n-type material is equal and opposite to V. Only mobile charge carriers originating within the depletion region are accelerated by the field, causing reverse bias leakage current to flow.

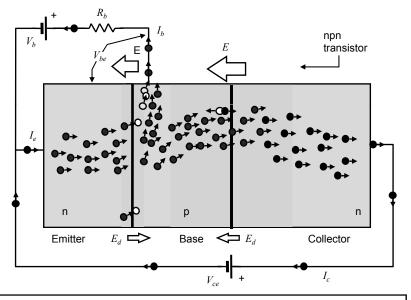
**Step 2.** Create an additional p-n junction on the left by adding some ntype material and make the new junction forward-biased by applying  $V_{k}$ .



#### 5. Bipolar Junction Transistor

#### Here's what happens:

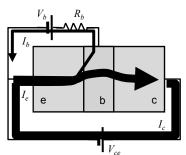
- Base-emitter junction is a forward-biased p-n junction so when the voltage  $V_{be} > 0.7$  V (for silicon) then the junction becomes conducting (just like a diode).
- Electrons coming from the heavily doped emitter cross the junction but before they have a chance to combine with holes in the p-type base and travel to the  $V_b$  positive terminal, they get swept up by the strong field which exists around the collector base junction, which is reverse-biased.
  - Because the base is made <u>lightly doped</u> (so that recombination in the base is unlikely to occur) and is made <u>very thin</u> (so that electrons coming across the forward-biased b-e junction do not have far to go before they "overshoot" and fall into the field across the c-b junction).
- Hence, only a few electrons go towards +ve  $V_b$  and most are attracted across the collector base junction and cause a large current in the
  - collector. If the electrons coming across into the base were not attracted across the c-b junction (e.g., if  $V_{ce} = 0$ ) then they would simply go towards  $V_{bb}$  and there would be a large base current. But, because of the large field surrounding the reverse-biased c-b junction, these electrons are "siphoned off," thus causing  $I_c >> I_b$ , and that any increase or decrease in  $I_b$  would be reflected by an increase or decrease in  $I_c$ .



The result is that a very small current in the base circuit causes a very large current to flow in the collector circuit.

# 5.2 Bipolar Junction Transistor - Operation

How is the **collector current** controlled? Electrons only cross the b-e junction because it is forward biased by  $V_b$ . Hence, all electrons which cross this junction initially want to go to  $+V_b$ . If the base current were to be increased, (by increasing the magnitude of  $V_b$ ), then there would be more electrons (per second) wanting to go towards  $+V_b$ 

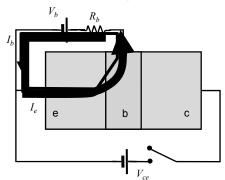


and hence more electrons (per second) being siphoned off towards the collector by the reverse bias field at the c-b junction. The magnitude of the base current controls the magnitude of the collector current. The ratio of the two currents is called the **current gain** and given the symbol  $h_{fe}$ .



Electrons which do go to the collector find their way around to the emitter again joining those which went through the base. Thus, in the emitter, there are two currents,  $I_b$  and  $I_c$ . Thus:  $I_e = I_c + I_b$ .

If  $V_{ce}$  were to be turned off, then one might expect that all these electrons would go towards  $+V_b$  and the base current would increase quite dramatically.



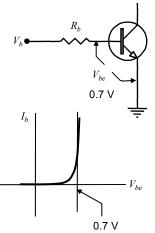
In practice, something else actually happens. This is where the resistance  $R_b$  comes into operation.  $R_b$  can be deliberately put there by us as an external resistor, or if no external resistor, may represent the internal resistance of the voltage source  $V_b$ . Now, we know that the voltage  $V_b$ supplies a voltage drop across the b-e junction of about 0.7 V and the remainder appears across  $R_b$ .

Now, if  $V_b$  is held constant, but  $I_b$  were to increase due to the removal of the reverse bias field at the c-b junction, then there would be an increase in the voltage drop across  $R_b$ . But, since  $V_b$  is a constant, this must mean that there is a reduction in the voltage across the forward bias b-e junction. Now, if  $V_{be}$  is decreased, then due to the exponential nature of the *IV* characteristics of the p-n junction, there is a substantial reduction in  $I_b$ . But this reduction in  $I_b$  also reduces the voltage drop across  $R_b$ , hence tending to increase  $V_{be}$  – negative feedback. The net result is a new equilibrium with  $V_{be}$  reduced slightly and a less-than-expected  $I_b$  is observed.

The **base current** is controlled by a resistor  $R_b$  which is inserted between the voltage supply  $V_b$  and the base so that  $I_b$  may be adjusted by adjusting  $V_b$ . Thus, consider the circuit below, which shows the "base-emitter" half of the transistor:

In this circuit,  $V_{be}$  remains at somewhere near 0.7 V and increasing the voltage  $V_b$ simply increases the voltage drop across  $R_b$  due to the increased current  $I_b$ . (A large change in  $I_b$  does not change  $V_{be}$  all that much compared to the change in voltage across  $R_b$ .) Thus, with the resistor  $R_b$  in place, we may adjust  $I_b$  by adjusting  $V_b$ .

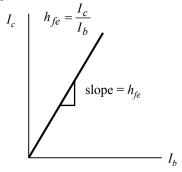
$$V_b = I_b R_b + V_{be}$$
  
Increasing  $V_b$  means an  
increase in  $I_b$  since  $V_{be}$  and  
are "constant."



A bipolar junction transistor (BJT) is a current controlled device. Resistors may be used to convert current control into voltage control, but the essential feature is that for a given base current  $I_b$ , there is a fixed value of collector current  $I_c$ .

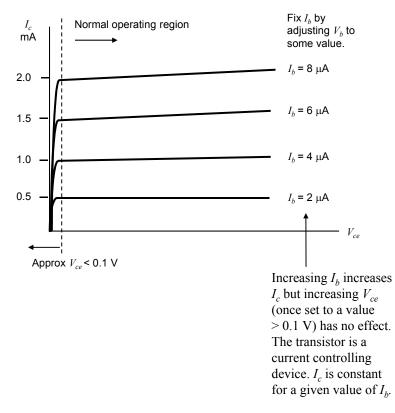
R

A plot of  $I_c$  vs  $I_b$  shows that the **current gain**  $h_{fe}$  is fairly constant. In practice,  $h_{fe}$  depends on manufacturing variables and is very different between actual transistor components. Values between 100 and 300 are typical.



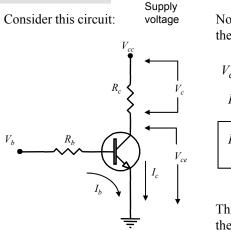
# 5.3 Transistor Characteristic

Transistor action can be summarised in one figure, which is called the **transistor characteristic**.



Note: in practice there is some slight increase in  $I_c$  when  $V_{ce}$  is increased. As  $V_{ce}$  is increased, the width of the depletion region associated with the reverse-biased c-b junction increases and the reverse bias field also increases. When this happens, for a given base current  $I_b$ , a greater proportion of the electrons are "collected" by the collector and  $I_b$  reduces. However, a reduction in  $I_b$  leads to a reduction in the voltage across the base resistor and an increase in voltage across the b-e forward bias junction. This leads to an increase in  $I_b$  due to the feedback mechanism discussed previously. The overall effect is for a fairly constant  $I_b$  and a slightly increasing  $I_c$  with increasing  $V_{ce}$ .

### 5.4 Load Line



Now consider the voltage drops down the right hand side of the circuit.

$$V_{cc} = I_c R_c + V_{ce}$$

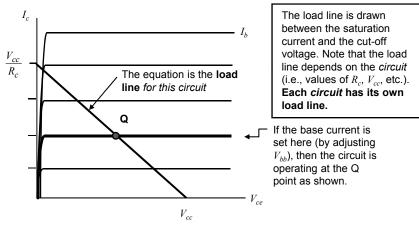
$$I_c = \frac{V_{cc}}{R_c} - \frac{V_{ce}}{R_c}$$

$$I_c = -\frac{1}{R_c} V_{ce} + \frac{V_{cc}}{R_c}$$

slope *y* axis intercept This linear equation describes the **load line** for this circuit.

 $V_{ce}$  here is determined by the *circuit*. That is,  $I_b$  controls  $I_c$ , which results in a voltage drop across  $R_c$ . Hence, if  $I_b$  goes up,  $I_c$  goes up and voltage  $V_c$  goes up and  $V_{ce}$  goes down.

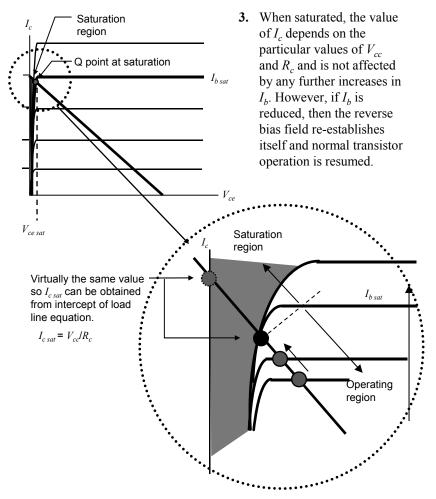
The load line may be superimposed on the transistor characteristic.



The load line shows the allowable values of  $I_c$  and  $V_{ce}$  for a particular circuit. The Q point is the value of  $I_c$  and  $V_{ce}$  which might be measured for a circuit at some particular value of  $V_b$ . The corresponding base current may be obtained from the transistor characteristic curve, which is coincident with the Q point.

### 5.5 Saturation

1. At low values of  $V_{ce}$  (i.e., high values of  $I_b$ ) the circuit follows the load line *until the transistor saturates*.

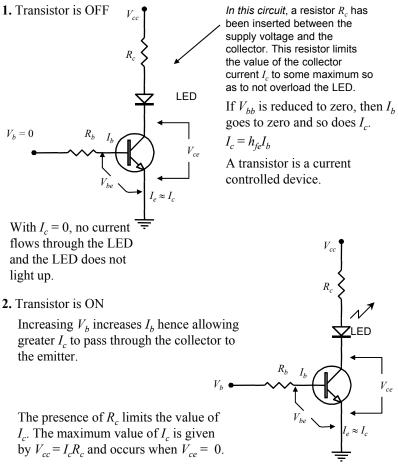


2. In the operating region, increasing  $I_b$  results in an increase in  $I_c$  and operating point moves up the load line. Eventually, a point is reached  $I_{b \, sat}$  where an increase in  $I_b$  results in no further increase in  $I_c$ . i.e., characteristic curves for  $I_b > I_{b \, sat}$  all intersect the load line at the same place  $I_{c \, sar}$ .

#### 5. Bipolar Junction Transistor

#### 5.6 Transistor Switch

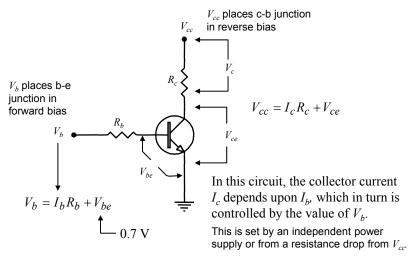
When the base current  $I_b$  is zero, no collector current  $I_c$  will flow (no matter how high  $V_{ce}$  might be) since there are no charge carriers present to be swept across the reverse-biased collector-base junction.



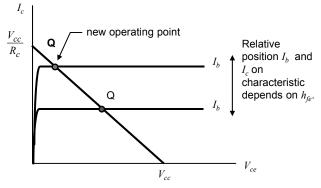
In this circuit, the voltage  $V_{ce}$  is not a constant but depends on the current  $I_c$ . If  $I_c$  increases, then so does the voltage drop across  $R_c$  and thus voltage  $V_{ce}$  decreases. Thus, if  $I_b$  is increased such that  $I_c$  becomes equal to the maximum allowed by  $R_c$ , then  $V_{ce}$  must be approaching zero volts – this is called **saturation**.

### 5.7 Simple Bias

Bias voltage is a steady DC voltage applied to the transistor at all times. This voltage is necessary so that the p-n junctions are placed in forward and reverse bias as appropriate so that correct transistor operation is obtained.



If  $h_{fe}$  increases (e.g., by changing the transistor for another one) then the transistor characteristic is changed and for a given  $I_b$  (fixed by  $V_b$ ),  $I_c$  increases and the relative position of the operating point (the Q point) on the load line changes.



This is not desirable since  $h_{fe}$  varies due to manufacturing variables and may vary anywhere from 100 to 200. For reasons to be given later, we require the operating point to remain approximately in the middle of the load line even when  $h_{fe}$  changes.

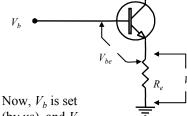
#### 5. Bipolar Junction Transistor

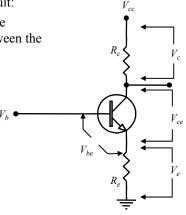
#### 5.8 Emitter Bias

The disadvantages of the simple bias arrangement can be overcome by the emitter bias circuit:

Remove  $R_b$  and let  $V_b$  represent the voltage measured at the base. Then, insert  $R_e$  between the emitter and earth.

Consider the "input" side of this circuit:





(by us), and  $V_{be}$ 

remains at about

0.7 V; thus the voltage drop across  $R_e$  is given by  $V_e = V_b - V_{be}$ .

The potential at the top of  $R_e$  is fixed by setting  $V_b$ . However, there are two currents running through  $R_e$ , i.e.,  $I_e = I_b + I_c$ , but for all practical purposes:  $I_e \approx I_c$ Thus:  $V_{\rho} = I_{c}R_{\rho}$ 

$$\begin{split} I_c R_e &= V_b - V_{be} \\ I_c &= \frac{V_b - V_{be}}{R_e} \quad \text{ all independent of } h_{fe} \end{split}$$

That is,  $I_c$  is fixed by the value of  $R_e$ . But, you say, what about  $I_b$ ? Doesn't  $I_b$ control  $I_c$ ? Yes it does, but here the focus is on  $I_c$  and  $I_b$  follows (according to the value of  $h_{fe}$ ). That is, we choose a "design value" of  $I_c$  by selecting  $R_e$ and  $V_b$  (assuming  $V_{be} = 0.7$  V). The "correct" base current  $I_b (= I_c/h_{fe})$ automatically flows when  $V_h$  is applied.

The load line for the circuit becomes: The underlying assumption is that  $h_{fe}$  is large. If  $I_b (= I_c/h_{fe})$  is included, then:  $V_e = \left(I_c + \frac{I_c}{h_{fe}}\right)R_e$  $I_c + \frac{I_c}{h_{fe}} = \frac{V_{bb} - V_{be}}{R_e}$ 

$$I_c = -\frac{1}{R_c + R_e} V_{ce} + \frac{V_{cc}}{R_c + R_e}$$

 $V_{cc}$ 

 $R_c$ 

 $V_{be}$ 

#### 5.9 Stabilisation

In the emitter bias circuit, if  $R_c$  is decreased, then  $V_c$  decreases and  $V_{ce}$  must increase by the same amount to compensate.  $I_c$  remains constant to maintain voltage drops from  $V_b$  down to earth.

If  $R_e$  increases, then  $V_e$  increases. Any increase in  $V_e$  has an important effect on  $I_b$ , as will be described below.

What happens if  $h_{fe}$  changes in emitter bias circuit?

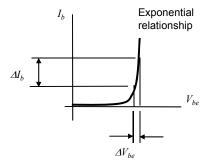
Coming down the right hand side of the circuit, we have:

$$V_{cc} = V_c + V_{ce} + V_e$$
  
=  $I_c R_c + V_{ce} + I_c R_e$   
=  $I_c (R_c + R_e) + V_{ce}$ 

If  $h_{fe}$  goes up (e.g., transistor is heated), then, for a given  $I_b$ ,  $I_c$  increases by some small amount  $\Delta I_c$ . If  $I_c$  increases, then  $V_c$  also increases and so also does  $V_e$ . Thus,  $V_{ce}$  must decrease to keep the voltage drops from  $V_{cc}$  to earth consistent. But  $V_b = V_{be} + V_e$ .

If  $V_e$  increases, then  $V_{be}$  must decrease since  $V_b$  is set:

- But  $V_{be}$  is the forward biasing voltage for the baseemitter junction. Hence a small drop in  $V_{be}$  results in a large drop in  $I_{b}$ .
- But a decrease in  $I_b$  results in a decrease in  $I_c$ . A new equilibrium is reached and  $I_c$  settles down to its former value with a reduced  $I_b$ being the result of the increased  $h_{fe}$ .  $I_c/I_b = h_{fe}$  as always but in this circuit,  $I_c$  is controlled (and hence the Q point) and  $V_{be}$  and hence  $I_b$ change to account for any variations in  $h_{fe}$ . The circuit is stabilised against changes in  $h_{fe}$ .



#### 5. Bipolar Junction Transistor

#### 5.10 Voltage Amplifier

Although we have so far examined the bias characteristics of the emitter bias circuit, we may note that the voltage at the collector  $V_{ce}+V_e$  could be considered an output voltage  $V_{out}$  and  $V_b$  may be considered an input voltage.

Any variations in the input voltage  $\Delta V_b$  constitute an **input signal**. Corresponding variations in the output voltage  $\Delta V_{out}$  is an **output signal**.

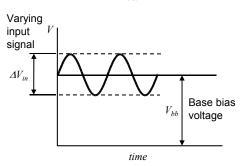
Small variations  $\Delta V_{in}$  cause large variations  $\Delta V_{out}$  because of the effect of the current gain  $h_{fe}$ . The ratio of the two signals is the **voltage gain**  $A_{v}$ .

$$\frac{\Delta V_{out}}{\Delta V_{in}} = A_v$$

 $V_{in} = V_b$ 

Later we will see how this voltage gain is obtained in more detail. For now, let us assume that such a voltage gain is possible and that small variations at the input  $\Delta V_{in}$  lead to large variations in the output  $\Delta v_{out}$ .

But, a varying input signal must not send the transistor to **cut-off** or **saturation** since then the output signal will be distorted or clipped. Further, the varying input signal must always be positive (i.e.,  $V_{be} >$ 0.7 V) so that the base-emitter junction is always in forward bias.



 $V_{cc}$ 

 $V_c$ 

 $V_{ce}$ 

 $V_{out} = V_{ce} + V_e$ 

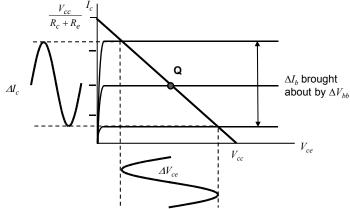
R,

 $V_{be}$ 

A bias voltage is a steady DC voltage applied to the transistor base so that correct transistor operation is obtained without cut-off or saturation when a varying input signal  $\Delta V_{in}$  appears in the input.

#### 5.11 Bias

The DC bias is set so that the operating point (the Q point) is halfway along the load line. This ensures that we get maximum output voltage swing at  $V_{out}$  without the transistor saturating or reaching cut-off.



Since, in the emitter bias circuit, the emitter potential is above that of earth  $(V_e)$  then at saturation,  $V_{out} = V_e$ . At cut-off,  $V_{out} = V_{cc}$ ; thus the output voltage can only swing between  $V_{cc}$  and  $V_e$  in this circuit.

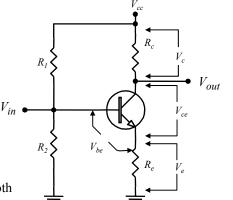
We can now call the voltage at the base " $V_{bb}$ " (for **base bias voltage**). A convenient way of supplying a steady  $V_{bb}$  is to use a voltage divider from the supply  $V_{cc}$ .

$$I_c = \frac{V_{bb} - V_{be}}{\prod_{e} R_e}$$

We must choose the bias voltage  $V_{bb}$  so that  $I_c$  falls in the middle of the load line.

The supply voltage  $V_{cc}$  provides both power for the output signal and also a

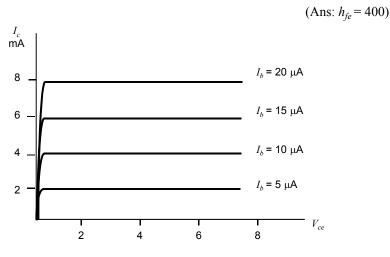
voltage  $V_{ce}$  which keeps the collector base junction in reverse bias. The combined value of  $R_c$  and  $R_e$  limits the maximum collector current (which may need limiting so as to not overload the transistor) and  $R_e$  should not be made too large so that there is sufficient allowable voltage swing at the output  $V_{our}$ 



#### 5. Bipolar Junction Transistor

### 5.12 Review Questions

1. Determine the current gain  $(h_{fe})$  of the transistor characteristic shown below in the normal operating region

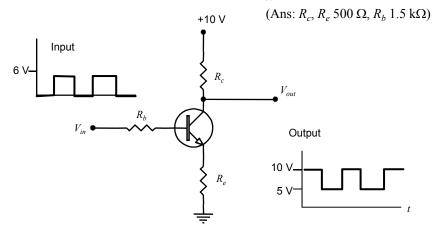


2. Using the equation below, plot  $I_c$  vs  $V_{ce}$  for  $I_0 = 10^{-15}$ A and  $V_A = 100$  V for  $V_{ce} = 5$ , 10, 15, 20, 25 V and  $V_{be} = 0.65$ , 0.675 and 0.7 V at T = 300 K (leave plenty of room on the negative x axis).

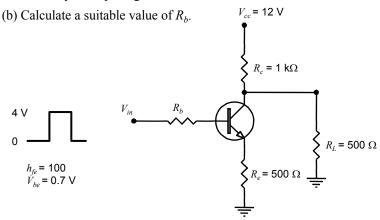
$$I_c = I_0 e^{\frac{qv_{be}}{kT}} \left(1 + \frac{V_{ce}}{V_A}\right) \qquad \qquad k = 1.38 \times 10^{-23} \\ q = 1.6 \times 10^{-19}$$

 $V_A$  is called the **Early voltage** and is the point on the –ve  $V_{ce}$  axis where the characteristic curves meet. Draw these characteristic curves on your graph and extrapolate them to the  $V_{ce}$  axis and indicate the Early voltage.

3. The switching circuit shown below converts a 0 to 6 V pulse into a 10 V to 5 V pulse. Determine the values of the components  $R_b$ ,  $R_e$  and  $R_c$  given that the current gain is 50 and the maximum current drawn from the 10 V power supply is 10 mA. Assume  $V_{be} = 0.7$  V.



- 4. The transistor switch below is operated by a 4 volt signal.
  - (a) Calculate the corresponding output voltages for input voltages of both 0 and 4 volts. Assume that the transistor is put either into saturation or cut-off by the input signal.



(Ans:  $V_{out}$  4, 2.4 V,  $R_b$  18.7 k $\Omega$ )

# 6. Common Emitter Amplifier

Summary  
Common emitter amplifier  

$$V_T = I_b R_T + V_{be} + I_c R_e$$

$$= I_b R_T + V_{be} + h_{fe} I_b R_e$$

$$= I_b (R_T + h_{fe} R_e) + V_{be}$$

$$h_{fe} = \frac{I_c}{I_b}$$

$$V_c = I_c R_c$$

$$I_c = \frac{V_e}{R_e}$$

$$V_{cc} = V_c + V_{ce} + V_e$$

$$V_{bb} = V_{be} + V_e$$

$$h_{ie} = \frac{25}{I_c} h_{fe}$$

$$h_{ie} = r_e h_{fe}$$

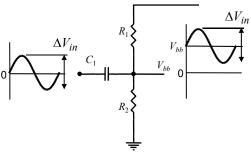
$$r_e = \frac{25}{I_c}$$

$$A_v = -\frac{R_{out}}{h_{ie}} h_{fe} = -\frac{R_{out}}{r_e}$$

$$= -R_{out} \frac{I_c}{25}$$

# 6.1 Coupling Capacitors

A voltage amplifier produces an output voltage that is proportional to the input voltage. Most signals that require magnification are AC.

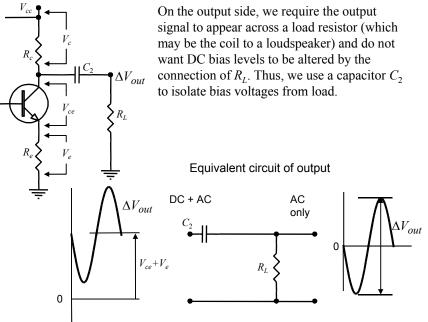


 $R_1$  and  $R_2$  provide the proper bias voltage to the base emitter junction. The input signal  $\Delta V_{in}$  needs now to be superimposed onto the DC bias level but the signal source should not load the circuit in any way. An isolating input **coupling capacitor**  $C_1$  is inserted to isolate transistor bias voltages from DC voltages from the signal source.

For a capacitor:

 $X_c = \frac{1}{\omega C} \qquad \begin{array}{c} \text{Open circuit @ low } \omega \\ \text{Short circuit @ high } \omega \end{array}$ 

Low frequency response is limited by  $C_1$ . The 3 dB point is calculated from  $R\omega C = 1$  where R is the input resistance  $R_{in}$  of the circuit.



#### 6.2 Bypass Capacitor

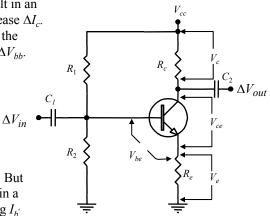
In the stabilised biasing circuit, a resistor  $R_e$  was inserted to keep the emitter potential a little bit above earth so that the collector current and  $V_{ce}$  would not be affected by changes in  $h_{fe}$  (stable DC bias Q point).

Consider a slight increase in  $V_{bb}$  to  $V_{bb} + \Delta V_{bb}$ . This would result in an increase  $\Delta I_b$  and hence increase  $\Delta I_c$ . But, since  $\Delta I_c = h_{fe} \Delta I_b$ , then the resulting  $\Delta V_e$  is larger than  $\Delta V_{bb}$ .

$$\Delta V_{bb} = \Delta V_{be} + \Delta I_c R_e$$
This term is
large compared

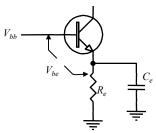
to  $\Delta V_{bb}$ .

This means that  $V_{be}$  must be reduced by an amount  $\Delta V_{be}$ . But any reduction in  $V_{be}$  results in a stabilising effect by reducing  $I_{b'}$ etc. However, for AC signals, we do not want this stabilising effect. We want changes in  $I_b$  to result in large changes in  $I_c$  but the mean value of  $I_c$  to remain at a Q point in the middle of the load line.



Thus, on the one hand, we require  $R_e$  to provide DC bias stability but on the other hand, we do not want  $R_e$  to reduce the signal, or AC voltage gain. The solution? Insert a "bypass" capacitor across  $R_e$  so that AC signals proceed directly to earth while DC bias is still stabilised.

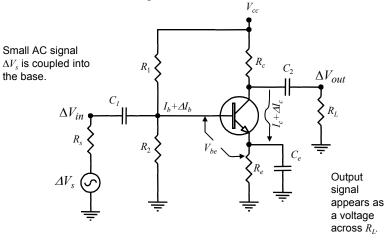
This bypass capacitor has a significant effect on the AC performance of the circuit and we shall have cause to examine its effect later on in more detail.



## 6.3 Voltage Amplifier

Voltage amplifying circuit

Emitter bias circuit with voltage divider



How does it work?  $\Delta V_{in}$  causes  $\Delta V_{be}$   $\Delta V_{be}$  results in  $\Delta I_b$   $\Delta I_b$  results in  $\Delta I_C$  $\Delta I_c$  results in  $\Delta V_{ce}$  which is  $\Delta V_{out}$  This circuit is called a **common emitter amplifier** because it is the emitter that is common to both the input (the base) and the output (the collector).

Note: if  $\Delta V_{in}$  is positive (an increase in voltage at  $V_b$ ) then  $\Delta V_{be}$  increases, which results in an increase in  $I_b$  and hence an increase in  $I_c$ . Thus,  $V_c$  goes up and  $V_{ce}$  goes down by  $\Delta V_{ce}$ . That is, the output is out of phase with the input signal by 180°.

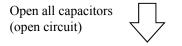
How to analyse this circuit?  $\longrightarrow$  Treat AC and DC separately. Given resistances and supply voltage, what are all the other voltages?

DC	AC
Open all capacitors	<ul> <li>Reduce DC sources to 0 volts</li></ul>
(open circuit)	(AC earth) <li>Short all capacitors</li>

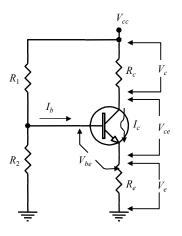
### 6. Common Emitter Amplifier

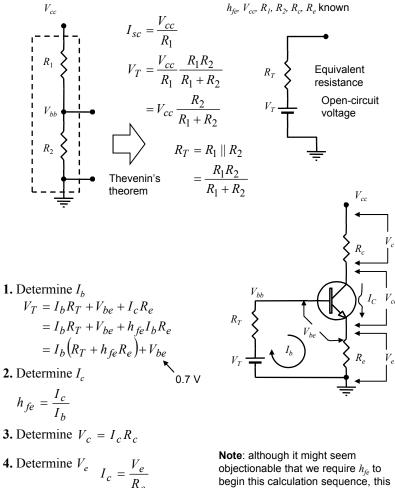
# 6.4 DC Analysis

 $V_{cc}$ Start with complete circuit:  $R_c$  $R_1$  $C_2$  $\Delta V_{out}$  $I_b + \Delta I_b$  $\Delta V_{in}$  $R_L$ R,  $R_2$  $V_{be}$  $C_e$ R,  $\Delta V_s$ 









Begin with simplifying the DC bias circuit using Thevenin's theorem.

5. Determine  $V_{ce}$ 

$$V_{cc} = V_c + V_{ce} + V_e$$

6. Determine

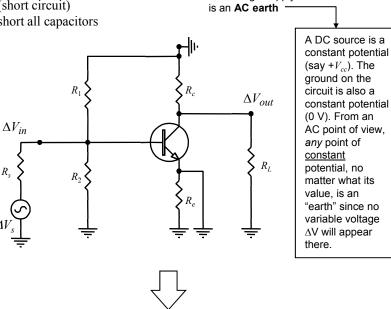
$$V_{bb} = V_{be} + V_{e}$$

**Note**: although it might seem objectionable that we require  $h_{fe}$  to begin this calculation sequence, this arises because we are taking into account the base current  $I_b$  and its effect on the current through  $R_2$ . If we disregard the base current and assume that the current through  $R_1$ and  $R_2$  is much larger than  $I_b$ , then  $h_{fe}$ need not be known beforehand.

# 6.5 AC Analysis

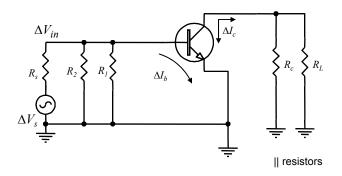
Start with complete circuit:

- reduce DC sources to 0 volts (short circuit)
- short all capacitors

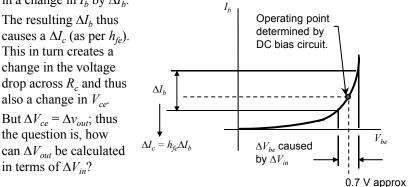


DC voltage supply

AC circuit

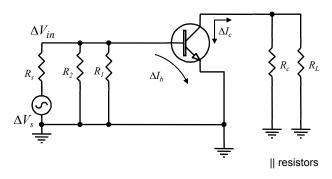


 $\Delta V_{in}$  at the base produces a  $\Delta V_{be}$  at the forward bias base-emitter junction (since the bypass capacitor shorts the emitter to ground). This  $\Delta V_{be}$  results in a change in  $I_b$  by  $\Delta I_b$ .



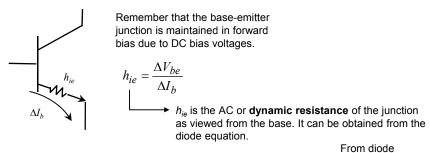
The first step is to determine: "What base current  $\Delta I_b$  is produced by the input voltage signal  $\Delta V_{in}$ ?"

Once we know  $\Delta I_b$  we can get  $\Delta I_c$  and hence  $\Delta v_{out}$ .



Observe that the presence of the bypass capacitor causes a portion  $(\Delta I_b)$  of the AC input current  $(\Delta I_s)$  to pass straight from  $\Delta V_{in}$  through the forward bias base-emitter junction directly to earth (the remainder going through the parallel resistors  $R_{1,2}$ ). Thus,  $\Delta V_{in} = \Delta V_{be}$ .

To get  $\Delta I_b$ , we must find out the resistance of the base-emitter junction (*as viewed from the base*). This is given the symbol  $h_{ie}$ .

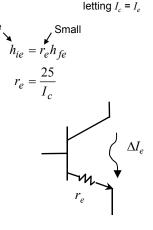


How to get  $h_{ie}$ ? It is given by the local slope of the *I*-*V* curve at the particular value of  $V_{be}$ ; hence:

 $I_{b}$   $h_{ie} = 1/\text{slope}$   $h_{ie} = \frac{25}{I_{b}}$  DC base current in mA  $= \frac{25}{I_{b}} I_{c}$   $h_{ie} = \frac{25}{I_{b}} I_{c}$   $h_{ie} = \frac{25}{I_{c}} h_{fe}$   $h_{ie} = \frac{25}{I_{c}} h_{fe}$   $DC \text{ emitter current in mA & a lot ion <math>I = I$ 

Large

From the emitter's point of view, a large current  $(\Delta I_e)$  appears to pass across the b-e junction. But, from the base point of view, only a small current  $(\Delta I_b)$  appears to pass across the b-e junction. Hence, when looking from the base to the emitter, the resistance  $h_{ie}$  appears large. When looking up from the emitter, the resistance appears to be small and is given the symbol  $r_e$ . The ratio of the two resistances is  $h_{ie}$ .

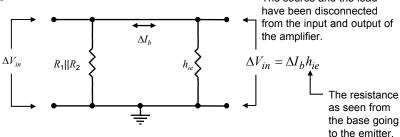


equation at T

= 300K

#### 6.6 Input and Output Resistances – AC

Consider the resistances (more correctly "impedances") as seen from the input terminals of the circuit to earth. The source and the load

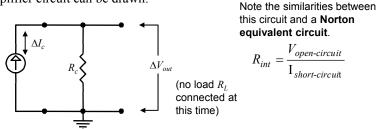


The input resistance is  $R_{in} = R_1 ||R_2||h_{ie}$ .

In a fully stabilised bias circuit, it is  $I_c$  which is "controlled" or designed and  $I_b$  adjusts according to the value of  $h_{fc}$ .

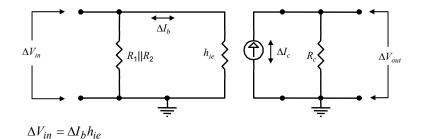
It will be later shown that (for other reasons)  $R_T = R_1 ||R_2$  is made >>  $h_{ie}$  so that the input resistance of the amplifier is dominated by the value of  $h_{ie}$  (since  $h_{ie}||R_T$ ). It is desirable to have a high input resistance so  $h_{ie}$  should be made to be fairly large – by choosing the lowest possible value of  $I_c$ .

For a given  $\Delta I_b$ , there will be a constant  $\Delta I_c$  in the collector, or output side of the circuit. That is, the transistor acts as a constant current source across which is connected a resistor  $R_c$ . This is the same situation as a Norton constant current source and parallel resistor. Thus, the output "half" of the amplifier circuit can be drawn:



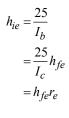
For the moment, we may refer to  $R_c$  as being the **output resistance** of the amplifier circuit  $R_{out}$  (i.e., no load resistor  $R_L$  present).

# 6.7 AC Voltage Gain



 $\Delta V_{out} = -\Delta I_c R_{out}$ 

If the load resistor is connected, then  $R_{out} = R_c || R_L$ .



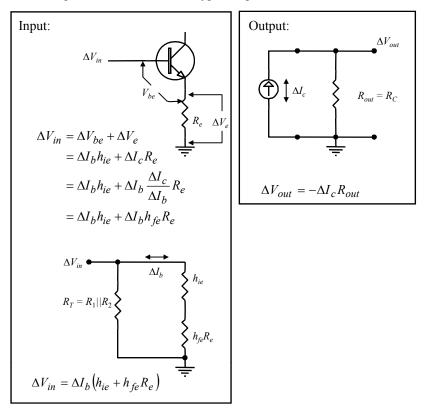
$$A_{v} = \frac{\Delta V_{out}}{\Delta V_{in}}$$
$$= -\frac{\Delta I_{c} R_{out}}{\Delta I_{b} h_{ie}}$$
$$A_{v} = -\frac{R_{out}}{h_{ie}} h_{fe}$$
$$Voltage gain$$
$$= -\frac{R_{out}}{r_{e}}$$
$$= -\frac{R_{out}}{r_{e}} I_{c} \text{ in mA}$$

Sign indicates phase shift. If  $\Delta V_{in}$  is positive,  $\Delta I_b$  is positive and  $\Delta I_c$  is positive. If  $\Delta I_c$  is +ve, then  $I_c$  increases slightly, which means that  $V_c$  increases. Thus  $\Delta V_{out} = \Delta V_{ce}$  must be negative.

Steps in AC analysis: 1. find  $h_{ie}$  (or  $r_e$ ) 2. find  $R_{out}$ 3. calculate  $A_v$ 4. calculate low frequency response at 3 dB point  $1 = R_{in}\omega C$ 

## 6.8 Bypass Capacitor

The AC equivalent circuit without bypass capacitor



Voltage gain *without* bypass capacitor:

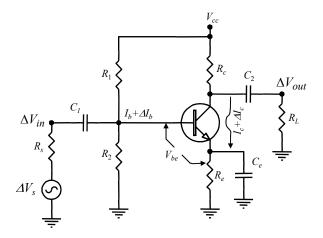
Voltage gain *with* bypass capacitor:

$$A_{v} = \frac{\Delta V_{out}}{\Delta V_{in}} \qquad A_{v} = -\frac{h_{fe}R_{out}}{h_{ie}}$$
$$= -\frac{\Delta I_{c}R_{out}}{\Delta I_{b}(h_{ie} + h_{fe}R_{e})}$$
$$= -\frac{h_{fe}R_{out}}{h_{ie} + h_{fe}R_{e}} \qquad \text{compare}$$

#### 6. Common Emitter Amplifier

### 6.9 Amplifier Design

Designing an amplifier involves choosing components to give the required gain  $A_v$  and input resistance  $R_{in}$ . Also, one must specify the low frequency cut-off so as to select appropriate values of coupling capacitors. The general circuit, with a fully stabilised bias, is:



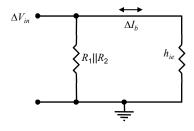
The following procedure allows the values of various components to be established in a systematic way.

- 1. Determine  $V_{cc} = A_v/20$
- **2.** Determine  $I_c$  from  $h_{ie}$  and  $h_{fe}$
- **3.** Determine  $I_b$  from  $I_c/I_b = h_{fe}$
- 4. Determine  $R_c$
- 5. Determine  $V_{ce} = V_{cc}/2$
- 6. Determine  $R_e$  from  $V_e$  and  $I_c$
- 7. Determine  $V_{bb}$  from  $V_{be}$  and  $V_{e}$
- 8. Determine  $R_1$  and  $R_2$
- 9. Determine  $C_e$
- **10.** Determine  $C_1$  and  $C_2$

### 6.10 Amplifier Design - Input Resistance

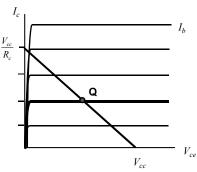
Now,  $R_{in} = R_T || h_{ie}$ . If  $R_T$  is made much larger than  $h_{ie}$ , then the input resistance is dominated by the value of  $h_{ie}$ . There are other constraints on the value of  $R_T$ ; thus keeping  $R_{in}$  as a strong function of  $h_{ie}$  enables us to adjust  $h_{ie}$  to the desired  $R_{in}$ .

One of the most important features of the bias of an amplifier is to obtain a Q point which is at the centre of the load line (to allow maximum swing of the output  $V_{out}$ ). This means that the selection of  $h_{ie}$ (for the desired  $R_{in}$ ) also fixes the collector current  $I_c$  under quiescent conditions (i.e., the value of  $I_c$  when there is no input signal).

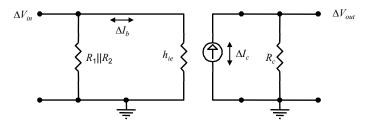


1. Thus, for a design value of  $h_{ie}$ ,  $I_c$ is found from:  $h_{ie} = \frac{h_{fe} 25}{|I_c|}$ 

This is the first step of our step-bystep procedure for designing a common emitter amplifier.



# 6.11 Amplifier Design – $V_{cc}$ , $I_b$



Now,

$$\Delta V_{in} = \Delta I_b h_{ie}$$

$$\Delta V_{out} = -\Delta I_c R_c$$

$$A_v = -\frac{\Delta V_{out}}{\Delta V_{in}}$$

$$= \frac{\Delta I_c R_c}{\Delta I_b h_{fe} 25} I_c$$

$$= \frac{h_{fe} R_c}{h_{fe} 25} I_c$$

$$= \frac{R_c I_c}{25} \qquad h_{ie} = \frac{h_{fe} 25}{I_c}$$

$$= 40V_c \qquad \text{volts}$$

$$V_{cc} \approx \frac{A_v}{20} \qquad \text{since } V_c = V_{cc}/2 \quad (\text{approx})$$

Thus,  $V_{cc}$  is set by the choice of gain  $A_{v}$ .

3. 
$$h_{fe} = \frac{I_c}{I_b}$$

**4.**  $R_c$  may be calculated from:

$$V_c = I_c \boxed{R_c}$$

5. For a Q point to be in the centre of the load line, then:  $V_{ce} = V_{cc}/2$ 

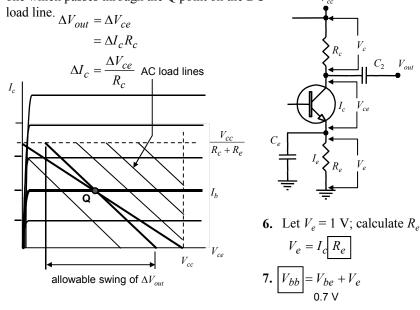
 $I_c = \frac{-V_{ce}}{R_c + R_e} + \frac{V_{cc}}{R_c + R_e}$ 

### 6.12 Amplifier Design – $V_{ce}$ , $V_{e}$ , $V_{bb}$

Now, the bypass capacitor is an AC short to ground potential. Thus,  $\Delta V_{out} = \Delta V_{ce}$ . The slope of the AC load line is simply  $-1/R_c$  (or  $-1/R_c ||R_L$  if  $R_L$ is connected). But, it is only *changes* in  $V_{ce}$  that are described by the AC load line. Thus, we may draw a series of parallel lines, all with slope  $-1/R_c$ , to represent all the possible AC load lines of a circuit.

The actual AC load line appropriate for a particular circuit depends on the choice of  $V_{ce}$  (the DC bias conditions). The DC bias conditions are described by the DC load line:

 $V_{ce}$  (the DC bias conditions). The DC bias conditions are described by the DC load line: Slope of DC load line Thus, the AC load line for a particular circuit is the one which passes through the Q point on the DC  $V_{ce}$ 

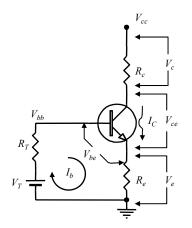


Increasing  $R_e$  would reduce the y axis intercept of the DC load line and also reduce the x axis intercept of the matching AC load line. Adding a load resistor  $R_L$  would increase the slope of the AC load line while leaving the DC load line unchanged, thus reducing the x axis intercept for the AC load line. Thus, to allow maximum swing on the output,  $R_e$  should be selected so as to not make  $V_e$  too large and the Q point should really be selected in the middle of the AC load line. However, selecting  $V_{ce} = V_{cc}/2$  is sufficient for a first approximation (i.e., middle of DC load line).

#### 6. Common Emitter Amplifier

# 6.13 Amplifier Design – $R_T$

As before, the Thevenin equivalent circuit for the DC bias is:



By Kirchhoff: V = L P + (V + L P)

$$V_T = I_b K_T + (V_{be} + I_c K_e)$$
 (1)

$$V_{cc} = V_c + V_{ce} + V_e$$
 ..... (2)

Now, in general:

$$h_{fe} = \frac{I_c}{I_b} \tag{3}$$

Thus, from (1), (2) and (3):

$$V_{ce} = V_{cc} - I_c (R_c + R_e)$$
  
=  $V_{cc} - h_{fe} I_b (R_c + R_e)$   
 $\Downarrow$   
=  $V_{cc} - \frac{h_{fe} (R_c + R_e) (V_T - V_e)}{(R_T + h_{fe} R_e)}$ 

Open-circuit voltage: V = V  $R_2$ 

 $V_T = V_{cc} \frac{R_2}{R_1 + R_2}$ 

Equivalent resistance

$$R_T = \frac{R_1 R_2}{R_1 + R_2}$$

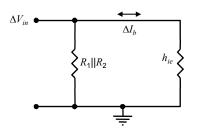
If 
$$R_T$$
 is made << than the product  $h_{fe}R_e$   
then  $V_{ce}$  loses its dependence on  $h_{fe}$ .

$$V_{ce} = V_{cc} - \frac{\left(R_c + R_e\right)\left(V_T - V_{be}\right)}{R_e}$$
$$R_T + h_{fe}R_e \approx h_{fe}R_e$$

 $R_T$  is set so that  $R_T << h_{fe}R_e$ . This ensures that  $V_{ce}$  is "independent" of  $h_{fe}$  and thus a stable Q point.

# 6.14 Amplifier Design – $R_1$ , $R_2$ , $C_1$ , $C_2$

Known:  $h_{ie}$ ,  $h_{fe}$ ,  $R_e$ ,  $V_{cc}$ ,  $V_c$ ,  $V_{ce}$ ,  $V_{bb}$ ,  $I_c$ ,  $I_b$ 



Let  $\frac{R_T}{h_{ie}} \approx \frac{h_{fe}R_e}{R_T}$  This will put  $R_T$  in the middle of  $h_{ie}$  and  $h_{fe}R_e$ .

Thus  $R_T \approx \left(h_{fe} R_e h_{ie}\right)^{1/2}$ 

Now, in the AC circuit,  $R_T$  is in parallel with  $h_{ie}$  and thus if  $R_T$  is too small, then the input resistance of the amplifier will be reduced. This is undesirable. Thus, let  $R_T >> h_{ie}$ .

For acceptable input resistance

For stable Q point

but

$$V_T = I_b R_T + (V_{be} + I_c R_e)$$

$$V_T = \frac{V_{cc} R_2}{R_1 + R_2} \quad (2)$$

 $R_T = \frac{R_1 R_2}{R_1 + R_2} \quad (1)$ 

Thus calculate  $V_T$ .

**8.** Two equations, two unknowns enables  $R_1$  and  $R_2$  to be determined.

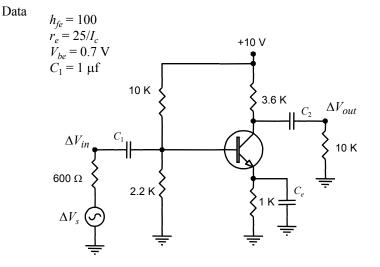
**9.** 
$$C_e$$
 from:  $\frac{1}{\omega C_e} = 0.1R_e$  Reactance of  $C_e$  ensures the lowest possible frequency for amplifier to operate according to design criteria.

**10.**  $C_1$  and  $C_2$  from:

$$\frac{1}{\omega C} = h_{ie}$$
Assume that  $R_r = R_1 ||R_2 \text{ is } >> h_{ie} \text{ so}$ 
that the input resistance is dominated  
by  $h_{ie}$  (which is in parallel with  $R_r$ ).

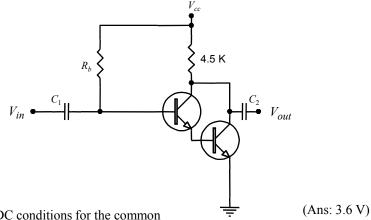
# 6.15 Review Questions

- 1. Analyse the DC and AC operation of the common emitter amplifier shown below, which includes the 10 k $\Omega$  load resistor.
  - (a) Determine the DC bias conditions  $V_{bb}$ ,  $I_b$ ,  $I_c$ ,  $V_{ce}$ ,  $V_e$ ,  $V_c$ .
  - (b) Determine the AC voltage gain  $A_v$  with and without the load resistor  $R_L$  present.
  - (c) Determine the frequency response of the amplifier (i.e., the lowest frequency that may be amplified).

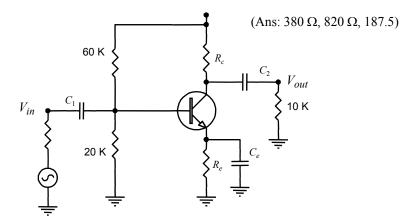


(Ans: 1.78 V, 10.8 µA, 1.08 mA, 5.04 V, 1.08 V, 3.88 V, -114.3, -155, 157 Hz)

2. A common emitter amplifier is constructed from a Darlington pair. If the current gain  $h_{fe}$  and input resistance  $h_{ie}$  of each transistor is 120 and 1.5 k $\Omega$ , respectively, determine the peak-to-peak output voltage if the peak-to-peak input voltage is 10 mV. (Assume that  $R_b >> h_{ie}$  and thus the input resistance of each stage of the amplifier is  $h_{ie}$ .)

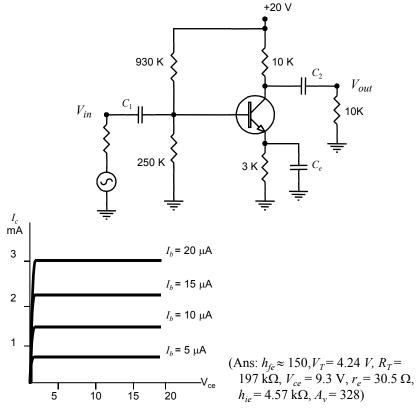


3. The DC conditions for the common emitter amplifier shown below are:  $V_{ce} =$ 6 V,  $I_c = 5$  mA,  $V_{bb} = 2.6$  V. Determine the values of  $R_e$ ,  $R_c$  and  $h_{fe}$ .

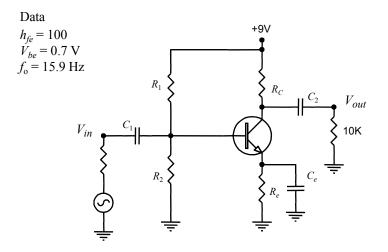


#### 6. Common Emitter Amplifier

- 4. Consider the fully stabilised common emitter amplifier shown below. Also shown is the transistor characteristic in graphical form.
  - (a) Determine an equation for the load line and draw the load line on the transistor characteristic.
  - (b) Using the transistor characteristic, determine a value for  $h_{fe}$ .
  - (c) Determine the Thevenin equivalent circuit  $V_T$ ,  $R_T$  of the base biasing circuit.
  - (d) Apply Kirchhoff's law to the Thevenin equivalent circuit and obtain an expression which relates  $I_c$  to  $I_b$  and thus determine values for  $I_c$  and  $I_b$  for this circuit.
  - (e) Determine  $V_{ce}$  and indicate the Q point on the load line.
  - (f) Determine a value for  $r_e$  or  $h_{ie}$  and thus estimate the AC voltage gain  $A_{y}$ .



5. Design a fully stabilised common emitter amplifier with a voltage gain of 200 and a 9 V battery as the power source. The lowest frequency of operation is to be 15.92 Hz and  $h_{fe}$  for the transistor to be used is 100. Assume that an acceptable input resistance is 1 k $\Omega$  and let the voltage across  $R_e$  be set to 0.5 V and that  $V_{be} = 0.7$  V.



Obtain values for  $R_{c'}$ ,  $R_{e'}$ ,  $C_{e'}$ ,  $R_1$ ,  $R_2$ ,  $C_1$  and  $C_2$ .

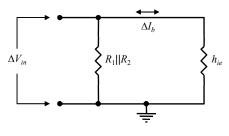
(Ans:  $R_c = 2 \text{ k}\Omega$ ,  $R_e = 200 \Omega$ ,  $C_e = 500 \mu\text{F}$ ,  $R_1 = 30 \text{ k}\Omega$ ,  $R_2 = 5.2 \text{ k}\Omega$ ,  $C_{1,2} = 10 \mu\text{F}$ ,  $I_c = 2.5 \text{ mA}$ )

# 7. Input/Output Impedance

Summary		
$R_{in} \approx h_{ie}$	Input resistance (common emitter)	
$R_{int} = \frac{\Delta V_{oc}}{\Delta I_{sc}}$	Output resistance (common emitter)	
$A_{v} = \frac{h_{fe}R_{e}}{h_{ie} + h_{fe}R_{e}}  \text{Common collector voltage gain}$		
$R_{in} \approx h_{fe} R_e$	Input resistance (common collector)	
$R_{out} = \frac{R_s}{h_{fe}}$	Output resistance (common collector)	

# 7.1 Common Emitter Input Impedance

The **input impedance** is that seen by someone looking in at  $\Delta v_{im}$ .

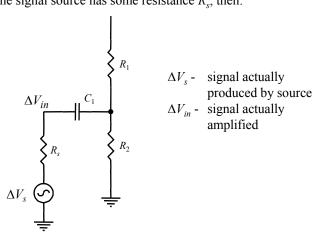


The total input impedance is  $R_{in} = R_1 ||R_2||h_{ie}$ 

If  $R_1 || R_2$  is made larger than  $h_{ie}$  (which is usually the case), then the input resistance is approximately equal to  $h_{ie}$ .

$$R_{in} \approx h_{ie}$$

If the signal source has some resistance  $R_s$ , then:



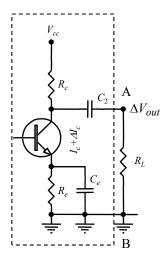
Ideally,  $R_{in} >> R_s$  because otherwise, there is negligible  $\Delta V_{in}$  at amplifier input. If  $R_s$  is large compared to  $R_{in}$ , then most of the voltage variations  $\Delta V_s$  appear across  $R_s$  and not at the amplifier input.

Amplifiers should have a high **input impedance**  $R_{in}$  compared to  $R_s$ . A typical value of  $h_{ie}$  is 1 k $\Omega$ , which is not all that much different from a typical  $R_s$ .

#### 7. IO Impedance

### 7.2 Common Emitter Output Impedance

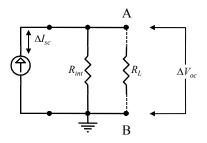
Consider the output side of the CE amplifier circuit.  $\Delta V_{out}$  is applied to a load resistor  $R_L$ .



It should be possible to replace this two-terminal "supply" by a Norton equivalent circuit consisting of a constant current generator which supplies  $\Delta I_{sc}$ and an internal parallel resistance  $R_{int}$ .

A **Norton equivalent circuit** is like a black box that contains a special generator that produces a variable voltage but always produces a constant current *I* equal to the short-circuit current no matter what value of  $R_L$  is connected to the output terminals.

A bipolar junction transistor is a current generator that produces a constant  $\Delta I_c$ . In the CE amplifier circuit, this constant  $\Delta I_c$  manifests itself as a voltage  $\Delta V_{out}$  across  $R_{int}$ .



The internal resistance is the **output resistance** of the circuit and is obtained from:

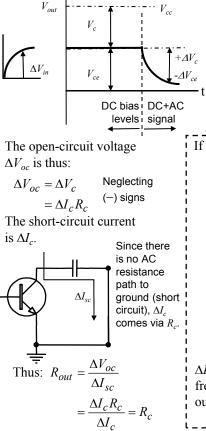
$$R_{int} = \frac{\Delta V_{oc}}{\Delta I_{sc}}$$

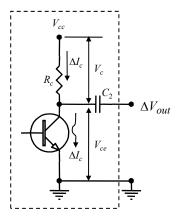
The output impedance is the "internal" resistance of a **Norton equivalent circuit** found from:  $p = \Delta V_{oc}$ 

$$R_{out} = \frac{\delta c}{\Delta I_{sc}}$$

We can ignore the presence of  $R_e$  at this stage since in the AC circuit, it is shorted to ground by the bypass capacitor.

Consider the trace on an oscilloscope connected just before  $C_2$  as there is a rise in the input voltage (+ve  $\Delta V_{in}$ ).





A  $+\Delta V_{in}$  (an "upswing" on the input signal) will produce a  $+\Delta I_b$  and hence a  $+\Delta I_c$ . This results in an increase in  $V_c$ by an amount  $+\Delta V_c$  across  $R_c$  and a corresponding decrease in  $V_{ce}$  by  $-\Delta V_{ce}$  (bypass capacitor shorts AC signal to ground at emitter so  $\Delta V_e = 0$ ).

Signal to ground at emitter so  $\Delta V_e = 0$ + $\Delta V_c = -\Delta V_{ce} = -\Delta V_{out}$ If a load resistor  $R_L$  is connected:  $V_c = \Delta I_1 R_c$  $V_c = \Delta I_1 R_c$  $R_L$  $\Delta I_c \text{ comes from both } R_c \text{ and } R_L; \text{ hence,}$ 

 $\Delta I_c$  comes from both  $R_c$  and  $R_L$ ; hence, from an AC point of view, the total output resistance is:  $R_{out} = R_c || R_L$ 

# 7.3 AC Voltage Gain

For a common emitter circuit, the AC voltage gain is:

$$A_{v} = -\frac{h_{fe}R_{out}}{h_{ie}}$$

For the amplifier on its own (with no load  $R_L$  connected)

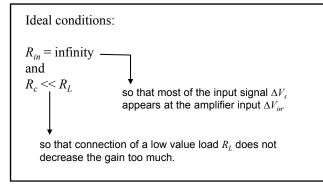
 $R_{out} = R_c$ 

If a load resistor is connected, then this appears in parallel with  $R_c$ , thus reducing the total effective output impedance  $R_{out}$  and thus reducing the gain.

 $R_{out} = R_c \parallel R_L$ 

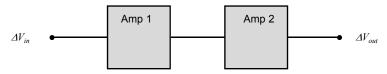
It is desirable that the connection of a load to the amplifier does not significantly reduce the gain (since if it did, we would have to specify the load too precisely for a given circuit design). Thus, for maximum "versatility" of the circuit, we need to have  $R_c$  be much less than any envisaged load  $R_L$ . That is, the **open-circuit output resistance**,  $R_{out} = R_c$ , should be as low as possible.

The ideal conditions for an amplifier are thus:



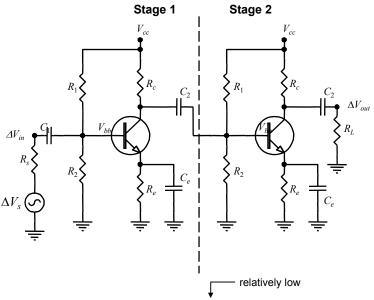
### 7.4 Impedance Matching

One method of increasing the gain for a particular application is to run two amplifiers together:



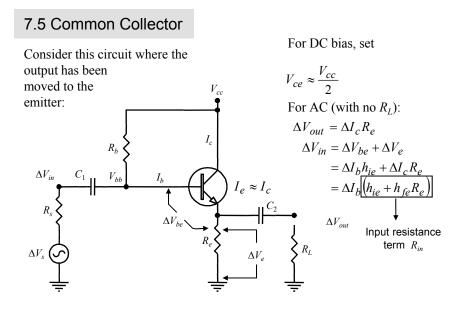
The overall gain would then be expected to be the product of the individual gains  $\longrightarrow$  but this is not observed.

Consider the circuit in detail:



The input impedance of the second stage  $(R_1||R_2||h_{ie})$  acts as a load resistance  $R_L$  for the output of the 1st stage. This reduces the gain  $A_v$  of the first stage since  $R_1||R_2||h_{ie}$  of the second stage is usually much less than  $R_c$ of the first stage.  $(R_1||R_2||h_{ie})||R_c$ 

$$A_{v} = -\frac{h_{fe}R_{out}}{h_{ie}}$$



Notes:

• In calculating  $\Delta V_{in}$ , we have ignored  $R_b$ , which is a path to (virtual) earth. However, if  $R_b$  is large compared to  $h_{ie} + h_{fe}R_e$  then it may be ignored. If included, then  $R_b$  appears in parallel with  $(h_{ie} + h_{fe}R_e)$ .

 $\Delta V_{in} = \Delta I_b \left[ \left( h_{ie} + h_{fe} R_e \right) \| R_b \right]$ 

• If an external load  $R_L$  is connected, then this appears in parallel with  $R_e$  and must be included with  $R_e$  in calculations.

 $\Delta V_{in} = \Delta I_b \left( h_{ie} + h_{fe} \left( R_e \parallel R_L \right) \right)$ 

Open-circuit AC voltage gain:

$$A_{v} = \frac{\Delta V_{out}}{\Delta V_{in}} = \frac{\Delta I_{c} R_{e}}{\Delta I_{b} (h_{ie} + h_{fe} R_{e})}$$
$$A_{v} = \frac{h_{fe} R_{e}}{h_{ie} + h_{fe} R_{e}}$$
 which is always less than 1

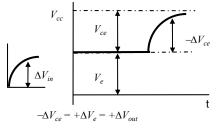
Since the output (emitter) voltage is in phase with the input, the **common collector** circuit is often called an **emitter follower**. In this circuit, it is the collector that is common to the input and the output.

### 7.6 Common Collector Output Impedance

As with a CE circuit, the Common Collector (CC) circuit can be replaced with a Norton equivalent circuit consisting of a constant current source and a parallel resistor which is the output resistance of the circuit.

$$R_{out} = \frac{V_{open \ circuit}}{I_{short \ circuit}}$$

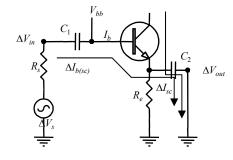
Now, since the input resistance of the common collector circuit is high, we can say that  $\Delta V_s = \Delta V_{in}$ , i.e., ignore the drop across  $R_s$ . Thus the open-circuit voltage



is  $\Delta V_s = \Delta V_{in} = \Delta V_{out}$  since  $A_v \approx 1$  and  $R_{in}$  is high.

In this circuit, the output is taken from the emitter. Hence a short circuit at the output increases the base current  $\Delta I_b$  since  $R_e$  is now bypassed (this is different from the CE circuit where a short circuit at the output does not affect  $\Delta I_b$ ). Hence, w.r.t.  $\Delta V_s$ , we have:

$$\Delta V_s = \Delta I_{b(sc)} (R_s + h_{ie})$$
$$= \frac{\Delta I_{sc}}{h_{fe}} (R_s + h_{ie})$$
$$\Delta I_{sc} = \frac{\Delta V_s h_{fe}}{(R_s + h_{ie})}$$



$$R_{out} = \Delta V_{out} / \Delta I_{sc}$$

$$R_{out} = \Delta V_s \frac{(R_s + h_{ie})}{\Delta V_s h_{fe}}$$

$$R_{out} = \frac{R_s + h_{ie}}{h_{fe}}$$
or
$$R_{out} = \frac{R_s}{h_{fe}}$$

Output resistance:

if 
$$h_{ie} \ll R_s$$
.

The **common collector** circuit has effectively reduced  $R_s$  by a factor of  $h_{fe}$ . The signal source with resistance  $R_s$  has been transformed into a signal source with a very low impedance  $R_s/h_{fe}$ . If  $V_s$  and  $R_s$  are actually  $V_{out}$  and  $R_{out}$  of a CE amplifier, then  $V_{out}$  can now appear to come from a low impedance output.

# 7.7 Common Collector Input/Output Impedance

#### Input impedance

#### **Output impedance**

$$\Delta V_{in} = \Delta I_b (h_{ie} + h_{fe} R_e)$$

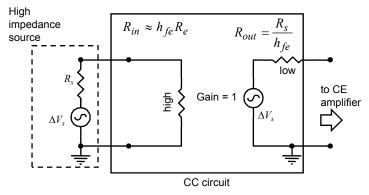
$$\boxed{R_{in} \approx h_{fe} R_e}$$
Compare with CE amp  $R_{in}$ 
May also need to
include  $R_b$ 

$$R_{out} = \frac{R_s}{h_{fe}}$$

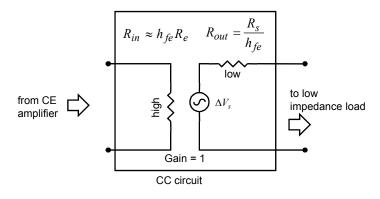
or

$$R_{out} = \frac{R_s + h_{ie}}{h_{fe}} \quad \text{if } h_{ie} \\ \text{included}$$

The CC circuit provides a suitably low source impedance from a high impedance source to a CE circuit.

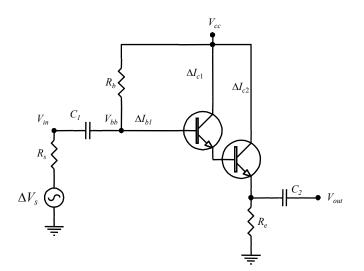


or the CC circuit provides a suitably high output impedance for the CE circuit for a low impedance load.



# 7.8 Darlington Pair

The impedance matching effect depends on  $h_{fe}$ . This may be enhanced by use of a **Darlington pair**:



Overall current gain  $h_{fe} = \Delta I_{c2} / \Delta I_{b1}$ =  $h_{fe1} h_{fe2}$ 

Now, for CC:

$$R_{out} \approx \frac{R_s}{h_{fe}}$$

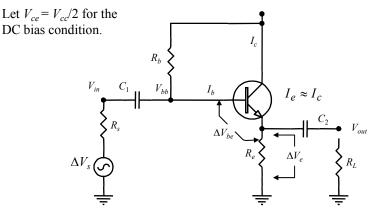
$$R_{in} \approx h_{fe} R_e$$
desirable

Thus, when  $h_{fe}$  is larger,  $R_{in}$  is larger and  $R_{out}$  is smaller. Overall  $h_{fe}$  is increased with a Darlington pair.

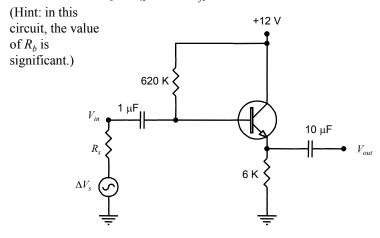
#### 7. IO Impedance

# 7.9 Review Questions

 A common collector circuit is shown below. Determine expressions for the AC voltage gain, input resistance, and output resistance and state any desirable properties of this circuit.

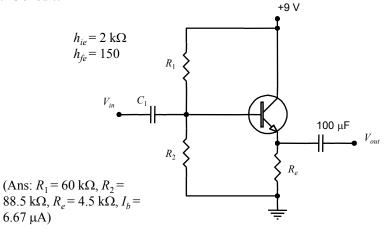


2. Calculate the input and output impedance of the common collector circuit shown below when a source voltage of output impedance  $R_s = 10 \text{ k}\Omega$  is connected to the input.  $h_{ie} = 2 \text{ k}\Omega$ ,  $h_{fe} = 180$ .

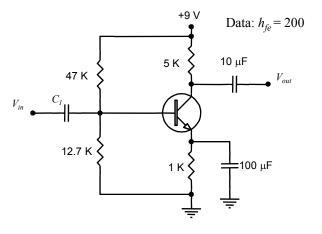


(Ans:  $R_{in} = 394 \text{ k}\Omega$ ,  $R_{out} = 67 \Omega$ )

3. Determine the component values required to bias the fully stabilised common collector amplifier shown below. Assume the emitter is held at  $V_{cc}/2$  when the quiescent collector current is 1 mA and that the lowest frequency of operation is 159.2 Hz. What will be the input impedance of this circuit?

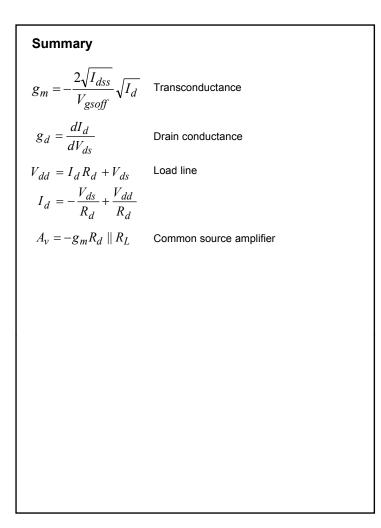


4. The circuit below is a fully stabilised common emitter amplifier with an open-circuit gain  $A_v = 100$ . What will be the overall gain if a pair of these amplifiers is cascaded to produce a two-stage amplifier?



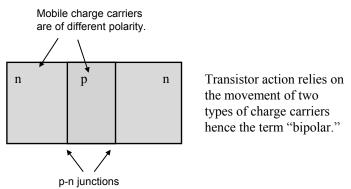
(Ans: 5000)

# 8. Field Effect Transistor



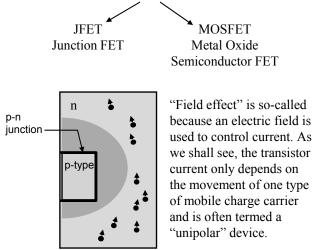
# 8.1 Field Effect Transistor

pnp and npn transistors considered so far are **bipolar junction transistors**. Bipolar junction transistors are current controlled devices. A small  $I_b$  controls a large  $I_c$ .



In a **field effect transistor**, the input *voltage* controls the output current. The input current is extremely small, < 1 pA.

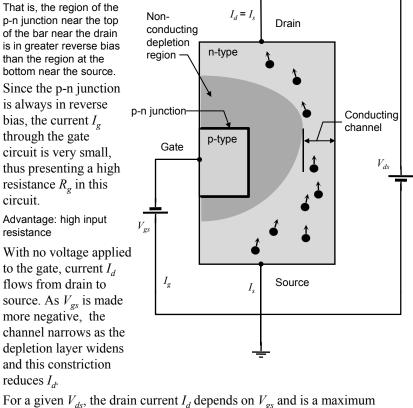
There are two main classes of FETs:



#### 8. Field Effect Transistor

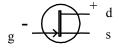
#### 8.2 JFET

When the gate is made negative ( $V_{gs} < 0$ ) the p-n junction is in reverse bias and a depletion region develops. The p-type gate is heavily doped compared to the n-type bar; thus, most of the depletion region exists within the bar. Because the drain is +ve w.r.t. the source, the depletion layer is wider at the top than at the bottom.



For a given  $V_{ds}$ , the drain current  $I_d$  depends on  $V_{gs}$  and is a maximum when  $V_{gs} = 0$ .

Voltage controlled device



n channel FET



p channel FET

 $V_{ds}$ 

### 8.3 JFET Characteristic

How does  $I_d$  vary with  $V_{gs}$  for a fixed value of  $V_{ds}$ ? Transfer characteristic  $I_d$   $\max I_d = I_{dss}$ At  $V_{gs} = 0, I_d$  is a max (no depletion region – channel is widest)  $V_{gsoff}$ 

As  $V_{gs}$  is made more negative, the channel gets narrower and  $I_d$  decreases. The decrease is given by:

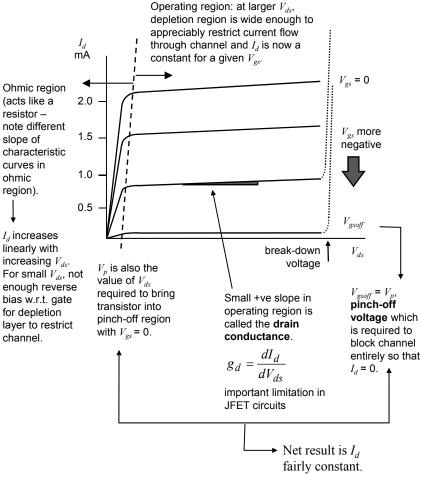
 $I_{d} = I_{dss} \left( 1 - \frac{V_{gs}}{V_{gsoff}} \right)^{2}$ The slope is  $g_{m} = \frac{dI_{d}}{dV_{gs}} = -\frac{I_{dss}}{V_{gsoff}} 2 \left( 1 - \frac{V_{gs}}{V_{gsoff}} \right)$ but  $\sqrt{\frac{I_{d}}{I_{dss}}} = \left( 1 - \frac{V_{gs}}{V_{gsoff}} \right)$ Note,  $g_{m}$ comes out +ve since  $V_{gsoff} \sqrt{\frac{I_{d}}{I_{dss}}} = \frac{2I_{dss}}{V_{gsoff}} \sqrt{\frac{I_{d}}{I_{dss}}}$ Note,  $g_{m}$ comes out +ve since  $V_{gsoff}$  is -ve. Note,  $g_{m}$ depends on square root of drain current. transconductance (units: mA/V = millisiemens) Typical values:

 $I_d = 5 \text{ mA}, V_{gs} = -1 \text{ V}, g_m = 5 \text{ mS}$ 

Anything which makes the p-n junction more reverse biased will affect the drain current. Thus, the transfer characteristic (and hence  $g_m$ ) changes depending on the value of  $V_{ds}$  since a larger  $V_{ds}$  will result in a larger depletion region for a given  $V_{gs}$ .

#### 8. Field Effect Transistor

## 8.4 JFET Drain Curve

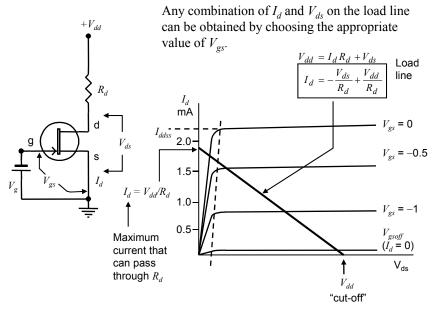


In the operating region, there are two competing conditions:

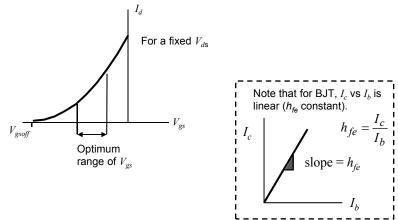
- increasing V<sub>ds</sub> tends to increase I<sub>d</sub> (just as in an ordinary resistor)
- but increasing  $V_{ds}$  makes junction more reversed biased and thus causes narrowing of conduction channel, which tends to decrease  $I_d$

# 8.5 JFET Load Line

Consider this circuit:



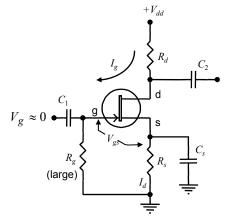
But, we need to choose  $V_{gs}$  so that Q point on the load line is within the operating region, e.g., cannot have  $V_{gs} > 0$ . Also, it is best to have  $V_{gs}$  in a "linear" region of the transfer characteristic to prevent distortion of large AC signals.



#### 8. Field Effect Transistor

## 8.6 JFET Biasing

Now, use of a separate voltage source at gate is not desirable; hence, consider this circuit.

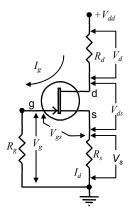


- Here, source is maintained +ve w.r.t. earth by inclusion of  $R_s$ .
- Gate is -ve w.r.t. the source by setting its potential V<sub>g</sub> close to earth (i.e., it can be considered to be 0 V).
- $R_g$  is present to offer a controlled high AC input resistance, and also to provide a path for the small leakage current  $I_g$  through the reverse bias junction to earth. Even though  $R_g$  is made large for large input resistance,  $V_g$  is very small because  $I_g$  is extremely small.

Circuit is self-stabilising. If  $I_d$  increases, voltage across  $R_s$  increases and hence gate becomes more negative w.r.t. source, tending to reduce  $I_d$ .

# 8.7 JFET Amplifier Biasing

DC circuit:



The voltages down the right hand side of the circuit are:

$$V_{dd} = V_d + V_{ds} + V_s$$
  
But,  $V_s = I_d R_s$  since  $V_g \approx 0$   
 $= -V_{gs}$ 

The DC value of  $V_{gs}$  is normally chosen so that the AC signal input has no possibility of producing a total voltage, which makes the gate positive w.r.t. source. For an AC signal with an amplitude of 500 mV,  $V_{gs}$  should be set to about -2.0 V. The resistor  $R_g$  provides a path for any leakage current to pass to earth and not cause any potential change at the gate which would affect the DC

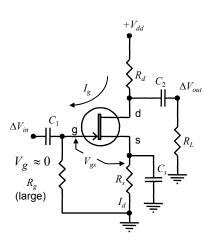
bias conditions.  $R_g$  should be as high as possible to maintain a high input impedance but not too high so that any leakage current produces a significant gate voltage. A value of 1 to 3 M $\Omega$  is usually sufficient.

The choice of 
$$V_{gs}$$
 also fixes the  
value of  $I_d$  thus the voltage  
across the drain resistor  $V_d$  is  
found from  $I_d$  and  $R_d$ :  
 $V_d = I_d R_d$   
For maximum swing on the  
output voltage,  $V_{ds}$  is set to  
approximately half the  
supply  $V_{dd}$ .  
 $I_d$   
 $I$ 

#### 8. Field Effect Transistor

## 8.8 Common Source Amplifier

Fully stabilised common source FET amplifier:



being some distortion of the output due to the non-linear dependence of  $I_d$  on  $V_{gs}$  (i.e.,  $g_m$  changes slightly as  $I_d$  oscillates). Because this non-linearity is a  $I_d$ square law, this results in production of a 2nd harmonic in the output signal. In contrast, in the CE amplifier  $\Delta V_{in}$  $V_{gs}$ causes changes in  $V_{be}$  which produces  $\Delta I_b$ and hence  $\Delta i_{c}$ , leading to  $\Delta V_{out}$ . The exponential  $\Delta V_{gs}$ relationship between  $V_{be}$ and  $I_{b}$  leads to much more harmonic distortion in the output signal compared to FET amp.

Note: AC signals on the input result in there

Voltage gain:

$$A_{v} = \frac{\Delta V_{out}}{\Delta V_{in}} \underbrace{ \begin{array}{c} \Delta V_{out} = -\Delta V_{d} \\ = -\Delta I_{d} R_{d} \end{array}}_{AC \text{ earth}} \text{Suppass capacitor is an } A_{C}$$

$$= -\frac{\Delta I_d R_d}{\Delta V_{gs}} \quad (-) \text{ sign denotes} \\ \text{a phase shift} \\ \text{but } g_m = \frac{\Delta I_d}{\Delta V_{gs}} \quad \text{transconductance} \\ \hline \begin{array}{c} A_v = -g_m R_d \parallel R_L \\ \hline \\ \text{Obtained from} \\ \text{slope of transfer characteristic.} \end{array} \quad \text{If a load resistor} \\ \hline \\ \text{Voltage gain is fixed} \\ \text{by choosing R}_d. \end{array}$$

The transconductance  $g_m$  should be calculated from the slope of the transfer characteristic appropriate to the DC value of  $V_{ds}$  (i.e.,  $V_{ds} = V_{dd}/2$ ) and hence  $I_d$ .

٩C

Without bypass capacitor:  

$$\Delta V_{in} = \Delta V_{gs} + \Delta I_d R_s$$

$$A_v = -\frac{\Delta I_d R_d}{\Delta V_{gs} + \Delta I_d R_s}$$

$$= \frac{-\frac{\Delta I_d}{\Delta V_{gs}} R_d}{\frac{\Delta V_{gs}}{\Delta V_{gs}} + \frac{\Delta I_d}{\Delta V_{gs}} R_s}$$

$$= -g_m \frac{R_d}{1 + g_m R_s}$$
Gain is reduced if no bypass capacitor

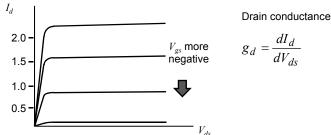
# 8.9 Drain Conductance $g_d$

To obtain a significant voltage gain, a reasonably large value for  $R_d$  is required.

$$A_v = -g_m R_d$$

For  $R_d$  about 10 k $\Omega$ ,  $A_v$  is about 30.

In the BJT, the transistor characteristic is flat, but for a JFET, the small +ve slope in the operating region may be significant compared to the value of  $R_d$ .



 $+V_{dd}$ 

 $R_d$ 

 $C_2$ 

Now, from the transfer characteristic,

$$g_m = \frac{\Delta I_d}{\Delta V_{gs}}$$
$$\Delta I_d = g_m \Delta V_{gs}$$

But for a real JFET,  $\Delta I_d$  depends on the change in  $V_{ds}$  as well as  $\Delta V_{gs}$  because of the non-zero drain conductance  $g_d$ . L

$$A_{v} = -g_{m}R_{d} \| \frac{1}{g_{d}}$$

$$= -g_{m}\frac{R_{d}\frac{1}{g_{d}}}{R_{d} + \frac{1}{g_{d}}}$$

$$= -g_{m}R_{d}\left(\frac{1}{1+R_{d}g_{d}}\right)$$

$$= -g_{m}R_{d}\left(\frac{1}{1+R_{d}g_{d}}\right)$$
Note, the gain is usually expressed as a positive number, but should be used in these formulas as a negative number, e.g.,  $A_{v} = -20$  for a gain of 20.

#### 8. Field Effect Transistor

## 8.10 Amplifier Design

#### Lowest operating frequency

The capacitors  $C_1$  and  $C_2$  serve to isolate the DC bias from the signal source and output device while allowing the AC signal to pass through.

The **3 dB point** is when 
$$\frac{\Delta V_{out}}{\Delta V_{in}} = \frac{1}{\sqrt{2}}$$

For RC high- and low-pass

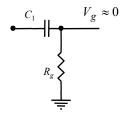
filters, this occurs when  $R\omega C = 1$ .

The 3 dB point fixes the lowest allowable frequency of operation. If frequency of input (or output) signal is less than this condition, then too much of the signal is attenuated by the circuit (i.e., too much AC signal is blocked by the capacitor and thus becomes unavailable for amplification).

At the 3 dB point, we have, for the lowest frequency of operation  $\omega$ :

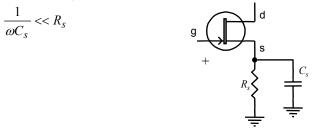
 $C_1$  and  $C_2$  calculated from:

$$1 = R_{\sigma}\omega C$$



#### **Bypass capacitor**

The bypass capacitor  $C_s$  allows the circuit to be self-stabilising for DC bias fluctuations while not offering any resistance to earth for AC signals. Thus, the capacitive reactance should be made much smaller than  $R_s$ .



I, bias

 $V_{gs}$ bias

# 8.11 Amplifier Design Procedure

Given or known parameters: • voltage gain  $A_v$ 

• transfer characteristic

- 1. Estimate values of  $V_{gs}$  and  $I_d$  for a point in the centre of the "linear" region of the characteristic and determine  $I_{dss}$  and  $V_{gsoff}$
- 2. Determine the transconductance  $g_m$

$$g_m = \frac{2\sqrt{I_{dss}}}{V_{gsoff}}\sqrt{I_d}$$

3. Determine the drain conductance 
$$g_d$$
 by measuring the slope of the operating region on the transistor characteristic at the chosen values of  $V_{gx}$  and  $I_d$ 

4. Calculate  $R_d$  from:  $A_v = -g_m R_d$  or  $A_v = -\frac{g_m R_d}{1 + g_d R_d}$ 5. Coloulate  $R_d$  from:  $P_{gg}$ 

5. Calculate 
$$R_s$$
 from:  $R_s = \frac{-r_{gs}}{I_d}$ 

6. Let  $V_{ds} = V_{dd}/2$  and thus calculate  $V_{dd}$  from:  $\frac{V_{dd}}{2} = I_d R_d - V_{gs}$ 

7. Choose  $C_1$  and  $C_2$  so that  $R_g \omega C = 1$  and  $C_s$  so that  $1/\omega C_s << R_s$ 

Note:  $V_{gs}$  is negative, and must be inserted into this formula as is, for example:

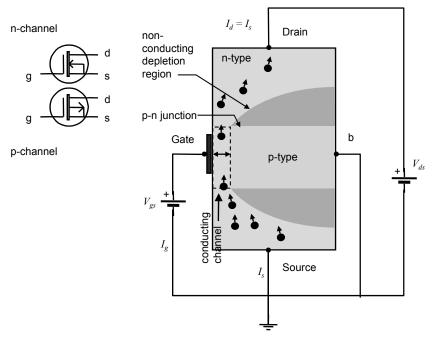
$$\frac{V_{dd}}{2} = I_d R_d - (-1.5)$$

In JFET,  $I_d$  is normally made smaller than  $I_c$  in a BJT circuit so as to avoid the use of a large voltage supply  $V_{dd}$ . For example, if  $I_d$  is 2 mA, and  $R_s + R_d$ = 20 k $\Omega$ , then  $V_{dd}$  = 80 V. Need to lower this to some reasonable value (e.g., 20 V) by sacrificing gain or lowering  $I_d$  (more negative  $V_{gs}$ ) and accepting more distortion.

#### 8. Field Effect Transistor

## 8.12 MOSFETS

Metal Oxide Semiconductor, Field Effect Transistor. A **MOSFET** is similar to a **JFET** but has the gate insulated from the channel.



When gate is made +ve, the field repels the holes in the p-type material, leaving behind what is essentially n-type silicon, which permits charge carriers to move from source to drain (conventional current from drain to source).

Or, attracts electrons from n-type to fill holes in p-type (similar to BJT). When all holes are filled, conducting channel is formed.

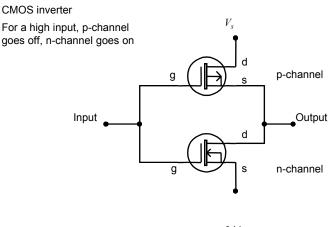
When  $V_{gs} = 0$ ,  $I_d = 0$ . MOSFET is normally OFF when  $V_{gs} = 0$  (unlike JFET). The drain current depends on gate voltage. Like JFET, drain current increases when the gate voltage is made more positive.

Very high input impedance,  $10^{11}\Omega$ .

# 8.13 CMOS

Complementary Metal Oxide Semiconductor

A CMOS chip contains both p- and n-channel MOSFETs on the same chip.



0 V

Characteristics of CMOS digital circuits:

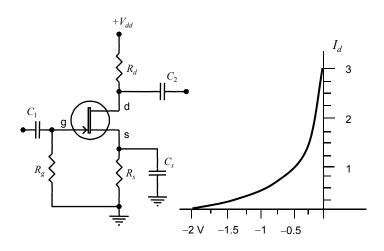
- very compact, allowing high packing density on a single chip
- low power consumption
- accept large range of power supply voltages (+3 to +15 V)
- slow speed compared to TTL

CMOS chips are used in computer circuitry because they only consume power when they change state. When they are in a particular state, no current flows and no power is consumed. This makes them ideal for portable electronic equipment.

Very high input impedance means very little current draw from inputs.

# 8.14 Review Questions

- 1. Explain, with the aid of a diagram, as briefly as possible, the principle of operation of a JFET. In your explanation, describe the effect of various applied voltages across p-n junctions and how transistor action is obtained.
- 2. In the circuit below,  $V_{ds}$  is measured by a student at 29 V. Calculate the DC bias conditions ( $V_{gs}$ ,  $I_d$ ) given that  $V_{dd} = 40$  V,  $R_s = 300 \Omega$ ,  $R_g = 2 M\Omega$ , and  $R_D = 6 k\Omega$ . Also calculate the AC voltage gain and the peak-to-peak output voltage when  $\Delta V_{in} = 30$  mV.

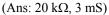


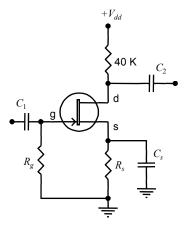
(Ans:  $I_d = 1.74 \text{ mA}, V_{gs} = -0.5 \text{ V}, g_m = 3.48 \text{ mS}, A_v = 20.9, \Delta V_{out} = 624 \text{ mV}$ )

3. An FET has an input resistance of 1000 M $\Omega$  and a transconductance of 4 mS. The drain conductance is 100  $\mu$ S at the operating point where  $V_{ds} = 14 \text{ V}$ ,  $I_d = 2 \text{ mA}$ ,  $V_{gs} = -2 \text{ V}$ . Draw a circuit for a single stage amplifier and determine the values of as many components as possible if a 30 V supply is available. Compare the voltage gain with and without the drain conductance being taken into consideration.

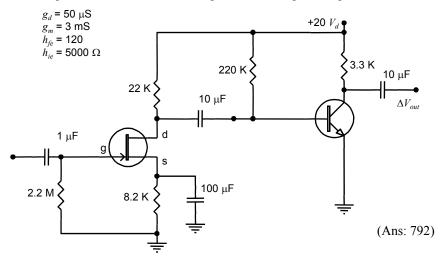
(Ans: 
$$R_d = 7 \text{ k}\Omega$$
,  $R_s = 1 \text{ k}\Omega$ ,  $A_v = 28$ ,  $A_v = 16.5$ )

4. An FET is used in an amplifier circuit with a load resistor of  $R_d = 40 \text{ k}\Omega$ . The gain is measured at 40. Calculate the output resistance and the transconductance of the transistor if the gain drops to 30 when the load resistance is halved.

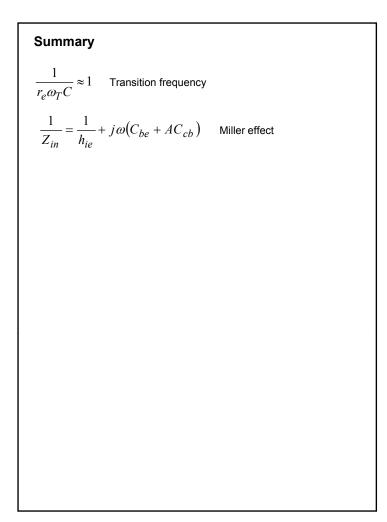




 An FET amplifier is used as the first stage of a two stage amplifier as shown below. The second stage is a simple-biased common emitter amplifier. Calculate the overall gain of the complete amplifier circuit.

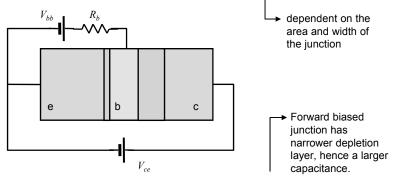


# 9. High Frequency



## 9.1 BJT Capacitance

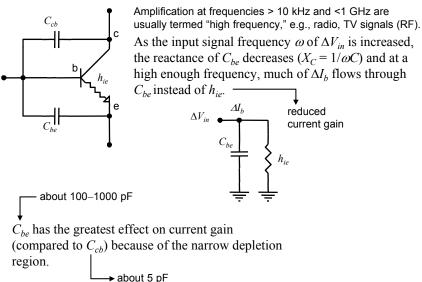
In a transistor, the reverse biased c-b junction behaves like a capacitor since the depletion region is an insulator. The capacitance is given as  $C_{cb}$ .



The forward biased b-e junction also possesses capacitance  $C_{be}$ .

- some of this capacitance is due to the presence of the depletion region
- some of this capacitance is due to the finite speed of diffusion of charge carriers across the junction and is significant when the input signal changes rapidly.

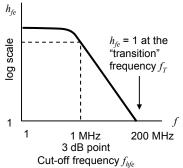
Both these capacitances restrict the **high frequency** response of the transistor. An equivalent circuit for a transistor is thus:



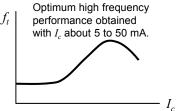
### 9.2 Transition Frequency

At high frequencies, the base current  $I_b$  is diverted more and more into  $C_{be}$  (since  $X_c$  decreases) and the effective current gain of the transistor is reduced.

The **transition frequency** marks the point where the transistor cannot be used as an amplifier. It depends upon the collector current since the input resistance  $h_{ie}$  is a function of the collector current.

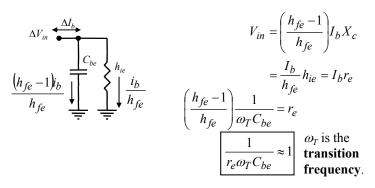


Thus, an increase in  $I_c$  results in a decrease in  $h_{ie}$  and since  $C_{be}$  is in parallel with  $h_{ie}$ , there is an increase in the transition frequency. At higher collector currents, the capacitance  $C_{be}$  begins to rise and dominate any effect of decreasing  $h_{ie}$ , causing transition frequency to — fall with increasing  $I_c$ .

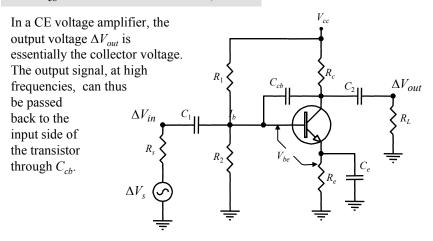


 $C_{be}$  rises due to a change in the apparent size of the base region as the depletion layer is shifted off-centre towards the emitter. This affects the time taken for charge carriers to pass through the base, which at high frequencies, is an effective capacitance.

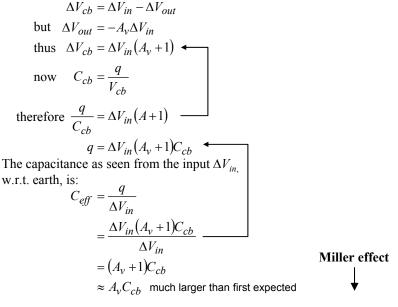
Let  $h_{fe}$  be the current gain of the transistor without any frequency effects. As the frequency gets higher, the overall current gain approaches 1, meaning that the current through the base which actually gets amplified is reduced to  $\Delta I_b/h_{fe}$ . The remainder of  $\Delta I_b$  goes through  $C_{be}$ .



## 9.3 C<sub>ch</sub> Common Emitter Amplifier



What is the value of  $C_{cb}$  as viewed purely from the amplifier input  $\Delta V_{in}$ ?

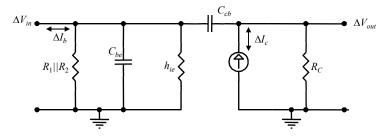


From the point of view of  $\Delta V_{in}$ , the capacitance  $C_{cb}$  actually appears to be much larger due to a feedback effect from the output side of the circuit. This is the most significant barrier to high frequency voltage amplification.

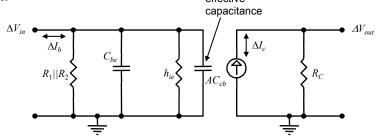
#### 9. High Frequency

# 9.4 Miller Effect

Consider this equivalent circuit of a CE amplifier:



Equivalent circuit can be shown with  $C_{cb}$  replaced by effective capacitance  $AC_{cb}$ : effective



The internal capacitances  $C_{be}$  and  $AC_{cb}$  serve to decrease the input impedance of the amplifier circuit. The total input impedance becomes frequency dependent and is given by:

$$\frac{1}{Z_{in}} = \frac{1}{h_{ie}} + j\omega (C_{be} + AC_{cb})$$
(neglecting  $R_1 ||R_2$ )

Thus, at high frequencies, the measured voltage gain of a CE amplifier circuit will decrease as the input impedance of the circuit becomes smaller in comparison to the output impedance of the source (i.e., less of  $\Delta V_{in}$  appears across the input to the amplifier and more across the internal resistance of the source).

What affects the value of  $C_{cb}$ ?

depends on charge carrier mobility

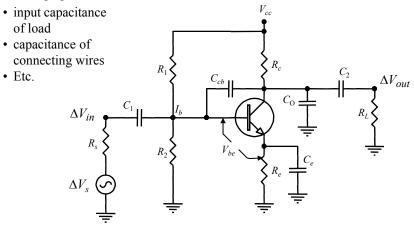
• the dimensions of the depletion layer

• the speed of diffusion of charge carriers across the junction

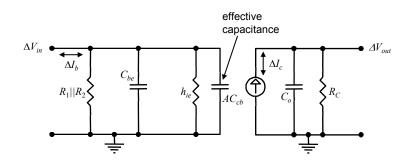
How can these effects be minimised?

## 9.5 Output Capacitance

At high frequencies, capacitances of various items connected to the output serve to short the output signal to earth, thus causing an apparent decrease in voltage gain:



If the frequency of the signal to be amplified is increased, and  $\Delta V_{out}$  decreases without any decrease in  $\Delta V_{in}$ , then the chances are that a **stray capacitance**  $C_o$  is shunting the signal to earth instead of into the desired output device. - such as would happen if  $C_{be}$  and  $AC_{cb}$  were significant.



#### 9. High Frequency

### 9.6 Amplification at High Frequencies

One example of a circuit with BJT transistor for high frequency applications is the **common base** amplifier circuit.

 $C_1$ 

 $\Delta V_{in}$ 

 $R_1$ 

 $R_2$ 

 $C_{be}$ 

R

How does it work?

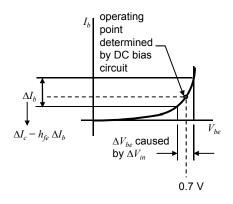
Input signal feeds into the resistance of the baseemitter junction as seen from the emitter, i.e.,  $r_e$  which is low.

$$r_e = \frac{25}{I_e} \rightarrow \text{DC emitter current}$$
  
in mA and  $I_c = I_e$ 

Thus, the circuit has a low input resistance (not desirable). However, the input signal only sees capacitance  $C_{be}$  and not  $A_v C_{cb}$ ; thus the Miller effect does not affect  $\Delta V_{in}$ .

This amplifier works somewhat backwards in that the input signal causes  $\Delta V_{be}$  to oscillate from the emitter side rather than from the base side but here, when the signal  $\Delta V_{in}$  increases,  $I_b$  decreases and so does  $I_c$  and thus  $\Delta V_{out}$  goes up – input and output are in phase.

- Voltage gain: same as CE amplifier
- Low input impedance (not so good but...)
- useful for preamplifier for television signals from coaxial cable (low impedance source 70 Ω)
- Miller effect on gain is reduced very desirable
- Useful high frequency response only limited by transition frequency  $f_T$



 $V_{cc}$ 

 $C_2$ 

•  $\Delta V_{out}$ 

## 9.7 Review Questions

1. The transition frequency for a certain transistor is specified at 320 MHz at  $I_c = 12$  mA. Determine the capacitance of the base-emitter junction.

(Ans: 239 pF)

2. Calculate the effective capacitance on the input of an amplifier  $A_v = 120$  which uses a transistor with  $C_{cb} = 6$  pF.

(Ans: 726 pF)

- 3. What capacitance has the most effect on the gain of:(a) a BJT transistor;(b) a common emitter amplifier.
- 4. An amplifier circuit has the following parameters. Calculate the input impedance  $Z_{in}$  at  $\omega = 200$  MHz,  $h_{ie} = 500 \Omega$ ,  $C_{be} = 150$  pF,  $C_{cb} = 5$  pF,  $A_{v} = 200$ . (Ans: 0.59  $\Omega$ )

154

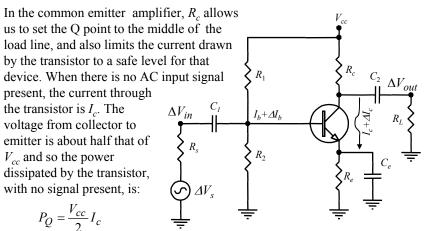
# 10. Power Amplifiers

Summary	
$P_Q = \frac{V_{cc}}{2} I_c$	Quiescent power consumption of transistor in common emitter amplifier
$P_{av} = \frac{V_{rms}^2}{R_L} = \frac{\Delta V^2}{8R_L}$	Average rms output power at load for common emitter and common collector amplifier
$P_S = \frac{2{V_{cc}}^2}{\pi R_L}$	Average power from supply for simple Class B amplifier
$A_v = \frac{R_L}{r_e + R_L}$	Voltage gain for simple Class B amplifier

## 10.1 Amplifier Power Output

The common emitter, common collector and common source amplifiers are suitable for **small signal amplification** and are generally constructed from lower power transistors.

Consider a **common emitter amplifier**. The output impedance is the parallel combination of  $R_c$  and  $R_L$ . The DC bias current  $I_c$  is typically a couple of mA. That is, the available current swing at the output is typically  $\pm 1$  mA or so.



As far as power dissipation within the transistor itself is concerned, it is the DC quiescent bias condition that represents the worst case, and so must be designed to handle that level of power output  $P_{Q}$ .

When there is an AC signal present, the current swings by  $\Delta I_c$  (peak-to-peak) and the power is transferred from the transistor to the output resistance  $(R_c||R_L)$ . It is only the power dissipated within the load resistor  $R_L$  that is important (since this is our "payload"). Thus, the net **average output power** in  $R_L$  is:  $V_{rmc}^2 (V_R)^2 = 1 (\Delta V)^2 = 1 \Delta V^2$ 

$$P_{av} = \frac{V_{rms}^2}{R_L} = \left(\frac{V_p}{\sqrt{2}}\right)^2 \frac{1}{R_L} = \left(\frac{\Delta V}{2\sqrt{2}}\right)^2 \frac{1}{R_L} = \frac{\Delta V^2}{8R_L} \xrightarrow{\text{peak-to-peak}} \text{peak}$$

The power supplied by the supply voltage is  $V_{cc}$  times the current draw through the bias divider resistors  $R_1$  and  $R_2$ , plus the collector current  $I_C$ . This DC power,  $P_{DC}$ , can be calculated once the DC bias voltage  $I_c$  is determined from the bias conditions.

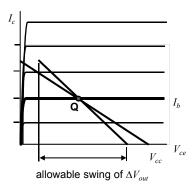
The ratio  $P_{av}/P_{DC}$  is the overall **efficiency** of the amplifier, and for a common emitter amplifier, is usually only a few percent, with a theoretical maximum of about 25%.

# 10.2 Class A Amplifier

In many applications, particularly in the first stages of amplification of a signal, low power circuits with high gain and good linearity are required. In the circuits examined so far, the bias currents are in the mA regime and would be unsuitable for driving loads such as audio **loudspeakers**, where outputs of 100 W or more may be required.

A common emitter amplifier, and all those that set the Q point in the middle of the load line, are termed Class A amplifiers.

Class A amplifiers generally produce a faithful representation of the input signal (highly linear, low distortion) with a reasonably large voltage gain and reasonable impedance matching for many applications.



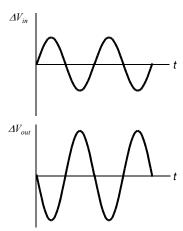
The main disadvantage is that Class A amplifiers dissipate most of their power

within the transistor when there is no signal present. This power dissipation occurs via heating of the component. Should the p-n junctions within the transistor become too hot (say 100 to 200 °C) the device may no longer function.

In principle, it is perfectly acceptable to scale up the common emitter circuits with lower value resistors and larger transistor construction so that the

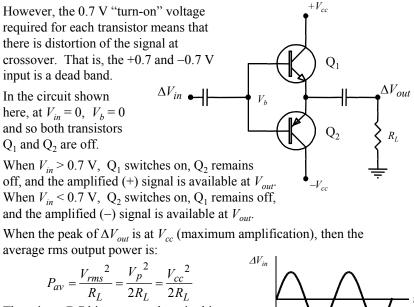
required output for a high power application may be obtained. This is seldom done due to the very poor **efficiency** of such a circuit.

To overcome these limitations, amplifiers for high power applications are usually made so that they consume little or no DC bias current.



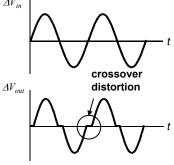
## 10.3 Class B Amplifier

A **Class B amplifier** uses two complementary transistors (one NPN and one PNP) that act in a **push-pull** capacity. Each transistor supplies half of the output waveform. At zero input voltage, there is no bias current drawn by the transistors, thus leading to greater efficiency.



There is no DC bias current draw in this circuit. The potential at  $+V_{cc}$  and  $-V_{cc}$  is constant but the current draw  $\Delta I_C$  varies according to the AC input  $\Delta V_{in}$ . Taking into account both supplies, the average power consumption from the source is given by:

$$P_S = \frac{2V_{cc}^2}{\pi R_L}$$



The ratio of  $P_{av}$  and  $P_s$  thus predicts a maximum efficiency of  $\pi/4 \approx 80\%$ . As with any common collector (or emitter follower) circuit, the **voltage** gain is less than 1 and in the circuit shown here is given by:

$$A_{\nu} = \frac{\Delta V_{out}}{\Delta V_{in}} = \frac{\Delta I_c R_L}{\Delta I_b \left(h_{ie} + h_{fe} R_L\right)} = \frac{R_L}{r_e + R_L}$$

Thus, a Class B circuit is a *power* amplifier, not a voltage amplifier.

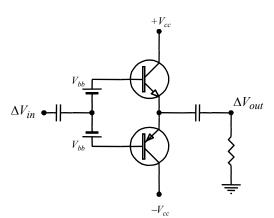
## 10.4 Class AB Amplifier

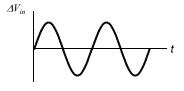
The crossover distortion of a Class B amplifier can be overcome by the biasing the two transistors into the on condition by a small amount so that there is a period during which both transistors are on near the crossover.

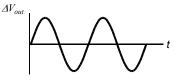
In the circuit shown here, a small bias voltage  $V_{bb}$  is applied across the base of each transistor. This results in a bias current  $I_c$  in each transistor from  $+V_{cc}$  to  $-V_{cc}$ , that is, there is a DC current flow in the collector-emitter circuit leg.

For small variations in  $\Delta V_{in}$ , there is a region where both transistors respond to the signal. For large variations, one transistor eventually turns off and the other one provides all the current gain.

Thus, for small input signals, the amplifier operates in Class A mode, while for larger signals, it operates as a Class B. Crossover distortion is very greatly reduced. The amplifier is referred to as being **Class AB**.





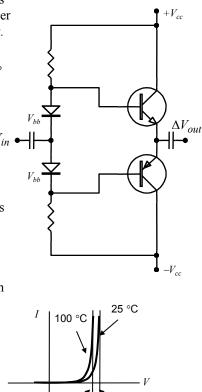


## 10.5 Class AB Diode Biasing

In practice, biasing for a Class AB amplifier is not provided by separate power supplies, or even from a resistor network, but instead, via diodes from the supply. Here, there is a forward bias voltage drop ( $\approx 0.7$  V) across the diodes and thus applied to the base-emitter junction. This is usually sufficient to provide a small bias current.

There is an important reason why diodes are used to provide the bias voltage rather than just using a resistor voltage divider. The base-emitter junction in each of the transistors is in forward bias. Usually,  $I_h$ is controlled by the bias resistors (since the voltage drop across them is large in comparison to  $V_{he}$ ). Large changes in  $I_h$ result in only small changes  $\Delta V_{in} \bullet$ in  $V_{be}$  due to the steepness of the diode characteristic curve. If the temperature of the transistor should increase, then  $V_{he}$  (the **knee voltage**) would decrease. The voltage drop across the bias resistors, thus  $R_b$  increases, and so the current  $I_b$  increases, and hence  $I_c$ would increase - thus raising the temperature of the junction more. A positive feedback condition exists which could eventually lead to thermal runaway.

In **diode biasing**, the forward junction of the diode is kept at or near the temperature of the transistor by placing it very close to it. As the temperature of the transistor rises, so does that of the diode, and the voltage across the p-n junction of the diode thus decreases – thus siphoning off some of the current going to the transistor base  $I_b$  and so stabilising the collector current  $I_c$  in the transistor.



Note: The diode equation would predict an increase in  $V_{be}$  with increasing temperature for a constant value of  $I_o$ , but  $I_o$  is a strong function of temperature (doubling with every 5 to 10 °C rise) and forces the characteristic curve to move to the left with increasing *T*.

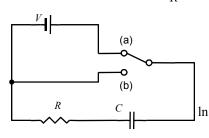
0.69 V 0.7 V

# 11. Transients

Summary	
	≻ R-C circuit: charging
$v_c = V e^{\frac{-t}{RC}}$ $v_R = -V e^{\frac{-t}{RC}}$	≻ R-C circuit: discharging
$v_R = V \left( 1 - e^{\frac{-Rt}{L}} \right)$ $v_L = V e^{\frac{-Rt}{L}}$	≻ R-L circuit: charging
$v_{R} = Ve^{\frac{-Rt}{L}}$ $v_{L} = -Ve^{\frac{-Rt}{L}}$	
$v_{out} = \frac{1}{RC} \int v_{in} dt$	Integrator
$v_{out} = RC \frac{dv_{in}}{dt}$	Differentiator

#### 11.1 R-C Circuit Analysis

Consider a series circuit containing a resistor R and capacitor C. If connection (a) is made, the initial potential difference across the capacitor is zero, and the entire battery voltage appears across the resistor. At this instant, the current in the circuit is: V



As the capacitor charges, the voltage across it increases and the voltage across the resistor correspondingly decreases (and so does the current in the circuit). After some time, the capacitor is fully charged and the entire battery voltage appears across the capacitor. The current thus drops to zero and there is no potential drop across the resistor (since there is no current).

When connection (b) is made, the capacitor discharges through the resistor. The current is initially high and then over time drops to zero.

$$v_{R} = iR; v_{C} = \frac{q}{C}$$

$$V = v_{R} + v_{C}$$

$$signify$$
instantaneous
values.
$$i = \frac{V}{R} - \frac{q}{RC}$$
but
$$i = \frac{dq}{dt}$$

$$\frac{dq}{dt} = \frac{V}{R} - \frac{q}{RC}$$
but
$$i = \frac{dq}{dt}$$

$$\frac{dq}{dt} = \frac{V}{R} - \frac{q}{RC}$$

$$\frac{dq}{dt} = \frac{dt}{RC}$$

$$\frac{dq}{RC} = \frac{dt}{RC}$$
1st order differential
equation - integrate
both sides.
$$-\ln(VC - q) = \frac{t}{RC} + \text{constant}$$
When  $t = 0$ ,
$$-\ln(VC - q) = \frac{t}{RC} - \ln VC$$

$$q = 0.$$

$$-\ln(VC - q) = \frac{t}{RC} - \ln VC$$

$$q = 0.$$

$$\ln(VC - q) - \ln VC = \frac{-t}{RC}$$

$$\ln \frac{VC - q}{VC} = \frac{-t}{RC}$$

$$\ln \frac{VC - q}{VC} = \frac{-t}{RC}$$

$$\ln \frac{VC - q}{VC} = \frac{-t}{RC}$$

$$\int \frac{q}{VC} = \frac{Q\left(1 - e^{\frac{-t}{RC}}\right)}{\frac{dq}{VC}}$$

$$q = VC\left(1 - e^{\frac{-t}{RC}}\right)$$

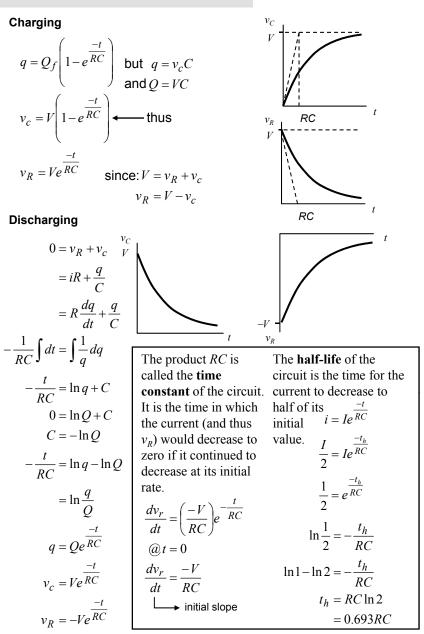
$$\int \frac{dq}{dt} = \frac{V}{R} e^{\frac{-t}{RC}}$$
Both current in
$$\frac{dq}{dt} = \frac{V}{R} e^{\frac{-t}{RC}}$$

$$I_{0} \text{ is the initial current in the circuit.}$$

$$\int \frac{q}{VC} = \frac{e^{\frac{-t}{RC}}}{VC}$$

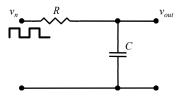
#### 11. Transients

#### 11.2 Time Constant and Half-Life

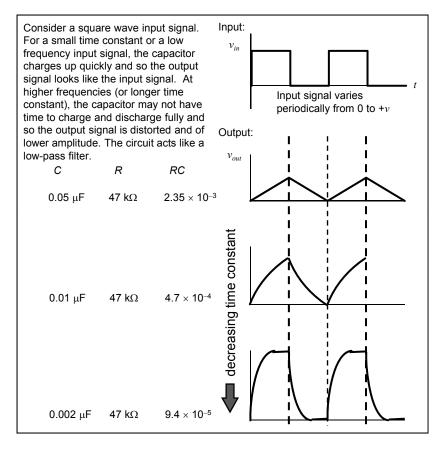


#### 11.3 R-C Low-Pass Filter

As the capacitor charges, the voltage across it  $(v_{out})$  increases. When the capacitor is fully charged, all of  $v_{in}$  appears across it and none across the resistor. As the time constant becomes smaller than the period *T* of the input pulse, the capacitor has more time to charge and discharge fully before the pulse changes polarity.

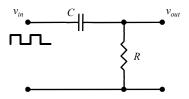


For a **low-pass filter**, we want *RC* << *T* to pass through low frequencies, i.e., small time constant.

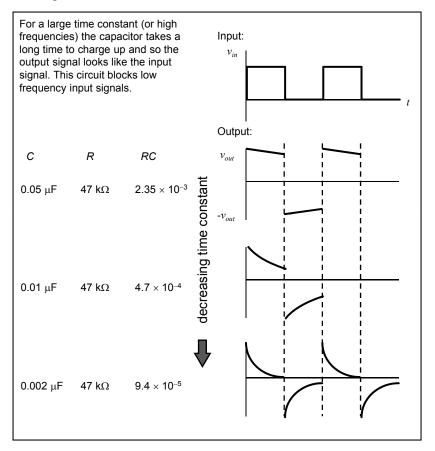


### 11.4 R-C High-Pass Filter

As the capacitor charges, the voltage across it increases and voltage across the resistor decreases. As the time constant becomes smaller than the period T of the input pulse, the capacitor has time to charge and discharge fully and the voltage across the resistor decreases to zero.



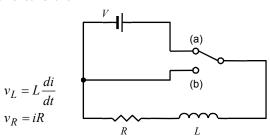
For a **high-pass filter**, we want RC >> T to pass through high frequencies, i.e., large time constant.



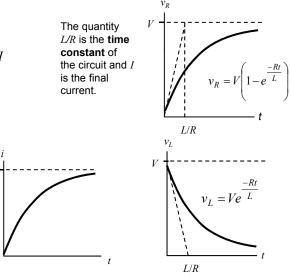
### 11.5 R-L Circuits

Charging  $V = v_R + v_I$  $V = iR + L\frac{di}{dt}$ = IR $\frac{IR}{I} = i\frac{R}{I} + \frac{di}{dt}$  $\frac{di}{dt} = \frac{IR}{I} - i\frac{R}{I}$  $=(I-i)\frac{R}{I}$  $\frac{di}{I_{i}} = \frac{R}{I} dt$  $\int \frac{R}{L} dt = \int \frac{1}{L - i} di$  $\frac{R}{I}t = -\ln(I-i) + C$ i = 0 (*a*) t = 0 $C = \ln I$  $\frac{R}{I}t = -\ln(I-i) + \ln I$  $-\frac{R}{I}t = \ln(I-i) - \ln I$  $=\ln\frac{(I-i)}{I}$  $\frac{(I-i)}{L} = e^{\frac{-Rt}{L}}$  $i = I\left(1 - e^{\frac{-Rt}{L}}\right)$ 

Note: as written here, we write +Ldi/dt to signify a voltage drop across the inductor in the direction of current flow.



Let connection (a) be made. Because of the selfinduced emf, the current (and hence  $v_R$ ) in the circuit does not rise to its final value at the instant the circuit is closed, but grows at a rate which depends on the **inductance** (henrys) and resistance (ohms) of the circuit.



### 11.6 R-L Circuits

#### Discharging

$$0 - v_L = v_R$$
  

$$0 = iR + L\frac{di}{dt}$$
  

$$-\frac{R}{L}dt = \frac{1}{i}di$$
  

$$-\frac{R}{L}\int dt = \int \frac{1}{i}di$$
  

$$v_L = L\frac{di}{dt}$$
  

$$-\frac{Rt}{L} = \ln i + C$$
  

$$v_R = iR$$
  

$$C = -\ln I$$
  

$$i = I @ t = 0$$
  

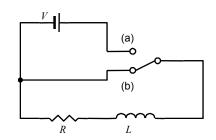
$$-\frac{Rt}{L} = \ln i - \ln I = \ln \frac{i}{I}$$
  

$$i = Ie^{\frac{-Rt}{L}}$$
  

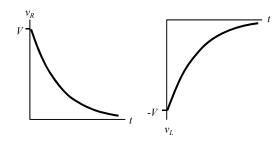
$$v_R = Ve^{\frac{-Rt}{L}}$$
  

$$v_L = -Ve^{\frac{-Rt}{L}}$$
  

$$v_L = -Ve^{\frac{-Rt}{L}}$$



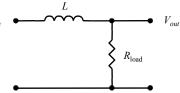
When connection (b) is made, the current (and  $v_R$ ) does not fall to zero immediately but falls at a rate which depends on *L* and *R*. The energy required to maintain the current during the decay is provided by the energy stored in the magnetic field of the conductor



### 11.7 R-L Filter Circuits

#### Low-pass (choke) circuit



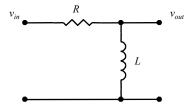


If the source voltage rises above its average value, then any increase in the current is opposed by inductor and energy is stored in the magnetic field of the inductor.

If the source voltage falls below its average value, then stored energy is released from the inductor to oppose any decrease in current. Result is that current through load resistor is maintained at near constant level. High frequencies are filtered out.

#### **High-pass filter**

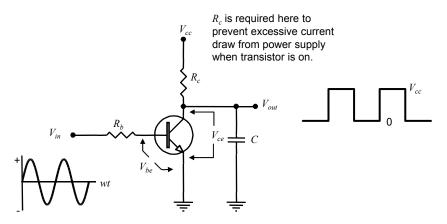
Low frequencies are shunted to ground by the inductor; high frequencies are passed through to  $v_{out}$ .



#### 11. Transients

### 11.8 Transistor Circuits

Transistor switch - this circuit will "square up" any repetitive waveform



Now, consider the effect of a capacitance on the output:

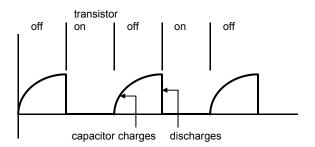
If the transistor is initially off, then  $V_{out} = V_{cc}$  and the capacitor will be charged also to  $V_{cc}$ .

But this charging takes place through  $R_c$ , i.e., time constant =  $R_cC$ , and the rate of rise of  $V_{out}$  is relatively long.

When the transistor is turned on, the  $V_{out}$  drops low and the capacitor discharges through  $V_{ce}$  to earth.

Since this connection through to earth is virtually a short circuit, through the transistor from collector to emitter, then discharge time is very short.

Resulting output:



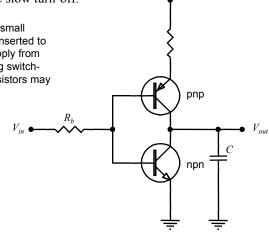
In active switching circuits, "turn-on" is faster than "turn-off."

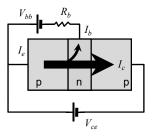
+ V

### 11.9 Active Pull-Up

Technique to overcome slow turn-off.

In an actual circuit, a small resistor  $R_c$  is usually inserted to protect the power supply from short to ground during switch-over, when both transistors may be momentarily "on".





Direction of hole current is shown.

Zero or negative input voltage:

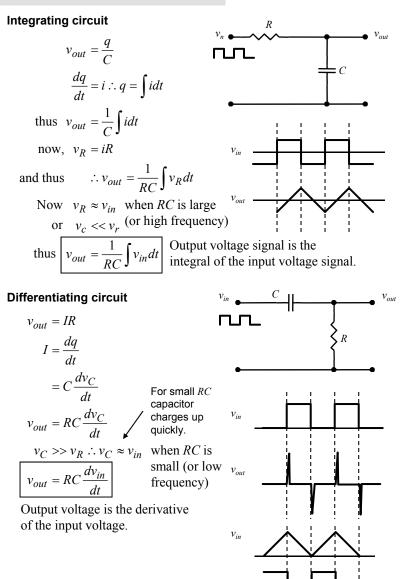
Positive input voltage:

- npn transistor base-emitter junction in forward bias so transistor turns on. Capacitor can discharge to earth through collector-emitter as before.
- pnp transistor base-emitter junction in reverse bias so transistor turns off and emitter-collector becomes non-conducting.  $V_{cc}$  is thus not shorted to earth through npn transistor. Capacitor voltage is now  $V_{ce}$  for npn since pnp is off.
- pnp transistor is turned on and  $V_{cc}$  appears across capacitor and also at  $V_{out}$ . But, charging time is very short since resistance  $R_c$  may be eliminated in this circuit.

The same effect can be obtained with two npn transistors if the bases of each are driven separately and out of phase so that one switches on when the other switches off.  $\longrightarrow$  IC logic circuits usually employ this

method since they are more easily fabricated on one semi-conductor chip.

### 11.10 Integrator/Differentiator

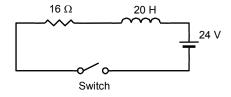


 $v_{out}$ 

### 11.11 Review Questions

- 1. A circuit containing an inductor 20 H with a resistance or  $16 \Omega$  is connected through a switch to a 24 V source. Calculate the following:
  - (a) the initial current when the switch is closed;
  - (b) the final steady-state current;
  - (c) the initial rate of change of current when the switch is closed;
  - (d) the time constant for this circuit.

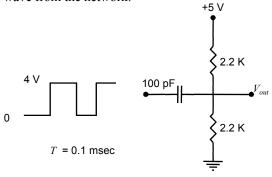
(Ans: 0, 1.5 A, 1.2 A s<sup>-1</sup>, 1.25 s)



2. A capacitor of 1  $\mu$ F is charged through a 50 k $\Omega$  resistor. Calculate how long it will take the capacitor to charge to 63% of the applied voltage.

(Ans: 0.05 s)

- 3. Design an RC filter to give at least 3 dB attenuation for all frequencies above 10 kHz.
- 4. A square wave of frequency 100 kHz is applied to the following network. If the square wave amplitude is 4 V, determine the output wave from the network.

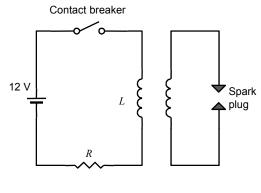


#### 11. Transients

5. A conventional ignition system in a motor vehicle consists of an induction coil, the current to which is periodically switched on and off through mechanical "contact breaker points." A high voltage is induced in the secondary side of the coil when the contact breaker opens and closes.

If the resistance of the primary side of the circuit is 8  $\Omega$  and the inductance of the coil is 2.4 H, calculate the following quantities:

- (a) the initial current when the contact breaker is just closed;
- (b) the initial <u>rate of change</u> of current when the contact breaker is just closed;
- (c) the final steady-state current;
- (d) the time taken for the current to reach 95% of its maximum value.



Primary

Secondary

(Ans: 0, 5 A s<sup>-1</sup>, 1.5 A, 0.9 s)

6. A 10,000  $\Omega$  resistor and a capacitor are connected in series and a 10 V potential is then applied. If the potential across the capacitor rises to 5.0 V in 1.0  $\mu$ s, find (a) the capacitance of the capacitor and (b) the time taken to charge the capacitor to 95% of maximum charge.

(Ans: 144 pF, 4.2 µs)

7. A 10,000  $\Omega$  resistor and an inductor are connected in series and a 10 V potential is then applied across them. If the potential across the inductor is 5.0 V after 1.0  $\mu$ s, find (a) the inductance of the inductor and (b) the time taken for the current in the circuit to reach 95% of its steady-state maximum value.

(Ans: 14.4 mH, 4.2  $\mu$ s)

#### Summary

Boolean algebra A + B = B + A $B \bullet A = A \bullet B$ (A + B) + C = A + (B + C) $(A \bullet B) \bullet C = A \bullet (B \bullet C)$  $A + AB = A \bullet (1 + B) = A$  $A \bullet (A + B) = A$  $A \bullet (B + C) = A \bullet B + A \bullet C$  $A + (B \bullet C) = (A + B) \bullet (A + C)$ A + A = A $A \bullet A = A$  $A \bullet \overline{A} = 0$ <u>A</u> + A = 1  $\overline{A} = A$ 0 + A = A $1 \bullet A = A$ 1 + A = 1 $0 \bullet A = 0$  $A + \overline{A} \bullet B = A + B$  $A \bullet (\overline{A} + B) = A \bullet B$ De Morgan's theorem  $(A + B) = \overline{A \bullet B}$  $\overline{(A \bullet B)} = \overline{A} + \overline{B}$ 

### 12.1 Digital Logic

Digital electronic circuits contain components which act like high speed switches that process voltage levels that are suitable for representing the binary numbers 0 and 1. These voltage levels may also represent **logic states** true and false and thus allow binary data to be processed using **Boolean algebra** in a digital circuit. The components of a digital circuit are called **logic gates**. Truth tables provide the rules for the

Boolean operators.

A AND B A•B

Output true

are true

only if both A and B

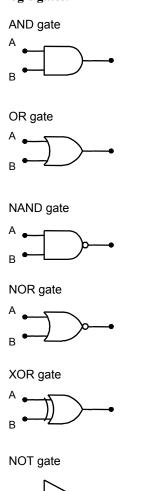
A B

0

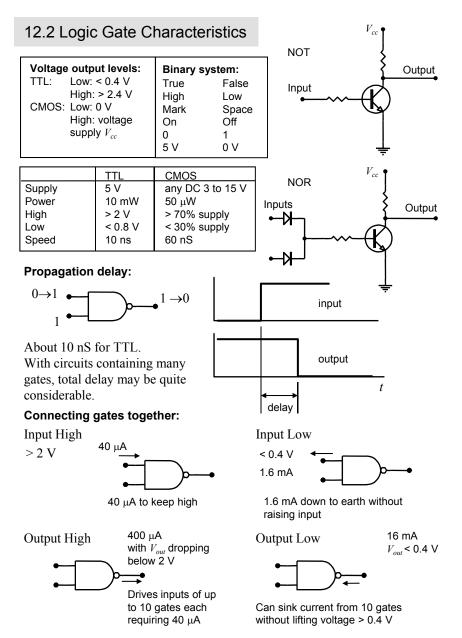
0 1 0

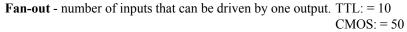
1 0 0

0 0



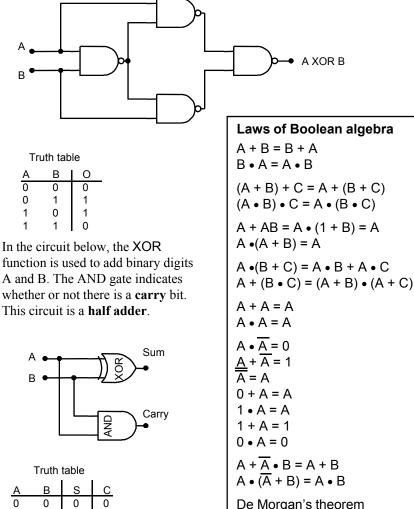
1 1 1 AND A A OR B A+B В Output true 0 0 0 0 if either A or B are 1 1 1 0 1 true 1 1 1 OR А В A NAND B 0 Output false if 0 1 both A and B are 0 1 1 1 true 1 0 1 1 0 NAND A NOR B A В Output false if either 0 0 1 0 1 0 A or B is true 1 0 0 1 1 0 NOR A XOR B А В True if either A or B 0 0 0 0 1 1 is true but not both 1 0 1 together 1 1 0 XOR NOT A A True if A is false 0 1 False if A is true 1 0 NOT





### 12.3 Digital Logic Circuits

Boolean algebra can be implemented using digital electronic circuits using combinations of logic gates, e.g., a combination of NAND gates gives a logical XOR function:



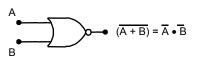
De Morgan's theore
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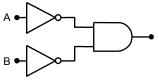
### 12.4 Boolean Logic Examples

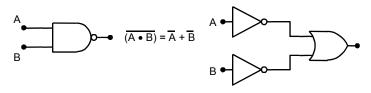
1. Associative law (A + B) + C = A + (B + C)



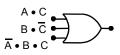
2. De Morgan's theorem



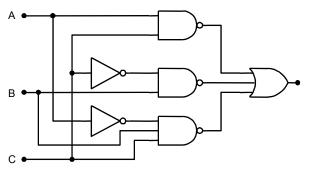




- 3. Example Out =  $A \cdot C + B \cdot \overline{C} + \overline{A} \cdot B \cdot C$   $\downarrow$  OR  $\downarrow$   $\rightarrow$  AND
  - 1. Work on the OR's first

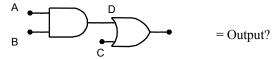


2. Add on AND's



### 12.5 Logic Circuit Analysis

Consider now a more systematic approach to formulating logic circuits.



1. Draw up truth table

Α	В	С	D = AB	Out = D+C	Min terms	2. AND inputs
0	0	0	0	0	$\overline{A} \cdot \overline{B} \cdot \overline{C}$	together with 0's
0	0	1	0	1	$\overline{A} \cdot \overline{B} \cdot C$	negated - min terms
0	1	0	0	0	$\widetilde{\overline{A} \cdot B \cdot \overline{C}}$	3. Circle min
0	1	1	0	1	$\overline{A} \cdot B \cdot C$	terms
1	0	0	0	0	$A \cdot \overline{B} \cdot \overline{C}$	showing a 1
1	0	1	0	1	$\overline{\mathbf{A} \cdot \overline{\mathbf{B}} \cdot \mathbf{C}}$	-
1	1	0	1	1	$\overrightarrow{A \cdot B \cdot C}$	
1	1	1	1	1	$(A \cdot B \cdot C)$	

4. OR circled min terms to form Boolean expression

 $Out = \overline{A} \bullet \overline{B} \bullet C + \overline{A} \bullet B \bullet C + A \bullet \overline{B} \bullet C + A \bullet B \bullet \overline{C} + A \bullet B \bullet C$  $= \overline{A} \bullet C \bullet (\overline{B} + B) + A \bullet B \bullet \overline{C} + A \bullet C \bullet (\overline{B} + B)$ but  $\overline{A} \bullet C \bullet (\overline{B} + B) = \overline{A} \bullet C$  and  $A \bullet C \bullet (\overline{B} + B) = A \bullet C$ thus,  $\overline{A} \bullet C + A \bullet C = C \bullet (\overline{A} + A)$ = Ctherefore Out  $= C + A \bullet B \bullet \overline{C}$ but  $X + \overline{X} \bullet Y = X + Y$ thus :  $Out = A \bullet B + \overline{C}$  = Simplified expression

### 12.6 Karnaugh Map

The Karnaugh map is a graphical method of analysing logic circuits.

1. Draw up truth table and circle min terms (using previous example)

А	В	С	Out = D+C	Min terms
0	0	0	0	$\overline{A} \cdot \overline{B} \cdot \overline{C}$
0	0	1	1 (	$\overline{A \cdot B \cdot C}$
0	1	0	0	$\overbrace{\overline{A} \cdot B \cdot \overline{C}}$
0	1	1	1 (	$\overline{A} \cdot B \cdot C$
1	0	0	0	$A \cdot \overline{B} \cdot \overline{C}$
1	0	1	1	$\overline{\mathbf{A} \cdot \mathbf{B}} \cdot \mathbf{C}$
1	1	0	1	$A \cdot B \cdot C$
1	1	1	1	$\overline{\mathbf{A} \cdot \mathbf{B} \cdot \mathbf{C}}$

2. Construct map as follows:

 (a) arrange rows and columns with every combination of input, changing only one variable at a time;

	С	$\overline{C}$	
AB	1	1	
ĀB	1		
$\overline{A}\overline{B}$	1		
$A\overline{B}$	1		

(b) put 1's in boxes corresponding to circled min terms in truth table;

Right	Wrong
AB	AB
ĀB	$\overline{A}B$
ĀB	$A\overline{B}$
$A\overline{B}$	$\overline{A}\overline{B}$

(c) draw boxes around groups of 1's. Boxes can only go vertically and horizontally. Boxes can also wrap around. Can only box even groups (powers of 2). Boxes of 3, 5 and 6, etc., are not permitted;

This example is a 3 input system

 (d) group contents of boxes by products and join boxes together with sums (Note: these are not yet Boolean AND's and OR's; we are simply following a procedure that will lead to a Boolean expression);

 $Output = ABC \overline{ABC} \overline{ABC} \overline{ABC} + ABC \overline{ABC}$ 

(e) cancel terms of opposite sign (i.e., remove them from the expression);

Output = 
$$ABC \overrightarrow{AB}C \overrightarrow{AB}C \overrightarrow{AB}C + ABC AB\overrightarrow{C}$$
  
= C + AB

 (f) now replace products with "AND" and sums with "OR" to obtain final logical expression.
 Output = C + A • B Consider this 4 input system:

	CD	$\overline{C}D$	$\overline{C}\overline{D}$	$C\overline{D}$
AB		1	1	
ĀB		1	1	
ĀB				
$A\overline{B}$				

Output =  $AB\overline{C}DAB\overline{C}\overline{D}\overline{A}B\overline{C}\overline{D}\overline{A}\overline{B}\overline{C}\overline{D}$ =  $B \bullet \overline{C}$ Groups of 4 eliminate 2 variables. Groups of 8 eliminate 3 variables.

	CD	БĎ	$\overline{C}\overline{D}$	$C\overline{D}$
AB	1	1		
ĀB				
ĀB				
$A\overline{B}$	1	1		

Boxes can wrap around
Output = ABCDAB $\overline{C}$ DA $\overline{B}$ CDA $\overline{B}$ CDA $\overline{B}$ CD = A • D

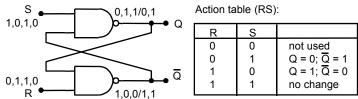
Remember: you can only group 2's, 4's, 8's, etc. Groups can be made from wrap-arounds from top and bottom and sides. You can also group the four corners into one group of four. A "1" on its own cannot be grouped and the associated min term must be + with the other grouped expressions.

#### Don't care states

Sometimes, it doesn't matter if there is a zero or a 1 in a logic circuit. On a Karnaugh map, an "X" is inserted in the position to indicate "don't care." X's may be grouped if desired if this leads to minimisation.

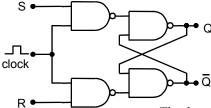
### 12.7 Flip-Flops

**Flip-flops** can be used to represent binary numbers. An RS flip-flop is a digital circuit which is stable in one of two states – **set** or **reset**. Such a circuit can be made using NAND gates. A truth or **action table** summarises the action of flip-flop. The voltage of one of the outputs can be used to represent or store a binary digit since it can be either voltage high (logic 1) or low (logic 0) and will remain at that setting until signals on the input, which only last for a short time, set or reset the outputs.



S and R are normally held at 1 and the outputs remain constant in any one of two states. Either Q = 0; Q = 1, or Q = 1;  $\overline{Q} = 0$ . An input sequence of 101 at S (with R = 1) ensures that Q = 1;  $\overline{Q} = 0$ . An input sequence of 101 at R (with S = 1) ensures that Q = 0;  $\overline{Q} = 1$ . In normal circuit design, the condition S = R = 0 should not be allowed since Q =  $\overline{Q} = 1$  is not very useful. For a flip-flop using NOR gates, the inputs S = R = 1 result in both outputs being at logic 0, again, not a useful condition for a circuit whose main feature is to have the outputs opposite to each other.

Clocked flip-flops are used in computers and are set on receipt of a timing or clock pulse.



Action table (clocked RS):

R	S	
0	0	no change Q = 1;
0	1	Q = 1;
1	0	Q = 0;
1	1	not used

Data at terminal S gets transferred to Q on the clock pulse and remains at Q even if the signal at S disappears and the clock goes low.

The data stays at Q because when the clock pulse goes low, the flip-flop circuits *within the chip* are at S = R = 1 (due to the NAND gates on the clock stage). Only when the clock goes high do the flip-flops react to the logic signals at D on the latch.

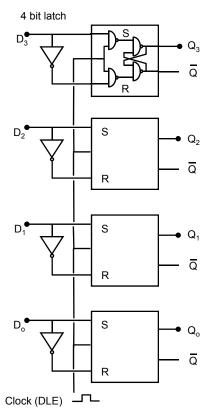
Note: this action table is different from the ordinary NAND flip-flop. Here, R = S = 1 is the "not used" state.

#### 12.8 D-Latch

A **latch** is a device which holds the data that appears on its input terminals. A memory cell in the microcomputer system is a latch. Typically, signals destined for storage in memory cells appear on the data bus momentarily and then disappear. The timing of the signals is regulated by the internal **clock** which runs at speeds typically in the MHz range. The decoding circuitry determines which buffer is to be activated. The activated buffer in turn connects the latch input terminals to the data bus. The signals on the data bus are transferred through buffers to the latch circuit, which stores the signals on its output terminals.

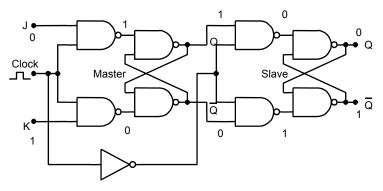
A latch circuit can be implemented using a series of RS **flip-flops**. In this figure, the 4 bit data at  $D_3$  to  $D_0$ is transferred to Q on the clock pulse. When a bit D is logic 1, S = 1 and R = 0 and the output Q becomes 1. When D is logic 0, S = 0and R = 1 and the output D = 0.

An **octal latch** has 8 inputs and 8 outputs. The data latch enable (DLE) pin, when set high, copies the voltage levels on the input pins to the corresponding output. The latch circuitry retains the signals on the output pins even if the input signals disappear and DLE goes low. It is important that DLE is set when data appears on the input. DLE is typically timed to go high when data appears on the data bus. The clock signals are used to synchronise this timing.

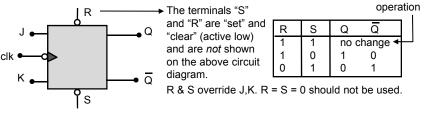


### 12.9 J-K Master-Slave Flip-Flop

Two clocked RS flip-flops in tandem constitute what is called a J-K or "master-slave" flip-flop. The two inputs to the device as a whole are labelled J and K for convenience and to avoid confusion with the terms R and S. The advantage of this arrangement is that the output responds to the state of the input only on the falling of the clock pulse and is not affected by jitter on the input when the clock is high.



When the clock is high, the inputs J and K control the outputs of the master according to the action table for a regular RS flip-flop. The output of the slave is not affected since its clock is low (via the inverter). When the clock pulse goes low, the outputs on the master are isolated from any changes in the input, and the slave flip-flop is now activated and the outputs respond to the output levels of the master.



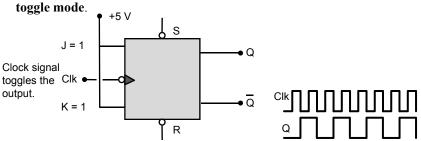
The net effect is for the inputs J and K to be read on the high part of the clock cycle and the output only responds to this input when the clock falls – hence the inversion bubble on clk.

#### Action table:

J	К	Clock pulse 1 to 0
0	0	no change, Q <sub>n+1</sub> =Q <sub>n</sub>
0	1	Q <sub>n+1</sub> = 0 (RESET)
1	0	Q <sub>n+1</sub> = <u>1</u> (SET)
1	1	$Q_{n+1} = \overline{Q}_n$ toggle

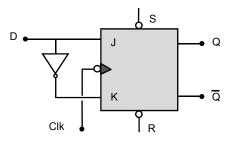
### 12.10 J-K Flip-Flop Examples

1. If the inputs of a J-K flip-flop are held at 1, then the flip-flop is placed in



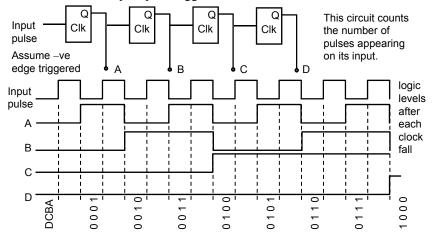
For a square wave input at the clock, the output Q is a square wave but half the frequency. The toggle mode connection is often called a **divide by two** circuit for this reason.

2. J-K flip-flop as a D-type latch: clock signal transfers data from D to Q.



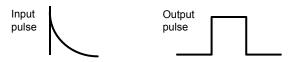
The **asynchronous inputs** R and S are normally held at 1 (depending on the IC being used). Setting S or R to 0 either sets (Q = 1) or resets (Q = 0) the flip-flop and overrides signals on J and K (with S and R active low).

3. A chain of J-K flip-flops in toggle mode.

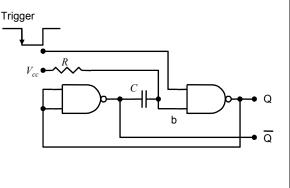


### 12.11 Monostable Multivibrator

Monostable **multivibrators** are used as "wave shaping" circuits. For example, it may be necessary to apply an output pulse which remains high for a pre-determined time on receipt of an input trigger pulse.



Consider the following circuit:



Astable: the outputs oscillate between 0 and 1 continuously. Monostable: the output terminals have one stable state and switch to the opposite state for a short time period before returning to the stable state. Bistable: the output terminals have two stable states, and can

be triggered from one to the other.

In this circuit, the trigger level is normally high. Thus, the output Q is low since this level is NANDed with  $V_{cc}$  through R. With Q low, the output  $\overline{Q}$  is high due to the inverting action of the first NAND gate. Since both sides of the capacitor are high, then there is no charge build-up on the plates and the circuit is stable in this condition.

When the trigger level falls momentarily, Q goes high, which sends  $\overline{Q}$  low. The voltage level at b drops to zero and rises back to  $V_{cc}$  as the capacitor charges according to a time constant which depends on the value of R and C.

When the capacitor charges up fully, voltage at b reaches  $V_{cc}$  and, since the trigger has already returned high, the output Q goes high and the circuit resumes its stable condition.

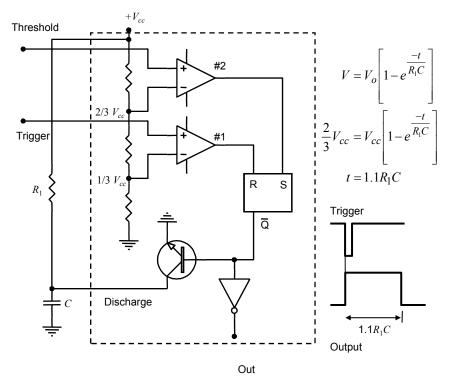
This is a single-shot **monostable multivibrator**. Variations on this circuitry allow the circuit to ignore any further triggers until the output goes back high (non-retriggerable).

#### 12.12 555 Timer

A popular choice for timing applications is the 555 timer IC.

Monostable operation

The 555 contains two comparators whose reference voltages are set at 2/3 and 1/3  $V_{cc}$  by internal resistors. The trigger terminal is usually kept high by an external circuit. When the trigger falls to 1/3  $V_{cc}$ , Comparator #1 sets the flip-flop and the output  $\overline{Q}$  goes low. The output of the IC goes high via the inverter. When  $\overline{Q}$  goes low, the transistor is turned off and the capacitor begins to charge. When the voltage at the capacitor reaches 2/3  $V_{cc}$ , Comparator #2 toggles the flip-flop and the transistor is turned on by  $\overline{Q}$ , thus discharging the capacitor to earth. Thus, a low-going pulse on the trigger causes a high pulse on the output which stays high according to the values of  $R_1$  and C in the external circuit.

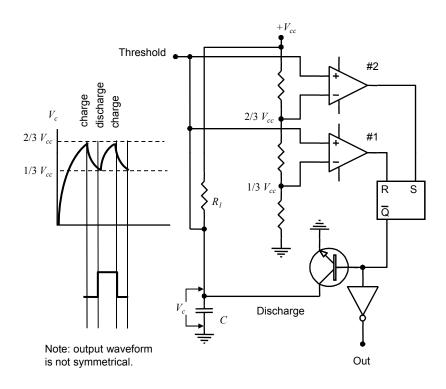


#### Astable operation

The 555 timer IC can be wired for astable operation. It is most often used as an astable timer.

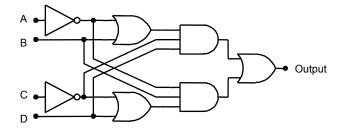
An astable device has no stable state. Its outputs oscillate between set and reset conditions at a fixed frequency. External components (e.g., resistor and capacitor) are usually used to set the frequency of oscillation.

The 555 contains two comparators whose reference voltages are set at 2/3 and 1/3  $V_{cc}$  by internal resistors. The capacitor C charges through  $R_1$  and  $R_2$ . When the voltage at threshold  $V_c$  reaches 2/3  $V_{cc}$  the flip-flop is set by Comparator #1. In this flip-flop,  $\overline{Q}$  goes high which turns on the transistor and discharges the capacitor through  $R_2$ . When the voltage at the threshold  $V_c$  falls to 1/3  $V_{cc}$ . Comparator #2 resets the flip-flop and the transistor is turned off and the capacitor begins to charge again.



### 12.13 Review Questions

- 1. Show how an inverter can be made using a (a) NOR gate, (b) NAND gate.
- 2. Derive an expression for the XOR function using AND and OR expressions.
- 3. Design a logic circuit which implements the AND function but using NOR gates only.
- 4. Design a logic circuit which implements the XOR function but using OR and NOR gates only.
- 5. Design a logic circuit which implements the XOR function but using AND and NAND gates only.
- 6. Express the logic operations of the circuit below in algebraic form.



- 7. Given two TTL packages, one a hex inverter (containing 6 independent NOT gates) and the other a quad 2-input NAND (containing 4 independent, 2 input NAND gates), design a single 4 input gate system to give:  $\overline{A + B + C + D}$ .
- 8. For a three input signal A, B, and C, the exclusive OR operation can be written:

$$(A + B + C) \bullet (\overline{A \bullet B \bullet C})$$

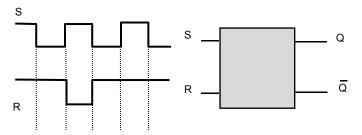
Design a logic circuit to perform this operation using 2- and 3-input NAND gates only. No more than 7 gates should be used.

- 9. Draw Karnaugh maps for the following logic operations and indicate the simplest form of the circuit using NAND gates.
  - (a)  $ABC\overline{D} + ABCD + A\overline{B}C\overline{D} +$ 
    - $AB\overline{CD} + \overline{A}BCD + A\overline{BCD}$
  - (b)  $\overline{ABCD} + \overline{ABCD} + \overline{ABCD}$
- 10. Design a logic circuit which gives an output of 1 whenever a 4 bit binary input is an even number (including zero).
- 11. Construct a Karnaugh map and derive a Boolean expression to implement the following truth table.

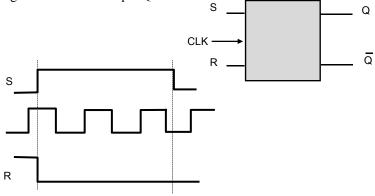
А	В	С	0
0	0	0	0
0	0	1	0 0 0
0 0 0 0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

12. Two 2 bit binary numbers A and B are represented by the bits A0, A1 and B0, B1. Design a simple logic circuit with 3 outputs X,Y and Z, such that X = 1 when A > B, Y = 1 when A = B and Z = 1 when A < B. Use NAND and NOR gates only.</p>

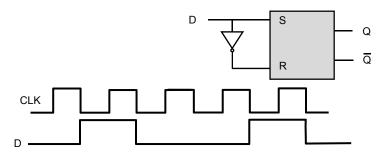
13. Sketch the output Q waveform resulting from the inputs to the RS flip-flop which operates as a NAND gate (assuming Q starts low):



14. A +ve edge triggered clocked RS flip-flop receives the following signals. Sketch the output Q.



15. Sketch the Q output for the input as shown below to a D latch.

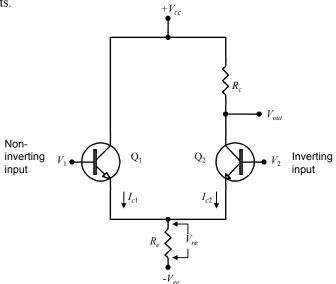


# 13. Operational Amplifiers

)pen-loop gain
lifferential gain
legative feedback
nverting amplifier
lon-inverting amplifier
common mode gain
$\frac{R_2}{R_1}(V_1 - V_2)$ Instrumentation amplifier

### 13.1 Differential Amplifier

A **differential amplifier** has two inputs. The output voltage is measured with respect to earth. The amplifier can be used to amplify both DC and AC. The circuit amplifies the difference between the voltages on the two inputs.



- 1. When  $V_1$  increases (by just a little),  $I_{c1}$  increases and therefore more current flows through  $R_{e'}$  thus causing  $V_{re}$  to increase.
- 2. Increasing  $V_{re}$  means a decrease in  $V_{be}$  of  $Q_2$  and this leads to a decrease in  $I_{b2}$  and hence a decrease in  $I_{c2}$ .
- 3. A decrease in  $I_{c2}$  means an increase in  $V_{out}$  (w.r.t. earth) since there is less voltage drop across  $R_c$ .

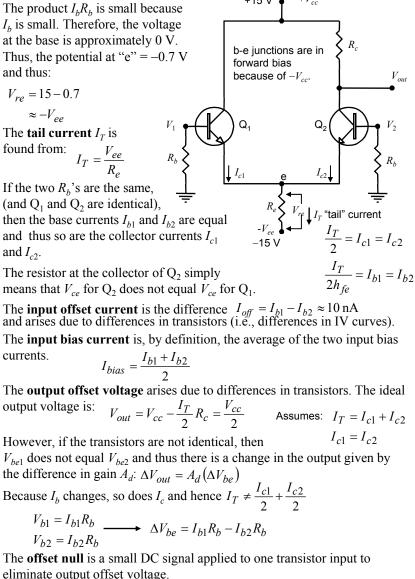
 $V_1$  is a **non-inverting input**. An increase in  $V_1$  results in an increase in  $V_{out}$ .

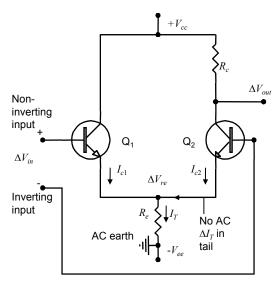
4. When  $V_2$  increases,  $I_{c2}$  increases and hence there is a decrease in  $V_{ce}$  and a larger voltage drop across  $R_c$ . Thus, there is a decrease in  $V_{out}$  (w.r.t. earth).

 $V_2$  is an **inverting input**. An increase in  $V_2$  results in a decrease in  $V_{out}$ .

#### 13. Operational Amplifiers

A useful connection is to tie the base of both transistors to ground through resistors  $R_b$ .





An increase at +ve input gives a decrease  $I_{c2}$  and an increase in  $V_{out}$ . A decrease in the –ve input gives a decrease in  $I_{c2}$  and increase in  $V_{out}$ . The output thus depends on the magnitude of the difference in voltage on the inputs.

 $I_T$  is the total of collector currents:  $I_T = I_{c1} + I_{c2}$ 

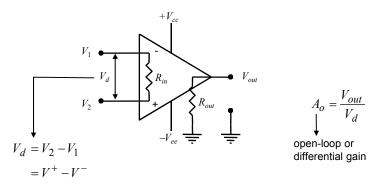
If  $I_T$  is more or less constant, then  $\Delta I_T = 0$  under ideal conditions; thus:

 $\Delta I_{c1} + \Delta I_{c2} = 0$ 

The voltage gain is found from:	in of lef re	Floating level, $R_a$ acts like an
	$\Delta V_{in}^{-} = \Delta I_{b2} h_{ie2} + \Delta V_{re}$	open circuit.
Let $h_{ie1} = h_{ie2}$ , then:	$\Delta V_{in} = \left( \Delta V_{in}^+ - \Delta V_{in}^- \right)$	
$h_{ie}$ is the input	$= h_{ie} \left( \Delta I_{b1} - \Delta I_{b2} \right)$	
resistance of the transistor.	$=2h_{ie}\Delta I_b$ lett	ing $\Delta I_{b1}$ = - $\Delta I_{b2}$
	$=2h_{ie}\frac{\Delta I_c}{h_{fe}}$	
	$\Delta V_{out} = -\Delta I_{c2} R_c$	
	$A_d = \frac{\Delta V_{out}}{\Delta V_{in}} = -\frac{h_{fe}R_c}{2h_{ie}}$	
		—— Input resistance

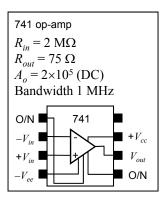
### 13.2 Operational Amplifier

An **operational amplifier** is a differential amplifier with a high AC and DC gain.



Ideal characteristics:

- 1.  $A_o$  is very high ( $\approx 10^6$ ), which gives stability with feedback components
- 2. infinite bandwidth  $-A_o$  is constant over a wide range of frequencies
- 3.  $R_{in}$  is very high
- 4. Rout is close to zero
- 5. minimal drift and low noise
- 6. maintains a constant phase relationship between input and output



### 13.3 Feedback

Consider this block diagram of a difference amplifier:

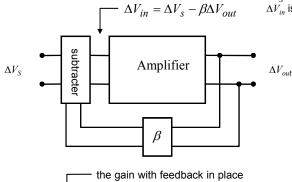


The input and output voltages are related by the **open-loop gain**  $A_o$ .

$$\Delta V_{out} = A_o \Delta V_{in}$$

Now consider the same amplifier with a factor  $\beta$  **feedback** which is subtracted from the input signal:

 $\Delta V_S$  is signal to be amplified  $\Delta V_{in}$  is signal to amplifier



The closed-loop gain is given by:

$$\begin{split} A_C &= \frac{\Delta V_{out}}{\Delta V_S} \\ \text{thus} \quad \frac{\Delta V_{in}}{\Delta V_{out}} &= \frac{\Delta V_S - \beta \Delta V_{out}}{\Delta V_{out}} \\ &= \frac{\Delta V_S}{\Delta V_{out}} - \beta \\ \frac{1}{A_o} &= \frac{1}{A_C} - \beta \\ \hline A_C &= \frac{A_o}{1 + \beta A_o} \end{split} \text{ Negative feedback reduces the voltage gain but, as we shall see, offers other benefits.} \end{split}$$

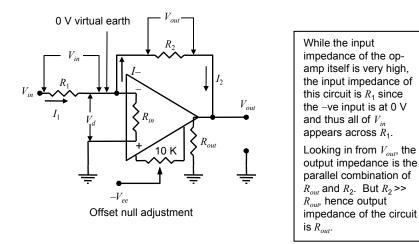
Note: when  $A_o$  is very high, then the closed-loop gain  $A_C$  approaches:

$$A_C = \frac{1}{\beta}$$

#### 13. Operational Amplifiers

### 13.4 Inverting Amplifier

When resistors are connected to allow feedback, the gain of the circuit is reduced and is termed the **closed-loop gain**  $A_c$ . Shown below is an op-amp with one terminal grounded and an input signal (AC or DC) applied (via  $R_1$ ) to the inverting input. This is a **single-ended** mode of operation.



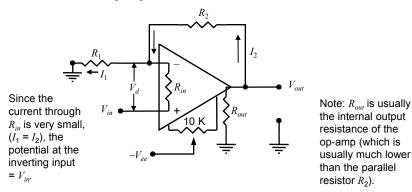
The input resistance  $R_{in}$  within the op-amp is typically very high so I- is very small. Thus,  $I_1 = I_2$  and there is negligible voltage drop across  $R_{in}$ . Hence, the voltage at the inverting input = 0 V but is actually isolated from earth. It is thus called a **virtual earth**.

The current  $I_1$  flows through  $R_1$  and, since I- is negligible,  $I_1$  must then go through  $R_2$  and to earth through the low impedance  $R_{out}$ . Since the -ve input is at 0 V (virtual earth) it follows that the potential at  $V_{out}$  must be < 0, hence the term: **inverting amplifier**.

$$\begin{split} V_{out} &= -I_2 R_2 \\ V_{in} &= I_1 R_1 \\ \frac{V_{out}}{V_{in}} &= -\frac{R_2}{R_1} \qquad I_1 = I_2 \\ \hline A_C &= -\frac{R_2}{R_1} = \frac{1}{\beta} \\ \hline A_c \text{ is the closed-loop gain of the inverting amplifier and depends only on the value of external resistors.} \end{split}$$

#### 13.5 Non-inverting Amplifier

With a little rearrangement, the inverting amplifier can be connected to form a non-inverting amplifier.



Since the potential at -ve input is at  $V_{in}$ , then current *I* flows from -ve to ground through  $R_1$ . Also, since this is a non-inverting amplifier,  $V_{out} > V_{in}$  so current  $I_2$  flows from  $V_{out}$  towards -ve input through  $R_2$ .

$$\begin{split} V_{in} &= IR_1 & \text{Note: the negative feedback ratio is:} \\ V_{out} &= IR_2 + V_{in} & \beta = \frac{R_2 + R_1}{R_1} \\ \hline A_c &= \frac{R_2 + R_1}{R_1} & A_c \text{ is the closed-loop gain non-inverting amplifier and depends only on external resistors.} \end{split}$$

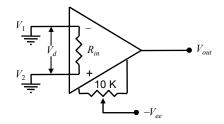
In this case, the input signal is applied directly to the +ve input on the op-amp and hence sees the high  $R_{in}$  associated with the circuitry of the op-amp itself. The output impedance is dominated by the relatively low output resistance of the op-amp but can be reduced by the presence of  $R_2$  in the circuit.

Note: if the currents I+ and I- are "negligible" and the voltage at both inputs is the same (0 V for inverting,  $V_{in}$  for non-inverting) then you might wonder how does the whole thing work? The amplifier works because there is (i) an infinite open-loop gain and (ii) feedback of the output back to the input. The combination of these enables the closed-loop gain to be dependent on the external resistors only.

#### 13. Operational Amplifiers

#### 13.6 Offset

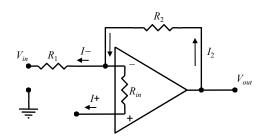
With both inputs at zero,  $V_{out}$  does not usually equal zero due to  $V_{be}$  of each input transistor usually being different.



**Offset null** allows adjustment to  $V_d$  to make  $V_{out} = 0$  when  $V_1 = V_2$ . The amount by which  $V_d$  is changed is called the **input offset voltage**  $V_{os}$ .

The first stage of an op-amp is a differential amplifier. The input transistors require input bias currents I- and I+. Thus a path to ground is required (cannot have any of the inputs "open" or floating).





The input bias current  $I_{bias}$  is the average of I+ and I-.

Due to differences in transistors, *I*- and *I*+ are usually not the same. The difference is called the **input offset current** and is usually an order of magnitude less than the average input bias current.

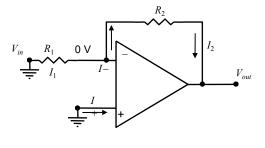
Typical values:  $I_{bias}$  = 80 nA,  $I_{off}$  = 20 nA.

The input offset voltage, input bias current and input offset current all contribute to an undesirable DC voltage at the output terminal.

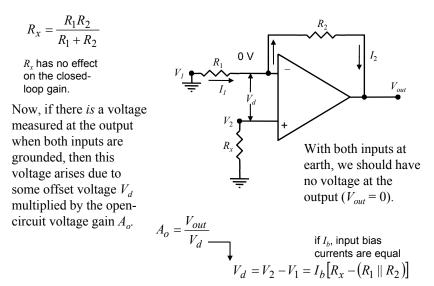
## 13.7 Op-Amp Bias

Consider an inverting amplifier. If both inputs are grounded, then let us assume that any output  $V_{out}$  arises solely from  $I_{off}$  (so that we can see what effect  $I_{off}$  has).

Note: in these types of circuits, current into the op-amp itself (*I*+ and *I*-) flows from earth into the +ve and -ve inputs. How can this be? Because of the presence of  $-V_{cc}$  which is below earth potential. Thus, the transistors within the op-amp are in forward bias (assuming npn).



Consider the resistance to earth as seen by both inputs. For the –ve input, it is evident that  $R_1$  and  $R_2$ , under these circumstances, are effectively in parallel but there is no corresponding resistance to earth for the +ve input. This would lead to an input voltage differential as the input bias currents would be drawn through different resistances. To avoid this, an additional balancing resistor  $R_x$  has to be inserted at the +ve input:



# 13.8 Common Mode Gain

One advantage of a differential amplifier is that the output ideally equals zero when the same signal appears on the inputs.

This is useful for amplifying a signal which contains "noise." If the signal + noise is applied to one input, and the noise alone is applied to the other input, then the differential amplifier will provide an amplified signal and the noise will be rejected (since it is common to both inputs).  $\Delta V_{in1}$ 

$$\Delta V_{in1} = \Delta I_{b1} h_{ie} + \Delta V_{re}$$
  

$$\Delta V_{in2} = \Delta V_{in1}$$
  

$$= \Delta I_{b2} h_{ie} + \Delta V_{re}$$
  

$$V_{in1} + \Delta V_{in2} = h_{ie} (\Delta I_{b1} + \Delta I_{b2}) + 2\Delta V_{re}$$
  

$$= h_{ie} \frac{\Delta I_T}{h_{fe}} + 2\Delta V_{re}$$
  

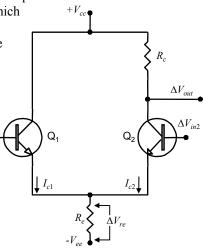
$$= \Delta I_T \left( \frac{h_{ie}}{h_{fe1}} + 2R_e \right)$$
  

$$\approx \Delta I_T 2R_e$$
  

$$2\Delta V_{in} = 2\Delta V_{re} \text{ since } \Delta I_{b1} = -\Delta I_{b2}$$

Δ

$$= 2\Delta I_T R_e \frac{R_c}{R_c}$$
$$\Delta V_{in} = \frac{\Delta I_c}{2} R_c \frac{R_e}{R_c}$$
$$= \Delta V_{out} \frac{R_e}{2R_c}$$
$$A_{cm} = \frac{\Delta V_{out}}{\Delta V_{in}}$$
$$\boxed{A_{cm} = \frac{2R_c}{R_e}}$$



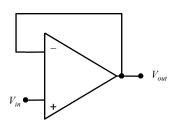
**Common mode rejection ratio** This is a measure of quality for the response of an amplifier to common signals on the inputs. A good amplifier has a small common mode gain  $A_{cm}$ .

$$CMRR = \frac{A_o}{A_{cm}} = 20 \log_{10} \frac{A_o}{A_{cm}}$$
  
e.g., CMRR = 100 db,  $A_o = 10^5$   
 $100 = 20 \log_{10} \frac{10^5}{A_{cm}}$   
 $A_{cm} = 10^{-3}$   
 $V_{in}+V_{cm}$   
 $V_{cm}$   
 $V_{cm}$   
 $+$   
 $V_{out} = A_o V_{in} + A_{cm} V_{cm}$ 

## 13.9 Op-Amp Applications

#### Voltage follower

A voltage follower is a non-inverting amplifier with  $A_c = 1$  and 100% feedback. This circuit makes use of the very



This circuit makes use of the very high open-loop gain of an op-amp to make a **buffer** which has a very high input impedance. Such a buffer may be connected at the inputs to an inverting or non-inverting amplifier to present a high resistance to the signal source.

> Input resistance: high Output resistance: low

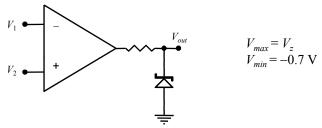
$$V_d$$
 normally = 0. Thus,  $V_{in} = V_{out}$ .

$$R_{in_{new}} = R_{in_{old}} (1 + |\beta| A_o)$$
  

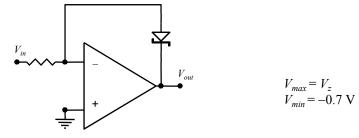
$$\approx R_{in_{old}} 10^5 \qquad \begin{array}{c} \beta = 1 \\ A_o = 10^5 \end{array}$$

#### Voltage limiter

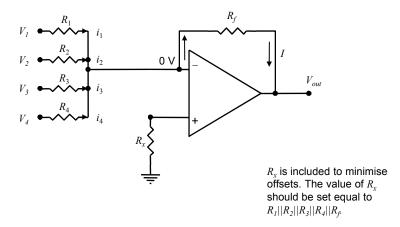
It is often required for  $V_{out}$  to be between 0 V and  $V_{max}$  where  $V_{max} < V_{cc}$ . This can be done using a zener diode and current limiting resistor in the output. The general circuit is shown below:



In another example, in the circuit below, when  $V_{in} > 0$  V,  $V_{out}$  is restricted to -0.7 V. When  $V_{in} < 0$ , then  $V_{out}$  is restricted to a maximum of  $V_Z$ .



# 13.10 Operational Adder



This type of "analogue" circuit was first used to perform an adding operation, hence the name **operational amplifier**. Op-amps are now used in a wide variety of other applications.

$$\frac{V_{out}}{V_{in}} = -\frac{R_f}{R}$$

$$V_{out} = -\left(\frac{V_{in}}{R}\right)R_f$$

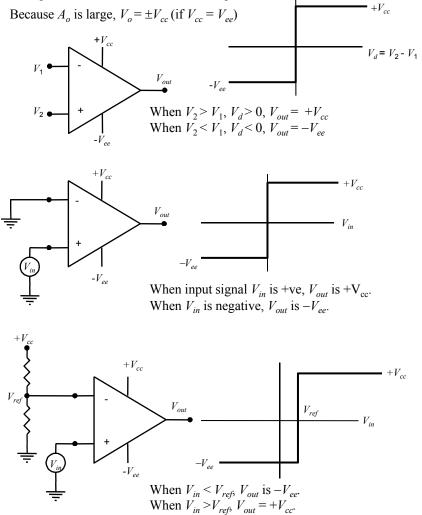
$$V_{out} = -(i_1 + i_2 + i_3 + i_4)R_f$$

$$= -R_f\left(\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} + \frac{V_4}{R_4}\right)$$

Output is the weighted sum of the input voltages. If  $R_1 = R_2 = R_3 = R_4 = R_f$ then the circuit simply sums the voltages on the inputs. If  $R_1 = R_2 = R_3 = R_4$ = R, and  $R_f = 4R$ , then the circuit finds the average of the voltages on the inputs.

## 13.11 Comparator

A comparator circuit switches the output on a change in relative polarity on the inputs. No feedback elements are required.

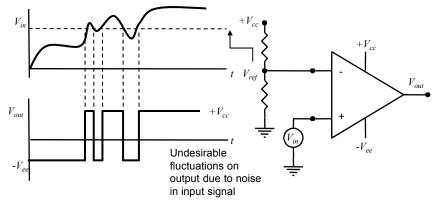


A typical example is for a thermostat, where  $V_{in}$  may be the output from a thermocouple. When the thermocouple output voltage reaches  $V_{ref}$ ,  $V_{out}$  goes positive, which may operate a relay which switches off the heating element.

#### 13. Operational Amplifiers

## 13.12 Schmitt Trigger

Comparators do not often work as desired when the input signal contains "noise." That is, fluctuations in  $V_{in}$  may cause the output of a comparator to toggle from  $+V_{cc}$  to  $-V_{ee}$  as the average value of  $V_{in}$  approaches  $V_{ref}$ .



The **Schmitt trigger** is a variation on the basic comparator circuit designed to overcome this problem. The reference voltage is taken from a voltage divider on the output. Thus, when the output changes state, the reference voltage changes.

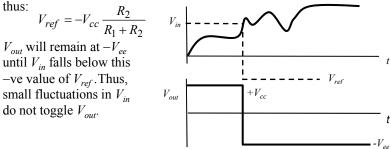
 $V_{in}$ 

Negative-going Schmitt trigger:

If  $V_{in}$  is initially less than  $V_{ref}$ , then  $V_{out} = +V_{cc}$ 

$$V_{ref} = +V_{cc} \frac{R_2}{R_1 + R_2}$$

The output will stay at  $+V_{cc}$  until  $V_{in}$  goes above this value of  $V_{ref}$ . When this happens,  $V_{out}$  goes to  $-V_{ee}$  and  $V_{ref}$  changes



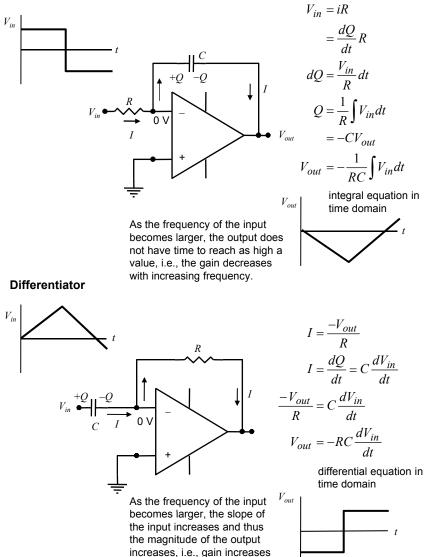
 $V_{out}$ 

 $R_1$ 

 $R_2$ 

# 13.13 Integrator/Differentiator

Integrator

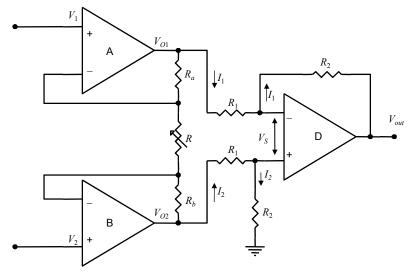


increases, i.e., gain increase with increasing frequency.

#### 13. Operational Amplifiers

## 13.14 Instrumentation Amplifier

An **instrumentation amplifier** has a high gain and high CMRR. It is formed by using cross-coupled inputs for high CMRR and high input impedance.



The gain of the input stage is:

$$\frac{V_{o1} - V_{o2}}{V_1 - V_2} = \frac{\left(R_a + R_b + R\right)}{R}$$

The gain of the output stage is:

$$A_d = \frac{R_2}{R_1}$$

Thus the total gain is:

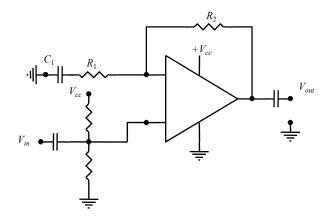
$$\begin{split} A_{\nu} &= -\frac{\left(R_a + R_b + R\right)}{R} \frac{R_2}{R_1} \\ &= -\frac{\left(R_a + R_a + R\right)}{R} \frac{R_2}{R_1} \\ A_{\nu} &= -\left(\frac{2R_a}{R} + 1\right) \frac{R_2}{R_1} \end{split} \quad \text{letting } R_a = R_b \\ \text{Note that if } V_1 = V_2, \text{ then } V_{out} = V_0 \\ \text{("infinite" CMRR).} \end{split}$$

The resistors  $R_1$  at the input to the output differential amplifier are trimmed to eliminate amplification of any common mode signal. It is usual to use the gain of the input stage to be the overall gain of the amplifier while the output stage is set to unity gain:  $R_2/R_1 = 1$ . The purpose of the output stage difference amplifier D is to simply reject any common mode signal.

0

# 13.15 Audio Amplifier

Often in portable equipment, a dual polarity power supply is not available. However, an op-amp circuit can be configured to operate using a single +ve power supply as shown below.



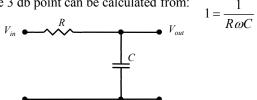
Since the  $-V_{ee}$  terminal is grounded, then the output from the op-amp is always positive. Actual circuit operation, however, is not affected, with all inputs lifted up by  $+V_{cc}/2$ . The capacitor  $C_1$  in the feedback path means that for DC, the circuit is a voltage follower with a gain of 1.

The +ve input is held at  $V_{cc}/2$  by a voltage divider. Since the DC gain of the amplifier is 1, then the output also sits at  $V_{cc}/2$ . Coupling capacitors isolate these DC "bias" levels from the input and output devices.

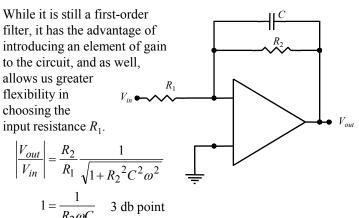
Use of an op-amp as an audio amplifier allows a reasonably high gain with low distortion and good input and output impedance characteristics.

## 13.16 Active Filter (1st-Order)

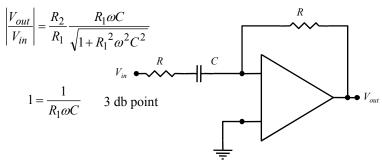
A passive **low-pass filter** is usually constructed from a resistor and a capacitor where the 3 db point can be calculated from: 1



This first-order filter has a roll-off of 20 db/decade. Using an op-amp, a first-order low-pass **active filter** can be obtained using the following circuit:



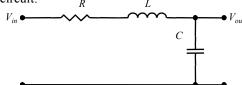
A first-order high-pass filter based on an op-amp is:



If one considers the inverting input to be the **virtual earth**, then these filters are essentially passive filter networks connected to a unity gain **voltage follower**, or **buffer**.

# 13.17 Active Filter (2nd-Order)

Ideally, a filter should have a sharp **corner frequency** and a steep roll-off so that only the desired frequency is passed. A first-order filter has a fairly leisurely 20 db/decade roll-off, which may not be suitable for many applications. A **second-order filter** can be made by a tandem connection of two first-order filters, but while this has a steeper roll-off, at 40 db/decade, the corner frequency is still too rounded. A better solution is an *LCR* resonant circuit: R L

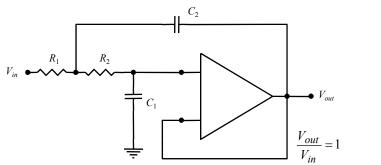


Here, the Q point of the circuit determines the strength of the peak while the roll-off remains at an acceptable level.

$$\frac{V_{out}}{V_{in}} = \frac{1}{1 - \omega^2 LC + R\omega Cj}$$

The resonant frequency is:  $\omega_o = \frac{1}{\sqrt{LC}}; \quad Q = \frac{\omega_o}{LR}$ 

In most electronic circuits, inductors are generally avoided due to cost and influence from magnetic fields. However, the characteristics of an *LCR* circuit can be replicated by an op-amp in the following configuration.



This second-order low-pass filter is one of a family of **Sallan and Key** filters. In this case, the op-amp is wired in voltage follower configuration and so has a gain of 1. The Q factor determines the shape of the response at the resonant frequency, or cut-off.

$$\omega_o = \frac{1}{\sqrt{R_1 R_2 C_1 C_2}}$$
$$Q = \frac{\sqrt{R_1 R_2 C_1 C_2}}{C_2 (R_1 + R_2)}$$

#### 13. Operational Amplifiers

# 13.18 Review Questions

1. A certain amplifier has an open-loop gain of 250. Calculate the overall gain if the amplifier is constructed with 10% negative feedback.

(Ans: 9.61)

2. If the open-loop gain of an amplifier is infinite, calculate the closed-loop gain with 20% feedback.

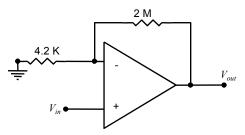
(Ans: 5)

3. A 2 mV input signal is applied to a differential amplifier on top of a 500 mV common mode signal. If the amplifier has a differential gain of 200, what CMRR is required for no more than 1% of the output signal to be contributed by the common mode input signal?

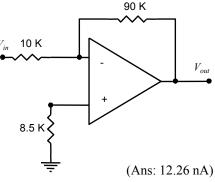
(Ans: 86 dB)

4. Calculate the closed-loop gain and the % feedback of the circuit shown:

(Ans: 477, 0.21%)

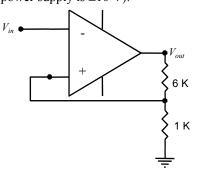


5. An inverting amplifier has an output of 460 mV when the input voltage  $V_{in}$  is zero. If the open-loop gain is 75000, calculate the bias currents drawn by each input assuming that the input offset current is approximately zero. 8.5 K



- 47 K 5 K 1.5 V• 10 K -0.4 V•  $V_{out}$ 20 K 0.8 V (Ans: -14.1 V, 2.7 kΩ) +20 V 7. Sketch the form of the output from the circuit shown below: +10 V 15 K  $V_{in}$ +6 V  $V_{out}$ t (msec) 5 K -6 V
- 6. Calculate the output voltage of the circuit shown and also calculate the value of  $R_{\chi}$ .

8. Determine turn on and turn off conditions for the Schmitt trigger circuit below (power supply is  $\pm 10$  V).



I

8

2

6

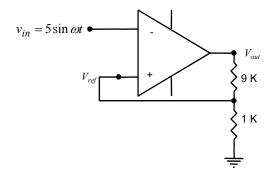
(Ans:  $V_{ref} = 1.43$  V)

-10 V

 $V_{in}$ 

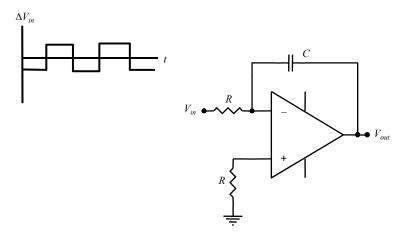
### 13. Operational Amplifiers

9. Determine which times the output goes from +10 V to -10 V in the Schmitt trigger circuit below when driven with a 1.592 kHz sine wave.

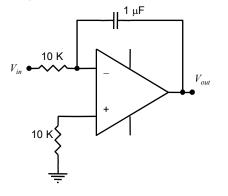


<sup>(</sup>Ans: 20.1 µs, 334 µs)

10. Sketch the output of the integrator circuit when fed with a square wave as shown:

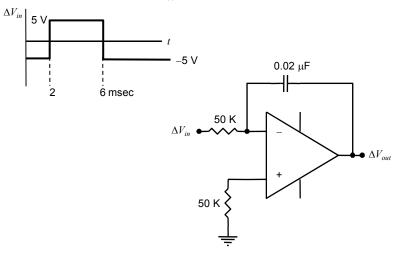


11. An integrator circuit has a 1  $\mu$ F capacitor as the feedback element and a 10 k $\Omega$  resistor. Calculate how long it will take the output to reach the power supply voltage –15 V if 5 mV DC is applied to the input (assume  $V_{out} = 0$  @ t = 0).



(Ans: 30 s)

12. The output of the integrator circuit shown below is 0 V at t = 0. Calculate the output voltage at t = 2 msec, 6 msec and 7 msec and sketch the output waveform ( $V_{cc} = \pm 15$  V).



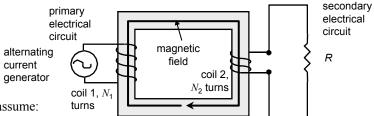
(Ans:  $V_{out} = +10 \text{ V}$  @ t = 2, -10 V @ t = 6, -5 V @ t = 7)

# 14. Transformers

Summary		
$I_{rms} = \frac{H_p l}{\sqrt{2}N}$	Magnetising current	
$\frac{E_1}{E_2} = \frac{N_1}{N_2}$ $= a$	Transformation ratio	
$R_{eq} = \left(\frac{N_1}{N_2}\right)^2 R$	Equivalent resistance	
$Z_p = Z_L \left(\frac{N_1}{N_2}\right)^2$	Reflected impedance	
$=a^2Z_L$		
$\eta = \frac{V_2 I_2 \cos \phi}{V_2 I_2 \cos \phi + (I_1^2 R_1 + I_2^2 R_2) + P_{CL}}$		
	Transformer efficiency	

# 14.1 Transformers

Transformers are generally used to change voltages levels – such as those at mains level to those required by electronic circuits.



Let us assume:

- the secondary terminals are initially open
- all the flux is confined to the iron core so that flux  $\Phi$  is same in each coil
- resistance of windings can be neglected

Considering the primary coil: e U  $V_L$   $V_L$ Note: using small e to denote instantaneous value of applied emf.

Any voltage that appears across the terminals of the coil (effectively an inductor) must be due to the self-induced voltage (**back emf**) in the coil by a changing current through it (**self-inductance**).

$$L\frac{di}{dt} = N_1 \frac{d\phi}{dt}$$
 Instantaneous  $e_L$  is proportional to rate of  
=  $-e_L$  change of current or rate of change of flux,

At any instant,  $e_L = -e$  by Kirchhoff

thus

$$e = L \frac{di}{dt}$$

$$= V_p \sin(\omega t)$$
Instantaneous current in coil  
lags instantaneous voltage  
across it.  

$$i = \left[\frac{V_p}{\omega L}\right] \sin\left(\omega t - \frac{\pi}{2}\right)$$

But the magnetic flux depends directly on the current. Thus, flux in the core lags the applied voltage *e* by  $\pi/2$ .

#### 14. Transformers

# 14.2 Transformer Equations

Now, since the magnetic flux is confined to the core, the same flux passes through each turn of the primary coil. The self-induced voltage in the primary is:  $d\Phi$ 

$$e_1 = N_1 \frac{d\Phi}{dt}$$

The flux in the core is sinusoidally varying with time:

$$\phi = \Phi_p \sin(\omega t - \pi/2)$$

$$\frac{d\phi}{dt} = \omega \Phi_p \cos(\omega t - \pi/2) \quad \text{max when cos term} = 1$$

$$-e_1 = N_1 \omega \Phi_p \cos(\omega t - \pi/2)$$

$$\frac{E_{1p} = N_1 \omega \Phi_p}{E_{1rms} = \frac{E_{1P}}{\sqrt{2}}} \quad \text{since } V_{rms} = \frac{V_p}{\sqrt{2}}$$

$$E_{1rms} = \frac{N_1 \omega \Phi_P}{\sqrt{2}}$$

For the magnetic circuit in the core:

$$R_{m} = \frac{f_{m_{1}}}{\phi} \longrightarrow \text{Magnetomotive force (mmf)} \\ \text{established by current in coil 1} \\ = \frac{N_{1}i_{1}}{\phi} \quad \text{(lower case denotes instantaneous values)} \\ \phi = \frac{N_{1}i_{1}}{R_{m}} \quad \text{The alternating flux in the core is} \\ \text{created by the alternating current in} \\ \text{the primary coil.} \\ \text{reluctance of the} \\ \text{magnetic circuit} \end{cases}$$

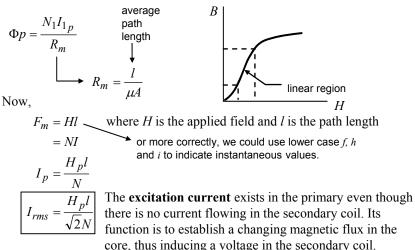
The maximum value of the current is thus:

$$\Phi p = \frac{N_1 I_{1p}}{R_m}$$
$$I_{1p} = \Phi_P \frac{R_m}{N_1}$$

This maximum current induces a maximum magnetic flux in the core.

# 14.3 Transformer Action

For the magnetic flux in the core to be a sine wave, the flux density in the core must remain in the linear region of the magnetisation curve for the steel being used (i.e., not saturated). The maximum flux will then depend only on the cross-sectional area of the core and the path length.



In the ideal case (no flux leakage), all the flux produced by the primary coil will link with the secondary coil  $\Phi_1 = \Phi_2$  and induce a voltage  $E_2$  in the secondary.

$$E_2 = N_2 \frac{d\Phi}{dt}$$

Expressed as an rms voltage, we have:

$$E_{2rms} = \frac{N_2 \omega \Phi_p}{\sqrt{2}}$$

The same changing flux is responsible for the induced voltages in both coils; thus the instantaneous and peak voltages  $e_1$ ,  $E_{1p}$  and  $e_2$ ,  $E_{2p}$  are in phase.

The ratio of voltages in the primary and secondary coils is:

$$\boxed{\begin{array}{c} \frac{E_1}{E_2} = \frac{N_1}{N_2} \\ = a \end{array}} \quad \begin{array}{c} \text{Instantaneous, rms} \\ \text{or peak values} \\ \text{since all in phase} \\ \text{Transformation ratio} \end{array}$$

**Transformers** thus provide a way to transform a given AC voltage to another. If a > 1 we have a step-down transformer, if a < 1, a step-up transformer.

#### 14. Transformers

## 14.4 Transformer Impedance

From Faraday's law, the voltage in the primary coil must be equal and opposite to that from the generator and is found from:

$$V_1 = -N_1 \frac{d\Phi}{dt}$$

In the ideal case (no flux leakage), all the flux produced by the primary coil links will the secondary coil  $\Phi_1 = \Phi_2$  and induces a voltage in the secondary. The induced voltage in the secondary is:

$$V_2 = N_2 \frac{d\mathbf{d}}{dt}$$
  
Since  $\Phi_1 = \Phi_2$ , then:  $\frac{V_2}{V_1} = \frac{N_2}{N_1}$ 

If  $N_1 > N_2$ , the amplitude of the secondary voltage is less than that of the primary and is called a **step-down transformer**. If  $N_1 < N_2$ , the amplitude of the secondary voltage is greater than that of the primary (**step-up transformer**).

The ratio of currents in the primary and secondary is given by:

$$N_1 I_1 = N_2 I_2$$

A transformer, as well as having the useful property of stepping up or stepping down voltages, can also be used for **impedance matching**. The magnitude of the load resistor determines the secondary current.

$$I_{2} = \frac{V_{2}}{R} = \frac{N_{1}}{N_{2}}I_{1} = \frac{N_{2}}{N_{1}}\frac{V_{1}}{R}$$
$$I_{1} = \left(\frac{N_{2}}{N_{1}}\right)^{2}\frac{V_{1}}{R}$$

Thus, the primary side sees an equivalent resistance:

$$R_{eq} = \left(\frac{N_1}{N_2}\right)^2 R$$

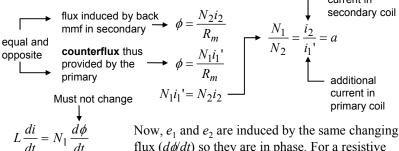
# 14.5 Load Component of Primary

If an impedance is connected to the secondary coil, then a current (AC) will flow due to the action of the induced voltage  $E_2$ . This current will create a back mmf in the secondary coil, which will tend to reduce the flux in the core (Lenz's law).

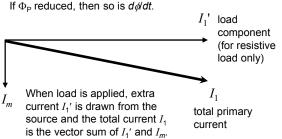
This opposing flux has the effect, from the primary side point of view, of decreasing the inductance (and

The induced current creates a magnetic field of its own. If the original field is increasing, then the direction of the induced field is such as to oppose that increase and thus is in the opposite direction.

hence decreasing the reactance  $\omega L$ ) seen by the voltage source. Hence, more current will flow in the primary. The increase in primary current  $i_1$ ' restores the peak flux back to its original value, thus keeping the rate of change of flux a constant and hence the induced back emf in the primary equal to the voltage level from the source (Kirchhoff).



flux  $(d\phi/dt)$  so they are in phase. For a resistive load on the secondary, the current  $i_2$  is in phase with  $e_2$  and hence with  $e_1$  and thus  $i_1'$  is also in phase with  $e_1$ . But, the **magnetising current** in the primary,  $i_m$ , lags the applied voltage by  $\pi/2$ . Thus, for rms and peak values the current is the vector sum of the rms or peak values of the two components.



 $-e_I = e$ 

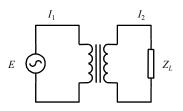
Φ

Before load is applied, the current  $I_1$  serves to create the magnetic circuit in the core and thus induce a voltage in the secondary and is thus called the **magnetising current** and given the symbol  $I_m$ .

#### 14. Transformers

## 14.6 Reflected Impedance

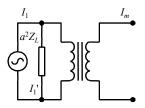
When a load is connected to the secondary, the primary current increases. The rms or peak primary current is the vector sum of the rms or peak magnetisation current and the additional or "load" component.



Now, an increase in the primary current can equally well occur if we insert an impedance in parallel with the primary coil and remove the load from the secondary as shown:

The parallel branch carrying  $I_1$ ' appears to have an impedance given by:

$$Z_{p} = \frac{E_{1}}{I_{1}} \text{ rms values}$$
  
but  $E_{1} = aE_{2}$   
and  $I_{1}' = \frac{I_{2}}{a}$   
 $\therefore Z_{p} = \frac{E_{2}}{I_{2}} \left(\frac{N_{1}}{N_{2}}\right)^{2}$ 



Note that  $I_1 \iff I_m + I_1'$  must use vector sum for rms or peak values.

But,  $E_2/I_2$  is the total impedance of the secondary circuit, i.e., approx  $Z_L$ . Thus, since impedance of secondary winding is usually small compared to load impedance:

$$Z_p = Z_L \left(\frac{N_1}{N_2}\right)^2$$
$$= a^2 Z_L$$

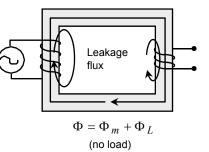
The impedance of the parallel branch of the primary circuit (sometimes called the **reflected impedance**)

Since the primary side of the coil itself does not dissipate any power (being a "perfect" inductor), then attaching a load impedance  $Z_L$  to the secondary, from an energy point of view, is the same as connecting an impedance  $a^2Z_L$  directly to the source.

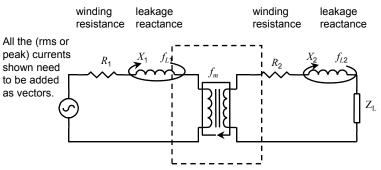
This property enables a transformer to be used for impedance matching.

## 14.7 Real Transformers

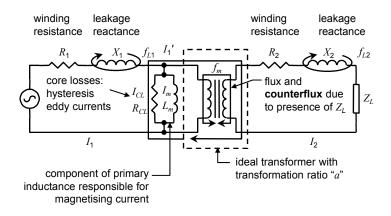
So far we have assumed that all the flux created by the magnetisation current in the primary links to the secondary coil. In practice, some flux lines leak and loop back without linking to the secondary coil. This is the primary leakage flux. The remainder of the total primary flux links with the secondary coil and is called the **mutual flux**  $f_m$ .



Leakage flux constitutes an inductive reactance  $X_1$  in the primary circuit. Similar events occur on the secondary (when  $Z_L$  connected) and if we add in the resistance of the windings  $R_1$  and  $R_2$ , the equivalent circuit is thus:



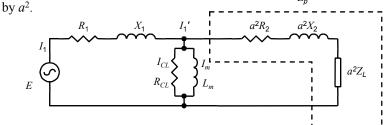
It is convenient to also separate out the inductance which is responsible for the magnetisation of the core and to group this with **core losses** thus:



#### 14. Transformers

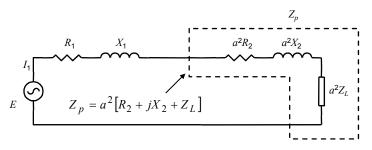
## 14.8 Transformer Tests

All the reactances on the secondary side can be transferred across to the primary side if they are multiplied  $Z_p$ 



#### Short-circuit test:

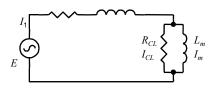
With  $Z_L$  connected,  $I_1'$  is usually much larger than  $I_m$  so that the branch  $I_{CL}$ ,  $I_m$  can be ignored. The primary side thus sees a total load impedance of:



With  $Z_L = 0$  (short circuit on secondary side) the only energy dissipation is due to  $R_1$  and  $R_2$ , the so-called **copper losses** for both windings. Note that the copper losses depend on the current ( $I^2R$ ).

#### **Open-circuit test:**

With  $Z_L$  = infinity,  $I_1' = 0$  and thus the only current is  $I_m$  and  $I_{CL}$ . The only energy dissipation is  $R_{CL}$ , the **core losses**. Further, for  $I_m$  and  $I_{CL}$  alone,  $R_1$  and  $X_1$  are also negligible so that the equivalent circuit is thus:

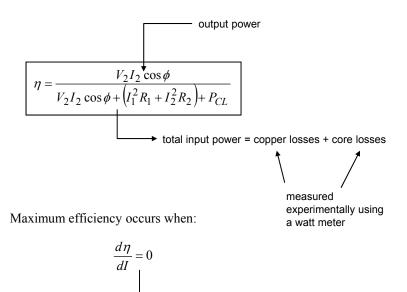


 $R_1$  and  $X_1$  are small and only cause an appreciable voltage drop when  $I_1'$  (much larger than  $I_m$  and  $I_{CL}$ ) is flowing.

Core losses  $R_{CL}$  can be assumed to be constant and independent of the current in the secondary  $I_2$ .

# 14.9 Transformer Efficiency

The efficiency of a transformer is an indication of the proportion of energy loss or dissipation when the transformer is transferring energy from the primary circuit to the secondary.



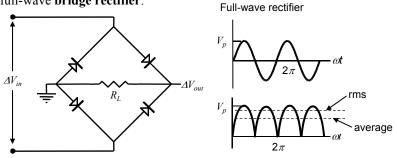
→ when copper losses = core losses

# 15. Power Supplies

Power dissipation in zener diode
Ripple voltage
Line regulation
Average value of a full-wave rectifier output

## 15.1 Rectification

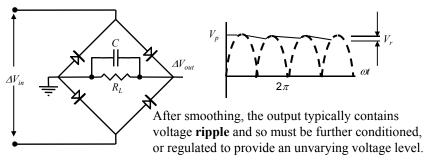
The AC output from a transformer is required to be converted to a steady DC value by rectification. This is usually accomplished using diodes in a full-wave **bridge rectifier**.



A rectified output consists of a positive voltage, but varying from 0 V to the amplitude of the transformer secondary output voltage (neglecting the drop across the diodes). The average **DC**  $V_{av} = \frac{0}{\pi}$ **equivalent value** of the output  $V_{avg}$  is the value that would be measured by a DC voltmeter. This is not the same as the rms value, which is measured by an AC voltmeter. The average value of a symmetric waveform is taken over half a cycle (since the average value over a full cycle would be zero).  $=\frac{2V_p}{\pi}$ 

 $= \frac{1}{\pi} \int_{0}^{\pi} V_{p} \sin \theta d\theta$  $= \frac{2V_{p}}{\pi} \quad \text{for a full-wave}$ 

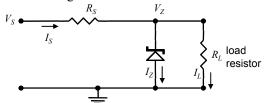
The most common method of providing a steady DC source is by the use of a **smoothing capacitor**. The capacitor alternately charges and discharges and serves to smooth out the variations in the output voltage from the rectifier.



The peak-to-peak ripple voltage is found from:  $V_r = \frac{V_o}{2fR_LC}$  f is in Hz

## 15.2 Regulation

**Zener diodes** find special application as voltage regulators. They have a very sharp reverse bias breakdown characteristic. In a **voltage regulator**, the supply voltage can change significantly but the zener diode voltage  $V_Z$  does not change.



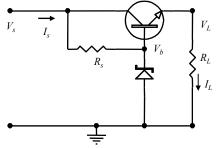
 $V_L = V_z$  and  $I_s$  is thus fixed and independent of  $R_L$ . If  $R_L$  increases, the zener passes more current to keep  $V_L = V_z$ . When  $R_L$  is infinite (open-circuit),  $I_z = I_s$ .

Maximum current in the zener diode occurs at open-circuit conditions where all the current passes through the diode. The **maximum power dissipation** in the diode depends on the input voltage, the breakdown voltage and limiting resistor  $R_s$ : (V - V)

$$P_{max} = V_z I_{max} = V_z \left(\frac{V_s - V_z}{R_s}\right)$$

If  $R_L$  were to decrease, then less current would pass through the zener diode. Since there is a minimum current which must pass through the diode ( $\approx 5$  mA) to maintain operation well into the breakdown region, this limits the amount of current that can be drawn by the load resistor  $R_L$ . If the maximum current through the zener is given by  $I_{max}$ , and approximately 5 mA is required for reverse breakdown, then the maximum current that can pass through the load resistor  $R_L$  is approximately ( $I_{max}$ -5) mA. This might typically be on the order of 10 mA or so.

A regulator for **high current output** may be constructed using a zener diode in conjunction with an emitter follower circuit.



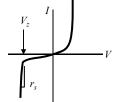
If the load resistance increases, the load voltage  $V_e$  increases. An increase in  $V_e$  leads to a decrease in  $V_{be}$  since the voltage at the base is held constant by the zener diode. The decrease in  $V_{be}$  results in an increase in  $V_{ce}$  and decrease in  $V_{e}$ , i.e., the output voltage is held constant.

Here the current output is increased over that normally available by a factor equal to the current gain of the transistor. The diode voltage must be selected to account for the 0.7 V drop across the base-emitter junction.

# 15.3 Load and Line Regulation

In voltage regulator circuits such as those shown previously, it is convenient to measure the performance of the circuit in terms of its **load regulation** and **line regulation**.

**Load regulation** is the percentage change in the output voltage for a change in the load current from zero to full load. In a zener diode circuit, load regulation is affected by the presence of the finite slope of the breakdown region, which is called the **dynamic resistance**  $r_{s'}$  which might be as much as a few ohms.



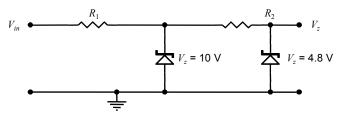
When  $V_{in}$  changes,  $I_Z$  also changes and so the output voltage is also changed via:  $V_{out} = V_z + I_z r_s$ 

The **line regulation** is the change in the output voltage divided by a change in the input voltage expressed as a percent:

Line regulation = 
$$\frac{\delta V_{out}}{\delta V_{in}} \times 100$$

A zener diode regulator incorporating an emitter follower has improved load regulation over that of a simple diode regulator but the line regulation is still limited by the dynamic resistance of the reverse breakdown region.

To overcome the effects of the dynamic resistance of the breakdown region of a zener diode, a second diode may be incorporated into the circuit to act as a pre-stabiliser. In the circuit below, the 10 V zener diode acts as a **prestabiliser** for the 4.8 V diode. In this case, the line regulation at the output is considerably improved. This type of circuit acts as a precision **voltage reference** where the output can be used for logic elements or op-amp supplies.

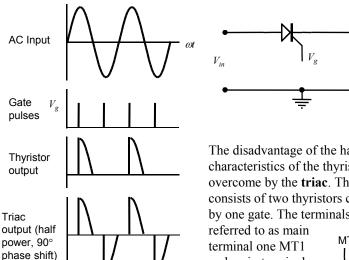


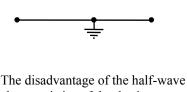
# 15.4 Thyristor and Triac

A thyristor, or silicon controlled rectifier, SCR, is a voltage regulator with a high breakdown voltage and current gain. c

The device has three terminals. Current flows from the anode to the cathode when a pulse is put at the gate terminal. Conduction stops when the supply voltage to the anode is removed whereupon it must be re-triggered at the gate even if voltage is restored to the anode.

This action acts as a rectifier when connected to an AC source. Gate pulses result in current flow until the supply AC falls below 0 V. The timing or phase of the pulses on the gate determines how much of the AC waveform is allowed to pass through the device. When the gate pulses coincide with the positive-going AC half cycle, we obtain a half-wave rectifier action.





characteristics of the thyristor are overcome by the triac. This device consists of two thyristors controlled by one gate. The terminals are MT1 and main terminal two MT2.

Triacs are particularly common in controlling the speed of electric motors or light dimming. They also are used in switched mode power supplies in which the low

frequency mains voltage is rectified directly into a high frequency voltage which is then fed into a step-down transformer and further rectified and regulated. The advantage of operating directly on the mains in this way is that the step down transformer and smoothing capacitors, operating at high frequency, can be made very compact.

g

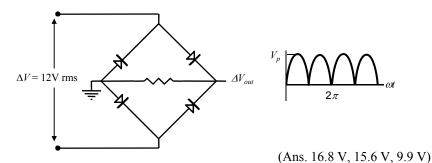
 $V_{out}$ 

g

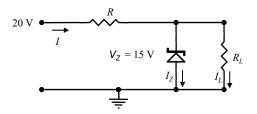
MT2

# 15.5 Review Questions

1. The output from a full wave rectifier (unfiltered) is shown. Allowing for 0.7 V across each diode, calculate (a) the peak voltage at the input to the rectifier, (b) the peak voltage at the output and (c) the average DC equivalent output voltage.



- 2. Explain the difference in behaviour of an unregulated power supply and a regulated power supply.
- 3. In the circuit below, the load resistor  $R_L$  carries a current of 150 mA. The maximum allowable current through the zener diode is rated at 60 mA. Determine (a) a suitable value of *R* if 20% of the rated load current is to be maintained in the zener diode and (b) the value of  $R_L$ .



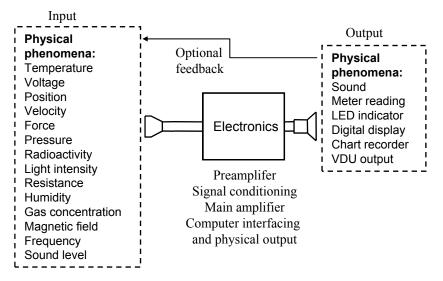
# 16. Instrumentation

Summary	
sensitivity = $\frac{\text{output signal}}{\text{input signal}}$	Transducer sensitivity
$SNR = 20\log_{10} \left  \frac{V_S}{V_n} \right $	Signal to noise ratio
$V_n^2 = 4kTR\Delta f$	Thermal noise
$P = \frac{V^2}{R} = 4kT\Delta f$	
$i_n^2 = 2eI_s \Delta f$	Shot noise
$P_n = i_n^2 R = 2\Delta f e i_n R$	
$\frac{V_{out}}{V_{in}} = \frac{1}{1 + R\omega Cj}$	Transfer function low-pass filter
$\frac{V_{out}}{V_{in}} = \frac{R}{R - \frac{1}{\omega C}j}$	Transfer function high-pass filter
$\frac{V_{out}}{V_{in}} = -\frac{1}{jR\omega C}$	Transfer function integrator
$\frac{V_{out}}{V_{in}} = -jRC\omega$	Transfer function differentiator

# 16.1 Instrumentation

The field of electronics can find application in many areas – from communications to household goods. One of the most important applications is that of scientific **instrumentation**. That is, measuring a physical quantity using a **transducer**, and then displaying a meaningful output.

The physical quantity may be such diverse things as **temperature**, **pressure**, **velocity**, **time**. Transducers convert the physical quantity into an electrical signal. The signal may then be processed by filtering and amplification and so become capable of being displayed or recorded. Recording to a computer will involve **analog to digital conversion** of the output signal.



Electronics also finds wide application in **control** of physical phenomena. For example, a user of a force testing machine might set the desired force by a computer command. This input is used to control the servo-motor (i.e., an **actuator**) that winds a lead screw and produces the desired force on the specimen. Control of equipment by electronics often requires **digital to analog conversions**.

In many circumstances, the user-controlled output results in a change in a physical quantity which is then measured using a transducer. The measured output can be fed back to the control input, thus causing the system to be in **closed-loop control**. Many servo-motion systems work this way.

# 16.2 Transducers

A **transducer** responds to a physical phenomena and converts this into an electrical signal.

Property	Transducer
Strain	Strain gauge
Temperature	Thermocouple
Humidity	Resistance change of hygroscopic material
Pressure	Bourdon tube attached to a pointer and scale
Voltage	Moving coil and pointer
Radioactivity	Electrical pulses resulting from ionisation of gas at
	low pressure (Geiger tube) or of flashes of light in a scintillation crystal
Magnetic field	Deflection of a current-carrying wire.

Transducers have certain characteristics that must be taken into account when selecting one for a particular application. For example, a moving coil voltmeter might not be suitable in an environment that is subjected to heavy mechanical vibration. Some examples of important characteristics are:

Static	Dynamic	Environmental
Sensitivity Zero offset Linearity Range Span Resolution Threshold Hysteresis	Response time Damping Natural frequency Frequency response	Operating temperature range Orientation Vibration/shock
Repeatability		

Other characteristics also to be considered are operating life, storage life, power requirements, safety aspects, cost and availability, service and parts.

## 16.3 Transducer Characteristics

The **sensitivity** of a transducer is a measure of the magnitude of the output divided by the magnitude of the input. e.g.,  $mV/^{\circ}C$  for a thermocouple.

sensitivity =  $\frac{\text{output signal}}{\text{input signal}}$ 

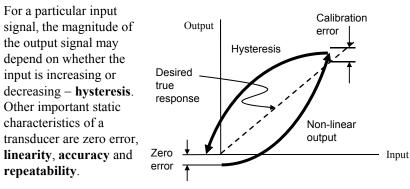
The output of most transducers is in the millivolt range for interfacing in a laboratory or light industrial applications. The proportion of wanted to unwanted signal is called the **signal-to-noise ratio** or SNR (usually expressed in decibels).

The higher the **SNR** the better. In electronic circuits, noise signals arise due to thermal random motion of electrons and is called white noise and appears at all frequencies.

$$SNR = 20\log_{10} \left| \frac{V_S}{V_n} \right|$$

The least detectable input is often referred to as the **noise floor** of the instrument. The magnitude of the noise floor may be limited by the transducer itself or the effect of the operating environment. It is often the noise floor of an instrument that determines its suitability for an application, not the theoretical **resolution**.

A continuous increase in the physical input sometimes results in a series of discrete steps in the output signal due to the nature of the transducer. The **resolution** of a transducer is defined as the size of the step  $\delta O$  divided by the **full scale deflection (fsd)** and is given in %.



## 16.4 Transducer Dynamic Response

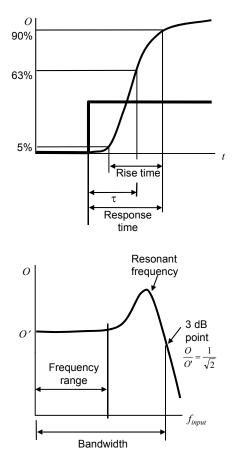
#### The dynamic response

determines the ability for the output to respond to changes at the input. Usually, a step input voltage is applied and the following characteristics are measured:

- Rise time
- Response time
- Time constant τ

The resulting output signal may be designed to be over-(slow rise), critically damped (fastest rise possible without ringing), or under-damped (some ringing or oscillation before settling down).

When the input is a regular time-varying signal such as a sine wave, then the output may depend upon the frequency range of the input, especially when this frequency is near the **resonant frequency** of the system.



## 16.5 Noise

**Thermal noise** and **shot noise** are present in electrical signals at all frequencies and are collectively called **white noise**.

Thermal noise (often called Johnson or Nyquist noise)

$$V_{nrms} = [4kTR\Delta f]^{\frac{1}{2}}$$
Noise power  $V_n^2 = 4kTR\Delta f$   
 $P = \frac{V^2}{R}$   
 $= 4kT\Delta f$   
 $= 4kT\Delta f$   
 $e.g., 10k resistor at 300 K over a bandwidth of 10 kHz gives an rms noise figure of 1.3  $\mu$ V$ 

**Shot noise** is associated with the randomness of charges moving across a potential barrier, such as soldered contacts in a circuit.

	$i_n^2 = 2eI_s \Delta f$	k	Boltzmann's constant $1.38\times 10^{-23}$ J/K
Noise power	$P_n = i_n^2 R$	Т	absolute temperature
		R	resistance
	$= 2\Delta fei_n R$	$\Delta f$	bandwidth
		е	charge on electron $1.6 \times 10^{-19} \text{C}$
		$I_s$	DC signal current (A)
		i <sub>n</sub>	noise current (A)

Note that the **noise power** is proportional to T and  $\Delta f$  and so may be reduced often by reducing the bandwidth and/or the temperature.

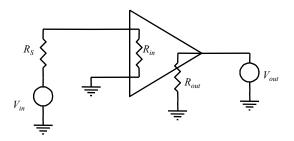
**Flicker noise** increases with decreasing frequency and is sometimes called 1/f noise. For this reason, sensitive measurements should not be made using DC. The precise origin of flicker noise is not well understood. It is usually insignificant compared to other noise above 1 kHz.

Environmental noise arises from sources outside the measuring system and is termed **interference**. Interference may be mechanical in nature (from mechanical **vibrations**) or electrical. Electromagnetic interference (**EMI**) is the most common and is usually legislated against in electrical standards as a safety issue.

The introduction of noise into the measurement system usually occurs at the first stage of amplification. For this reason, a **preamplifier** should be located as close to the transducer as possible. The preamplifier should be a differential amplifier with a good CMRR. All shields should be grounded at a common point so as to eliminate **ground loops**.

## 16.6 Transfer Function

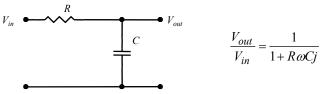
One of the most important issues in taking a signal from a transducer and then amplifying and recording it is **impedance matching**.



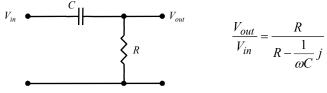
Ideally,  $R_{in} >> R_s$  since we want most of the variations in signal to appear across the input resistance of the amplifier, not across the internal resistance of the transducer. Similarly, a low amplifier output resistance ensures the most efficient transfer of signal to the output device.

The mathematical expression for the relationship between the input and the output signals is called the **transfer function**.

For a simple *RC* first-order **low-pass filter**, or integrator, the transfer function is expressed:

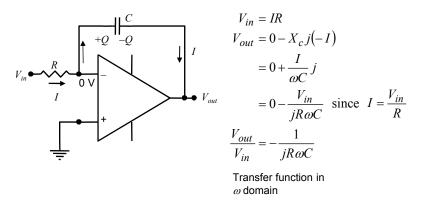


The transfer function for a simple *RC* first-order **high-pass filter**, or differentiator, is:



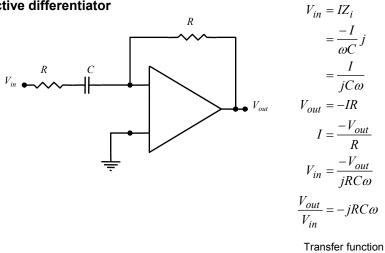
## 16.7 Integrator/Differentiator

## Active integrator



It is usual to connect a feedback resistor in parallel with C to reduce DC drift.

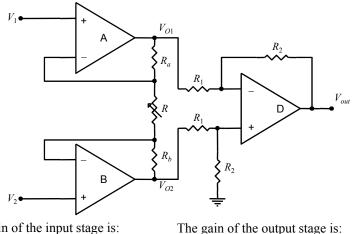
### Active differentiator



in  $\omega$  domain

## 16.8 Amplification

An instrumentation amplifier has a high gain and high CMRR. It is formed by using cross-coupled inputs for high CMRR and high input impedance.



The gain of the input stage is:

$$\frac{V_{o1} - V_{o2}}{V_1 - V_2} = \frac{\left(R_a + R_b + R\right)}{R}$$

 $A_d = \frac{R_2}{R_1}$ 

)

Thus the total gain is:

$$A_{v} = -\left(\frac{2R_{a}}{R} + 1\right)\frac{R_{2}}{R_{1}}$$
  
And so:  $V_{out} = -\left(\frac{2R_{a}}{R} + 1\right)\frac{R_{2}}{R_{1}}\left(V_{1} - V_{2}\right)$ 

Advantages:

- Both inputs have a high input impedance.
- The gain of the amplifier can be easily adjusted via R.

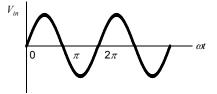
The resistors  $R_1$  at the input to the output differential amplifier are trimmed to eliminate amplification of any common mode signal. It is usual to use the gain of the input stage to be the overall gain of the amplifier while the output stage is set to unity gain:  $R_2/R_1 = 1$ . The purpose of the output stage difference amplifier D is to simply reject any common mode signal.

## 16.9 Sampling

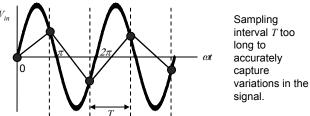
Interfacing to a computer is the process whereby the analog electrical signal from a transducer is digitised by an **analog to digital converter** (**ADC**) and then stored in computer memory.

The ADC can be located either near the transducer, or, as is more common, on a special purpose interface card installed inside the computer. The interface card interfaces directly to memory either by direct memory access (DMA) or as a memory-mapped driver.

The first task to be performed in an analog to digital conversion is to sample the input. The input is usually a smoothly varying signal. In the simplest case, it might be a sine wave:



The input signal needs to be sampled at sufficiently small time intervals, so that the sampling is fine enough to capture the desired level of detail in the signal.



The smaller the interval, the more accurate the representation of the original signal when we come to reconstruct it from the data. In the above example, the sampling interval is too large in comparison with the time-varying nature of the signal.

The **Nyquist criterion** states that the sampling rate (samples per second) should be greater than twice the highest frequency component (cycles per second) of the signal.

## 16.10 Digital Resolution

When analog data is to be stored in a digital system, the analog signal (usually voltage) is sampled at regular intervals, and then these samples have to be represented by a digital number. For example, for an 8-bit conversion from analog to digital, the magnitude of the full range of the original analog data would be between the binary numbers 00000000 and 11111111 (or 0 and 255 in decimal). Numbers that don't fit exactly within a "bin" are rounded up or down to the nearest one and then stored.

For example, if an ADC were able to accept input voltages from -10 to +10 volts, then full range, or 20 volts, at the input would correspond to the number 255 on the output. The resolution of the ADC would be:

$$\frac{20}{255} = 0.0784$$
 V

Thus, for an input range of -10 to +10 volts, the resolution of an 8-bit ADC would be 78.4 mV per bit.

In general, the **resolution** of an *N* bit ADC is:

$$\Delta = \frac{V_{ref}}{2^N}$$

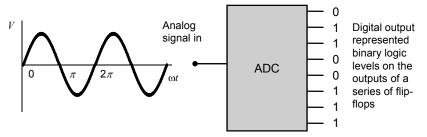
where  $V_{ref}$  is the range of input for the ADC in volts.

This rounding of the data introduces a **quantisation error**  $\Delta e$  and is  $\pm$  half a bit (i.e., the **least significant bit** or **LSB**). For a full scale of 0 to  $V_{ref}$  volts, the error for an N bit digitisation is thus:

$$\Delta e = \frac{V_{ref}}{2(2^N)}$$

## 16.11 Analog to Digital Conversion

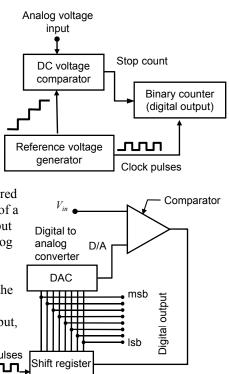
An **analog to digital converter** samples an input voltage and produces a binary integer on its output whose value is proportional to the magnitude of the input voltage. A single conversion usually takes a few milliseconds.



In the **staircase method** (or **integrating method**), conversions are performed by comparing the unknown input signal voltage to an internal **reference voltage**.

The reference voltage is linearly increased in small steps until it equals or exceeds the signal voltage and a digital counter is used to record the number of voltage steps tested during the conversion time. The digital count is thus an indication of the magnitude of the voltage input.

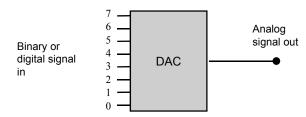
In the successive approximation method, the input voltage is compared (using a comparator) to the output of a digital to analog converter. The input signal is compared against the analog output of the DAC, which is set, starting with the MSB = 1 and the remaining bits 0 (i.e., half way up the scale0 and progressively lowered. When  $V_{in}$  falls below the DAC output, the bit pattern on the DAC is the conversion value. Clock pulses



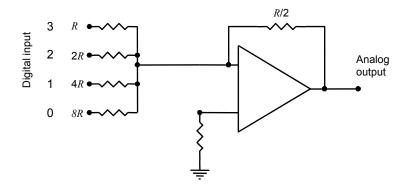
## 16.12 Digital to Analog Conversion

Interfacing often involves the control of analog physical systems, such as servo-motors and actuators, based upon a digital input. A common example is the conversion of digitally stored music to analog sound in a speaker.

This conversion is accomplished by a digital to analog converter or DAC.



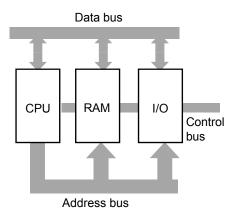
In the DAC, a summing amplifier is used to create the analog signal from the magnitude of the digital input. Each digital input is a TTL logic level. The logic level connected to the lowest value weighting resistor has the greatest influence on the magnitude of the output. Thus, the larger the magnitude of the digital input, the larger the magnitude of the analog output. This arrangement of resistors is often called a ladder network.



## 16.13 Computer Architecture

The analog to digital conversion is usually performed by a dedicated circuit positioned either external or internal to the **computer**. The final output of the conversion, in digital form, has to be then captured and stored in computer memory for eventual further processing, display and disk storage if required.

A computer has a very well organised architecture: comprising a central processing unit (**CPU**), memory (**RAM**) and an input/output system. These components are connected by parallel wires (on a printed circuit board) called a **bus**.



Each memory location is capable of holding 8 bits, or 1 byte, of data and is physically constructed using flip-flops. Each memory location has a unique **address**. The maximum addressable memory depends upon the width of the address **bus**. A bus is a parallel series of wires that carries digital signals. Early personal computers had a 16-bit address bus which gave 640 KB of addressable memory, or **RAM**.

The **data bus** is **bi-directional** and transfers data in both byte and word length to and from the CPU and memory. Early computers had an 8-bit data bus.

The **control bus** carries various synchronisation and control signals such as the **read/write** signal. During a read cycle, the processor receives data from either memory or a memory-mapped peripheral device. During a write cycle, the processor sends data to either a memory location or a **memory-mapped** device.

The physical process of transferring digital TTL voltage levels onto the various buses is quite complicated and very ingenious. Individual memory locations are isolated from the data bus by **buffers**. **Decoding** circuitry that reads the address bus determines the actual buffer to be activated. The data is then passed through the buffer to a **latch**, or **flip-flop**. All this takes place in a sequence determined by the **CPU clock**, which typically runs at GHz speeds.

## 16.14 Ports

The path from transducer to computer generally takes place via hardware connections called **ports**. A port has the job of managing various issues connected with external devices such as:

- incompatible voltage levels
- changing current levels
- electrical isolation
- timing of data transfers

As well as the above, there are further problems with servicing priorities, different speeds (e.g., hand keyboard press compared to ADC data transfer).

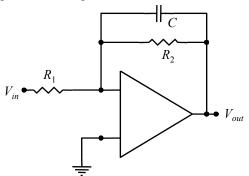
A **port** is a connection from the outside world to the microprocessor architecture. A **input port** transfers information from the outside world to the microprocessor. An **output port** provides signals to the outside world from the microprocessor.

Each port has a unique address and is connected to the address bus and the data bus. From the CPU point of view, a port is very much like a memory location. Ports generally require servicing. That is, data to and from the port has to be collected or sent when appropriate. There are three main methods of accomplishing this:

Polling	The CPU continually and sequentially interrogates each device. If a device requires servicing, then the request (or bus access) is granted. If the device does not require servicing, then the CPU interrogates the next device. This is simple, but CPU intensive since the processor must spend a large amount of time interrogating devices which do not require servicing.
Interrupts	The device raises a flag which is recognised by the CPU to stop whatever is currently underway, and service the port. Interrupts are controlled by a dedicated <b>programmable interrupt</b> <b>controller.</b> The <b>IRQ</b> allocation is a <b>hardware device interrupt</b> <b>number</b> and is used to conveniently prioritise different devices. The lower the IRQ, the higher the priority.
Direct memory access (DMA)	Data is transferred directly between memory and the I/O port. DMA requires full control of the address, data and control buses. When a DMA transfer is to occur, a <b>DMA controller</b> requests control of the bus from the CPU. The CPU grants control and suspends any bus-related activity of its own. The DMA controller then transfers data from port to memory, or memory to port directly, without any CPU overhead.

## 16.15 Review Questions

- 1. Calculate (a) the open-circuit rms noise voltage over the frequency range 0 1 MHz between the terminals of a 100 k $\Omega$  resistor at a temperature of 27 °C and (b) the available noise power from this resistor.
  - (Ans: 0.04 mV,  $4.14 \times 10^{-15}$  W)
- 2. With respect to the integrator circuit below:



- (a) What is the function of the feedback resistor  $R_2$ ?
- (b) Derive an expression for the transfer function and sketch the response for low frequency and high frequency.
- (c) Determine values of resistors and capacitors to give integration of signals above 50 Hz.
- 3. A 10-bit analog to digital converter accepts an input voltage from 0 to 5 V. Determine the resolution of the ADC. (Ans:  $4.88 \times 10^{-3}$  V)
- 4. The conversion of an analog signal to a digital output for a successive approximation ADC takes a fixed amount of time called the **conversion time**. If the analog input signal is changing during the conversion time, then the converted output will be in error by what is called the **aperture error**. Calculate the smallest increment of input signal  $\delta$  that can be registered by an 8-bit ADC as a fraction of the full scale input voltage.
  - (Ans: 0.00039)
- 5. The aperture time  $t_a$  is the largest time within which the conversion can take place before there is any aperture error. For a sinusoidal input of frequency *f*, it is given by:  $t_a = \frac{\delta}{2\pi f}$  (see answer to Q4)

Calculate the aperture time for a 100 Hz input signal to an 8-bit ADC.

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## 17. Laboratory

Experiment 1: Thevenin's theorem Experiment 2: AC circuits Experiment 3: Diode characteristics Experiment 4: Energy gap Experiment 5: Diode circuits Experiment 6: Clippers and clamps Experiment 7: Transistor characteristics Experiment 8: NiCad Battery charger Experiment 9: Transistor amplifier Experiment 10: Amplifier design Experiment 11: Impedance matching Experiment 12: Field Effect Transistor Experiment 13: Common source amplifier Experiment 14: Logic gates Experiment 15: Logic circuits Experiment 16: Counters and flip-flops Experiment 17: Op-amps Experiment 18: Comparator Experiment 19: Integrator

# Recommended parts required for laboratory experiments:

**Resistors:** (× 2 except where noted) 100, 220, 270, 390, 410, 470, 680, 1K, 1.2K, 1.5K, 2.2K, 2.7K, 3.3K, 3.6K, 4.7K, 6.8K, 10K, 20K, 28K, 36K, 47K, 100K, 270K, 470K, 680K, 1M, 2M decade resistance box × 1.

**Capacitors:** ( $\mu$ F, × 2 except where noted) 0.01, 0.82 × 1, 1.0, 4.7, 10, 47, 100 × 1, 1000 × 1

#### Inductors:

**33 mH** × 1

#### Semiconductor devices: (x 1 except where noted)

BC107 BJT × 3 2N5484 FET × 3 4.8 V 1N4732 Zener diode × 3 1N4002 diode × 6 Germanium diode 7400 NAND 7402 NOR 7408 AND 7404 INV 7432 OR 7476 JK flip flop 741 op-amp

#### Test equipment:

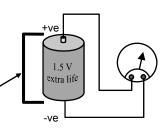
1.5 V dry cell
6 V dry cell
Dual output adjustable power supply ±15 V
Multimeter with mA range and diode test facility × 2
Signal generator 4 kHz
2 channel Oscilloscope
Bunsen burner
Beaker of water and tripod
Thermometer

#### 17.1 Thevenin's Theorem

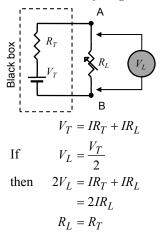
Try this simple experiment: Obtain an ordinary AA size 1.5 volt dry cell. Using a voltmeter, measure the voltage between the terminals. Now connect a piece of wire directly from one terminal to the other and measure the voltage between the terminals. Hopefully you will get about 1.5 V for the first measurement and 0 V for the second.

What has happened to the 1.5 V in the second measurement? Since there is no voltage at the output terminals, then all the voltage must be dropped across the internal resistance of the cell. If you can, measure the current that flows in the wire when it is connected between the terminals. This is called the "shortcircuit" current. The voltage measured when there is no wire connected is called the "open-circuit" voltage. According to Thevenin, any twoterminal output of a power supply circuit containing resistors and voltage sources can be simulated with just a single voltage source  $V_T$  and a single resistance  $R_T$ . The voltage  $V_T$  is usually measured by measuring the opencircuit output voltage  $V_{oc}$ . The resistance,  $R_T$ , is found by measuring the short-circuit current Isc and calculating:  $R_T = \frac{V_{oc}}{I_{sc}}$ 

But, it is not practical to measure short-circuit current in most cases since most equivalent resistances are low, making the short-circuit currents very high. That is, do NOT try measuring  $I_{sc}$  using a car battery.



The short-circuit current will be very high and the battery will explode. In practice, measuring short-circuit currents could lead to a risk of fire or injury. An alternative procedure is to connect a variable load resistor  $R_L$  to the output terminals and adjust it until the output voltage is equal to  $V_T/2$ . At this condition,  $R_T = R_L$ .

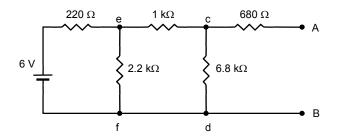


Even this procedure is not safe unless the source has a fairly high internal resistance. In the experiment to follow, we shall use a fairly safe 6 V dry cell power supply. Do not attempt measurements of this type unless you are certain that the currents obtained will not cause injury or damage.

#### **Pre-work**

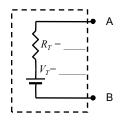
Imagine that you are an electrical engineer who has designed the following power supply circuit. When the circuit is used, various "load resistors" are to be connected to the output terminals. Now, to calculate the output terminal voltage and current through the load resistor would be a very tedious task if we had to solve the whole circuit each time we changed  $R_L$ ; thus, it is easier to find the Thevenin equivalent circuit ( $V_T$  and  $R_T$ ), and then solve a simple current loop for the output voltage and current no matter what value of  $R_L$  we might like to consider.

Calculate the numerical value of the Thevenin equivalent circuit ( $V_T = V_{AB}$  and  $R_T$ ) of the circuit below:



Hint: use a Kirchhoff's law approach by drawing in two current loops and recognising that  $V_{AB} = V_{cd}$  in the above diagram at open circuit.

Write your answers here:



#### Procedure

1. Construct the circuit shown previously but do not connect  $R_L$  (i.e., leave the output at open circuit). Measure the voltage  $V_{ab}$  with a voltmeter and record the value.

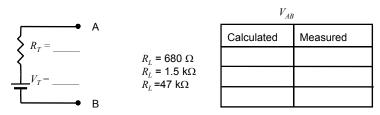


2. Disconnect the 6 V power supply leads from the circuit. Put a short circuit across the points in the circuit where the power supply used to be connected. Using an ohmmeter, measure and record the resistance between the output terminals AB. Remove the short circuit and reconnect the 6 V power supply.

Compare these measured values with those calculated on the previous page.



**3.** Using *measured* values for  $V_T$  and  $R_T$ , use a Thevenin equivalent circuit to calculate the voltage that will appear across  $R_L$  when  $R_L$  takes on the values shown:



Connect these resistors in turn to terminals A and B in the actual circuit and measure the voltage  $V_{AB}$ . Comment on any differences with calculated values.

4. Connect a decade box resistor as the load resistor in the above circuit. Adjust the decade box so that the voltage  $V_{AB}$  is one half of the open-circuit voltage. Compare the resistance of the decade box in this condition with the calculated equivalent Thevenin resistance. Make a brief comment about why you observe any correspondence between these two values of resistance.



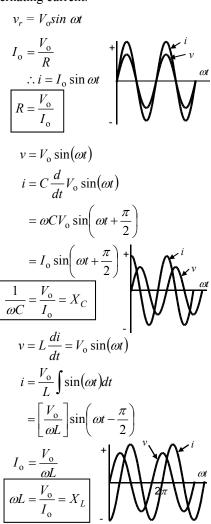
#### 17.2 AC Circuits

AC is alternating current, that is, the current in a conductor flows one way, then a very short time later, flows the other way. This transition in direction of flow happens very smoothly. In domestic power lines, the reversal in direction of current is 50 times per second. Here we will look carefully at exactly what AC is and how various components like resistors, capacitors and inductors can resist the flow of alternating current.

The voltage and current in an AC circuit usually varies sinusoidally. For a resistor,  $I_o$  and  $V_o$  are in phase and  $I_o$  is determined by the value of *R* just as in a DC circuit.

For a **capacitor**, the resistance to AC, and thus the magnitude of  $I_0$  for a given  $V_0$ , depends on the value of the capacitor *and* the frequency of the applied voltage. At high frequencies, the polarity of the voltage applied to the capacitor changes before the capacitor has had a chance to charge up; thus the current  $I_0$  is large. Thus, the reactance of a capacitor decreases with increasing frequency. Further, the maximum voltage occurs when the current is zero and decreasing; thus  $I_0$  leads  $V_0$  by  $+\pi/2$ .

For an **inductor**, the magnitude of  $I_0$  again depends on the frequency of  $V_0$ . For high frequencies, the magnitude of the induced back *emf* is large and this restricts the maximum current that can flow before the polarity of the voltage changes over. Thus, the reactance increases with increasing frequency. The maximum voltage occurs when the rate of change of current is a maximum and increasing, thus  $I_0$  lags  $V_0$  by  $\pi/2$ .

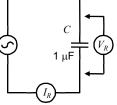


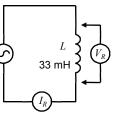
#### Procedure: Part A. Reactance

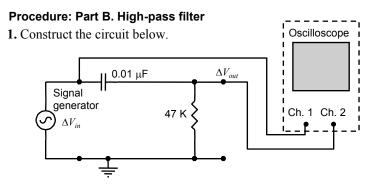
- 1. Construct the circuit shown. Set the function generator to 1 V peak-to-peak at a 500 Hz sine wave.
- 2. Set the multimeters to AC operation and measure the rms voltage across the  $270 \Omega$  resistor and also the rms current. Now adjust the amplitude of the sine wave to obtain 0.5 V rms on the voltmeter.
- **3.** Record values of rms voltage and current for each of the frequencies as shown in the table. **Keep the rms voltage at 0.5 V by adjusting the amplitude each time you change the frequency.**
- 4. Replace the resistor with a 1  $\mu$ F capacitor and measure rms voltage and current as a function of frequency. Keep rms voltage at 0.5 V at each frequency step. Record results in the table.
- **5.** Replace the capacitor with the inductor supplied and measure the rms voltage and current as a function of frequency as above. Record results in the table.
- 6. *Calculate* the resistance or reactance for each device at each frequency using the experimentally measured rms voltages and currents  $X_C = V_{rms}/I_{rms}$ .
- 7. Verify for one set of readings (say 500 Hz) that the value for reactance calculated using rms values corresponds to that using the formula on the previous page, i.e.,  $X_C = 1/\omega C$ ,  $X_L = \omega L$ .

$\frac{1}{Resistor}$			Capacitor			Inductor			
Frequency	V <sub>rms</sub>	I <sub>rms</sub>	R	V <sub>rms</sub>	I <sub>rms</sub>	$X_C$	V <sub>rms</sub>	I <sub>rms</sub>	$X_L$
100 Hz									
200									
300									
400									
500									
600									
700									
800									
900									

 $\begin{array}{c} R \\ 270 \Omega \\ \end{array}$ 





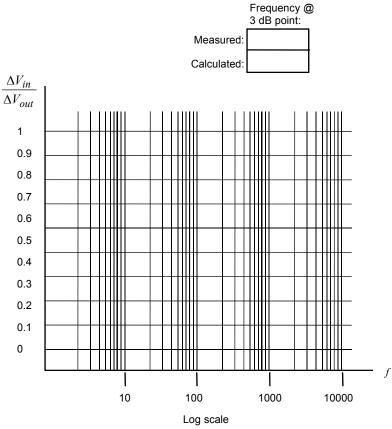


- 2. Set the signal generator output for  $\Delta V_{in}$  to be a sine wave, 1 V peak-topeak, at 50 Hz. If you have wired up the circuit correctly, the input signal will appear on Channel 1 of the CRO and the output signal on Channel 2.
- 3. Once you have got the CRO settings adjusted so that you can view both input and output signals, measure and record the peak-to-peak output voltage as a function of frequency (50, 100, 200, 300, 400, 500, 1000, 2000, 4000 Hz). Make sure that the input signal  $\Delta V_{in}$  is maintained at 1 V peak-to-peak. Adjust the amplitude of the signal generator if necessary. Enter the measured values of  $V_{out}$  in the table below.

	$\Delta V_{in} = $		
Freq. (Hz)	$\Delta V_{out}$ (Measured)	$\Delta V_{out}$ (Calc)	Calculations:
50			$\Delta V_{out}$ $R\omega C$
100			$\frac{\Delta V_{out}}{\Delta V_{in}} = \frac{R\omega C}{\sqrt{R^2 \omega^2 C^2 + 1}}$
200			Let $R\omega C = 1$
300			
400			$\frac{V_{out}}{V_{in}} = \frac{1}{\sqrt{2}}$
500			3 dB point (by
1000			definition)
2000			
4000			

- **4.** Using the nominal values of the components you are using, calculate values of output voltage for each of the frequencies used in the measurements with an input voltage of 1 V peak-to-peak.
- **5.** <u>Calculate</u> the 3 dB frequency for this circuit. Enter data in the table above and the 3 dB frequency in the box on the next page. Hint: examine calculations shown above to find  $\Delta V_{out}$  as a function of  $\Delta V_{in}$ , *R*, *C* and  $\omega$  and thus calculate  $\Delta V_{out}$  for each frequency step.

6. Plot a graph of  $\Delta V_{out} \Delta V_{in}$  as a function of frequency for both measured and calculated values (plot on the same graph) using log/linear graph paper. Determine the "measured" 3 dB point from the appropriate graph and enter in the table below.

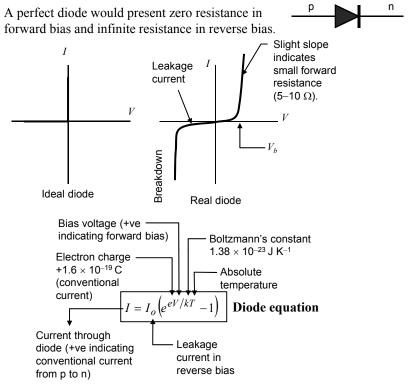


7. Comment on any features of interest in your graphs and on any differences you see between measured and expected values.

## 17.3 Diode Characteristics

Diodes were the first semiconductor electronic devices. A **crystal** in a crystal set radio is a diode. Diodes are used to convert AC signals to DC signals, protect electronic equipment from voltage fluctuations, provide stable DC voltage levels and many other functions. How can such a simple device accomplish so much?

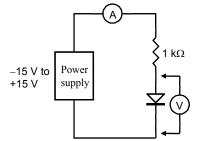
A p-n junction will conduct current in forward bias and act as an insulator in reverse bias. Such a process is called **rectification** and the device as a whole is called a **diode**.



There are different types of diodes. A **zener diode** is specially constructed so that it has a well-defined reverse bias breakdown voltage. The value of the breakdown voltage can be set during manufacture (where the forward bias voltage is fixed by the barrier potential of the semiconductor material). Zener diodes are usually connected in reverse bias and can be used to regulate voltage.

#### Procedure: Part A. Normal diode

**1.** Construct the circuit shown below using a normal diode. Use the bipolar adjustable supply from the laboratory power supply.



- 2. Adjust the power supply so that the diode is placed in reverse bias with a voltage of -6 V. Set the ammeter on the most sensitive scale (200  $\mu$ A).
- 3. Measure and record the current through the diode for voltages from -6 V to 0 V in 2 V steps. Be careful not to burn out the fuse on the ammeter adjust the voltage slowly.

V	I μA
-6	
-4	
-2	
0	

4. Change to a higher scale on the ammeter, say 200 mA. SLOWLY increase the voltage in 0.1 V steps up to a value of +0.5 V and then in 0.05 V steps to 0.8 V or a maximum of 15 mA.

**WARNING**: Do not run a large current (> 15 mA) through the diode. It will burn out.

V	Ι	V	Ι	V	Ι
+0.1		+0.5		+0.7	
+0.2		+0.55		+0.75	
+0.3		+0.6		+0.8	
+0.4		+0.65			

- 5. Plot a graph of current ( $\mu A$ ) versus voltage (-6 to 0).
- 6. Plot a graph of current (mA) versus voltage (0 to +0.8).
- 7. Determine as accurately as possible the leakage current in reverse bias.
- 8. Using the diode equation, plot on the same graph as above the expected characteristics of the diode.
- **9.** Comment on any other features you think are significant.

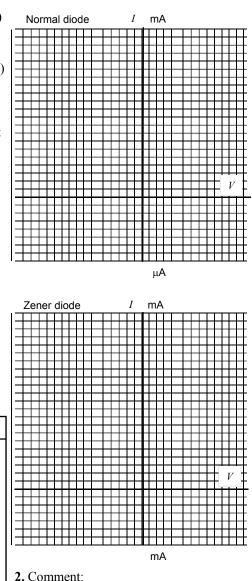
#### Part B. Zener diode

1. Determine the *I-V* characteristic for a zener diode using the voltage steps as suggested below.

Reverse bias

Forward bias

V	<i>I</i> mA	V	<i>I</i> mA
0		-0.5	
0.1		-1.0	
0.2		-1.5	
0.3		-2	
0.4		-2.4	
0.5		-2.6	
0.6		-2.8	
0.7		-3	
0.75		-3.2	
		-3.4	
		-3.6	
		-3.8	

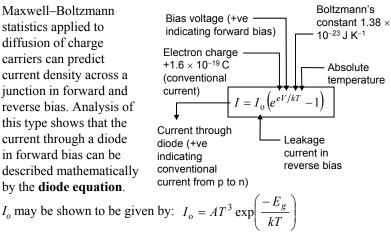


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## 17.4 Energy Gap

In this experiment, you will determine the energy gap in germanium and silicon by investigating the temperature dependence of the electrical conductivity of a forward biased p-n junction.

Maxwell–Boltzmann statistics applied to diffusion of charge carriers can predict current density across a junction in forward and reverse bias. Analysis of this type shows that the current through a diode in forward bias can be described mathematically by the diode equation.



where A is a constant and  $E_{\alpha}$  is the energy gap of the material.

Combining this with the diode equation gives:

$$V = \frac{E_g}{e} + \frac{k}{e} \ln\left(\frac{I}{A}\right)T - \frac{3kT}{e}\ln T$$

which may be re-arranged to give the following linear form:

$$V + \frac{3kT}{e} \ln T = E'_g + \frac{k}{e} \ln \left(\frac{I}{A}\right) T$$

where the energy gap is expressed in electronvolts.

#### Procedure:

- 1. Connect the germanium diode to the digital voltmeter and turn the voltmeter to the diode setting. This setting is indicated on the meter by the diode symbol. (See note below.)
- 2. Place the germanium diode adjacent to a thermometer bulb. Place both the diode and the thermometer into a beaker of water. Make measurements of the temperature of the water and the voltage across the diode between 0 °C and 100 °C. Stirring the water will help to assure uniform temperatures throughout.
- 3. Repeat the above procedure using a silicon diode.

**4.** Plot a graph of 
$$V + \frac{3kT}{e} \ln T$$
 on the y axis against T (in K) on the x axis.  
You should obtain a straight line whose intercept is the energy gap  $E_g$  (in eV).

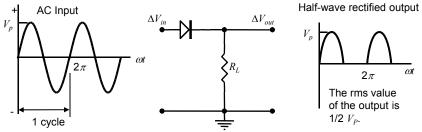
- 5. Answer the following questions:
  - (a) What are the accepted values for  $E_g$  for germanium and silicon? Calculate the percentage difference between the values of  $E_g$  you obtained and the accepted values.
  - (b) Show clearly the algebraic steps necessary to obtain the linearised form of the equation given in the box on the previous page.
  - (c) From the gradient of the graphs find *A* for the germanium and silicon diodes.
  - (d) Is  $E_g$  temperature dependent?
  - (e) What are the major sources of error involved in the experiment? and how may these errors be minimised?

**Caution:** The diodes should be **forward biased** during this experiment. This can be done by making sure that the black plug connected to the diode is inserted into the "common" (or com) socket of the meter and the red plug is inserted into the volts socket of the meter. When the meter is on the diode setting, the voltage appearing on the meter should be between 0.2 and 0.5 V.

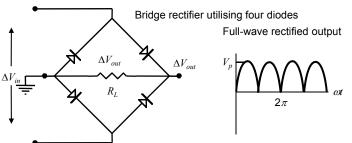
#### 17.5 Diode Circuits

Your portable radio/CD player operates off batteries, right? But, you can also run it off the power point at home to save batteries if you wish. How can this be? Batteries provide DC but the power point is 240 V AC. The answer of course is that the AC is converted into DC either inside the machine or in an external **battery saver** which uses diodes.

The conversion of AC voltage to DC voltage is called **rectification**. Most portable equipment uses low voltage DC. A transformer may be used to produce low voltage AC from the 240 V AC mains, but this then has to be rectified to obtain a steady DC output. Simple rectification can be had with just a single diode.



Although we have obtained a positive going output, it is by no means a very steady one. A better output can be obtained with a "bridge" rectifier and offers "full-wave" rectification. Full-wave rectification involves a clever arrangement of 4 diodes to produce a DC signal but with a large ripple.

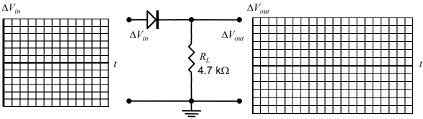


Although we still have a fairly non-steady output, it is a vast improvement on the half-wave design and may be easily modified to give a smooth DC output voltage.

Rectification involves the use of diodes connected in forward bias. But, you say, what about **zener diodes**? They break down at fairly low reverse bias voltages. What can they be used for? Zeners are used for voltage regulation, and we will look at this application of diodes later in this experiment.

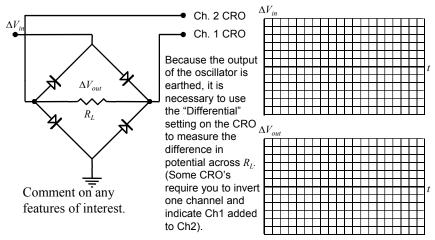
#### Procedure: Part A. Voltage rectification

1. Construct the circuit shown below using normal diodes. Adjust the signal generator to give a 5 volt peak-to-peak sine wave output at a "reasonable" frequency. Attach the oscilloscope probes so that the input and output signals can be displayed on the monitor simultaneously.



Sketch the wave forms and comment on any features of interest.

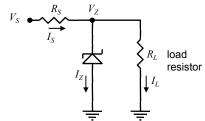
2. Now construct a full-wave rectifier circuit using the 4.7 k $\Omega$  load resistor. Apply the 5 V peak-to-peak signal from the signal generator and sketch the wave forms.



**3.** Modify the circuit by adding components where you think necessary to obtain a steady DC voltage across  $R_L$ . Describe what you think is happening and the significance of the value of the component(s) you used to smooth this output.

#### Procedure: Part B. Voltage regulation (zener diode)

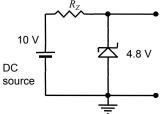
Zener diodes find special application as voltage regulators. They have a very sharp reverse bias breakdown characteristic. In a voltage regulator, the supply voltage can change significantly but the zener diode voltage  $V_Z$  does not change.



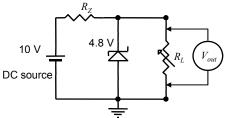
 $V_L = V_Z$  and  $I_S$  is thus fixed and independent of  $R_L$ . If  $R_L$  increases, the zener diode passes more current to keep  $V_L = V_Z$ . When  $R_L$  is infinite,  $I_Z = I_S$ .

But, useful as they are, the diodes are only capable of passing a certain maximum amount of current before they overheat. Thus, we need to have a current-limiting resistor in series with the device to limit the maximum current (and hence power dissipation) in the device.

1. For the circuit shown below, calculate the value of a current-limiting resistor  $R_Z$  required so that the power dissipated by the 4.8 V zener diode does not exceed 25 mW.



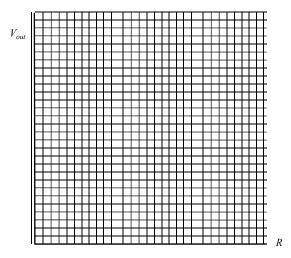
2. Construct the circuit and attach a decade resistance box as a variable load resistor  $R_{I}$ .



**3.** Starting from 10 k $\Omega$ , decrease the value of  $R_L$  in appropriate steps until the voltage  $V_{out}$  drops to about 70% of its original value. Record your readings in the table.

Resistance	V <sub>out</sub>	Resistance	V <sub>out</sub>

4. Plot this data and comment on the significance of your findings.



#### 17. Laboratory

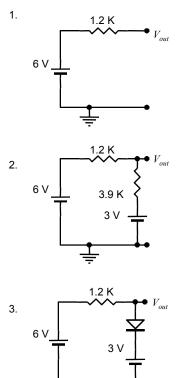
## 17.6 Clipper and Clamps

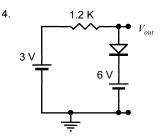
Ever heard a **Geiger counter** click? Ever wondered how your computer can obtain a stable voltage for the internal circuitry from the mains supply which varies according to what appliances are operating nearby? These are examples of simple diode circuits in action.

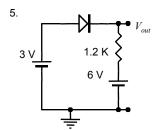
In order to protect sensitive circuitry from high voltages, it is usual to incorporate diode **clippers** into circuits. In this lab we will build a clipper and measure its characteristics. We will also build another very useful circuit, the diode **clamp**, in which a DC level shift can be applied to a signal.

#### Pre-work

Inspect the following circuits 1 to 5 and calculate the expected output voltage of each.



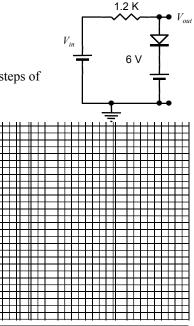




## Procedure: Part A. Clipper

- 1. Construct the circuit shown.
- 2. Increase  $V_{in}$  from -14 V to +14 V in steps of 2 volts and measure  $V_{out}$  at each step.
- **3.** Plot a graph of  $V_{out}$  versus  $V_{in}$ .

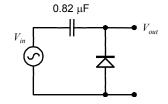
V <sub>in</sub>	V <sub>out</sub>	V <sub>in</sub>	V <sub>out</sub>



- 4. How would you modify the circuit so that V<sub>out</sub> clipped at 2 V?
- 5. Do that modification and check whether clipping does occur at 2 V.
- 6. Replace the DC power supply labelled  $V_{in}$  in this circuit with an oscillator. Set to sinusoidal output with  $\Delta V_{in}$  at 10 V peak-to-peak (use oscilloscope to measure  $\Delta V_{in}$ ). Sketch the output waveform.
- 7. Repeat step 5 with  $\Delta V_{in}$  at 20 V peak-to-peak. Sketch the output waveform.

#### Procedure: Part B. Clamp

- 1. Construct the circuit shown.
- 2. Set  $V_{in}$  to 10 V peak-to-peak and show  $V_{in}$  and  $V_{out}$  on an oscilloscope.
- **3.** Sketch the waveform that results.
- 4. Explain any differences you observe between  $V_{in}$  and  $V_{out}$ .



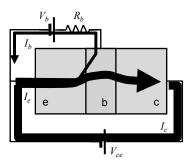
#### 17. Laboratory

#### 17.7 Transistor Characteristics

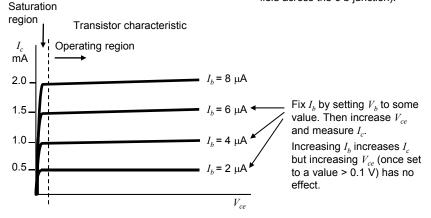
The transfer resistor, or **transistor**, was invented in 1947 by scientists working at the Bell Telephone Laboratories in the United States. It revolutionised the field of electronics since it allowed amplification of electrical signals to take place using a small, low power, robust device which eliminated the need for bulky, fragile vacuum tubes. In this experiment, we examine the electrical characteristics of a common npn silicon transistor which can be purchased for about 50 cents.

How does it work?

- 1. Base-emitter junction is a forwardbiased p-n junction so when  $V_{be} > 0.7$  V, the junction becomes conducting (just like a diode).
- 2. Electrons coming from the heavily doped emitter cross junction but before they have a chance to combine with holes in the p-type base and travel to the  $V_b$  positive terminal, they get swept up by the strong field which exists around the collector base junction which is reverse biased.
- Hence, only a few electrons go towards +ve V<sub>b</sub> and most are attracted across the collector base junction and cause a large current in the collector.

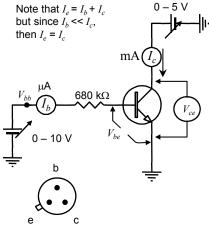


The base is made lightly doped (so that recombination in the base is unlikely to occur) and is purposely made very thin (so that electrons coming across the forwardbiased b-e junction do not have far to go before they "overshoot" and fall into the field across the c-b junction).

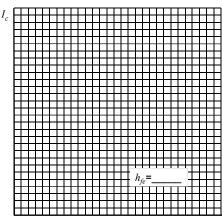


#### Procedure:

- 1. Construct the circuit shown using two independent power supplies so that  $V_{ce}$  and  $I_b$  can be controlled independently. Adjust  $I_b$  to 2  $\mu$ A and record values for  $I_c$  at  $V_{ce} = 15$  V, 10 V, 5 V, 2 V, 1 V, 0.5 V and 0.1 V.
- 2. Repeat these measurements for  $I_b = 4 \mu A$ ,  $6 \mu A$ ,  $8 \mu A$  and  $10 \mu A$  and record results in a table.
- 3. Construct a plot (below) showing the transfer characteristic at  $V_{ce} = 5$  V and determine the current gain  $(h_{fe})$ .
- Draw a graph of *I<sub>c</sub>* vs *V<sub>ce</sub>* for different values of *I<sub>b</sub>* and identify the operating and saturation regions (next page).

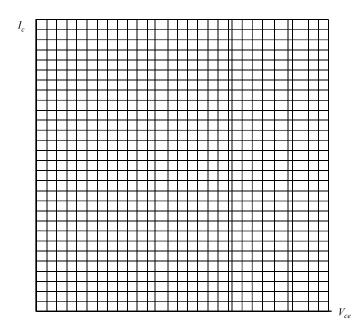






V <sub>ce</sub>	<i>I<sub>b</sub></i> = 2	4	6	8	10 µA
15					
10					
5					
2					
1					
0.5					
0.1					

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**5.** Comment on any features of the above transistor characteristic that you think are significant.

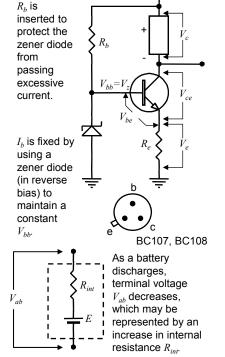
6. Examine the effect of reducing  $V_{ce}$  down to zero volts on the base current. That is, what value of  $I_b$  do you obtain when  $V_{ce} = 0$ ? Can you explain your reading?

# 17.8 NiCad Battery Charger

Rechargeable batteries are widely used in portable equipment. The most popular type are NiCad cells. The best operating conditions for NiCad batteries are regular use. However, NiCad batteries, unlike lead-acid batteries, can only be charged in a "short" time (usually about 15 hours) using a **constant current**. After the specified charge time, the charging current must be turned off. The constant current characteristics of a transistor can be used to make a NiCad battery charger.

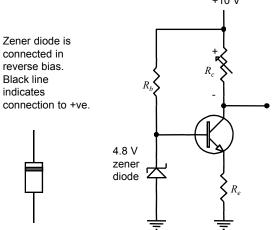
How does it work? Consider the circuit shown at the right:

- 1. The battery to be charged is placed in the circuit in lieu of  $R_c$ .
- 2. The charging current is set by the value of the zener diode to some "design value," say 10 mA.
- 3. When a "flat" battery is first inserted, its internal resistance is high (same as a high  $R_c$ ) and thus the "charging" voltage  $V_c$  is high and  $V_{ce}$  is low to maintain constant  $I_c$ .
- 4. As battery terminal voltage increases (i.e., decreasing " $R_c$ ") charging voltage decreases and  $V_{cc}$  increases.
- 5. When battery terminal voltage reaches a maximum, i.e., fully charged ( $R_{int}$  levels off to some "low" value),  $V_c$  is low and  $V_{ce}$  is high.



Throughout this process, and even when the battery is fully charged,  $I_c$  is still flowing so another circuit must switch off after a specified time period. However, having  $I_c$  a constant during charging ensures that the battery is charged at the maximum rate and to full capacity. Some NiCad battery chargers do not use a constant current source but supply a "trickle" charge. Trickle chargers can be left on for days without harm to the cells, but the cells would take 2 or 3 days to reach full charge from a completely discharged condition.

1. Calculate the values of  $R_e$  and  $R_b$  required for a constant current of  $I_c = 10$  mA using a supply voltage of 10 V and a 4.8 V zener diode. The zener diode is to pass a current of no more than 20 mA. Show all calculations. +10 V



Hint:  $I_b$  is very much smaller than the current through the zener.

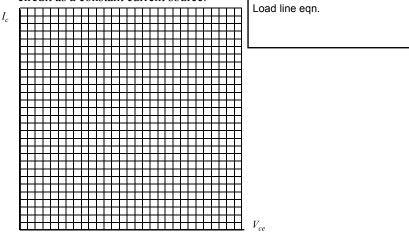
2. Construct the circuit and measure the current  $I_c$  with the "load" resistance  $R_c$  set to 0  $\Omega$ . Make sure the ammeter is connected between  $V_{cc}$  and the collector. Do not connect the ammeter between the emitter and  $R_e$  or between  $R_e$  to ground.  $I_c$  should be approximately 10 mA. Seek help if this is not the case.

Measured value  $I_c$  at  $R_c = 0$ :

**3.** Using the decade box as a load resistor, record the current  $I_c$  starting from about 10 k $\Omega$  (or higher if possible) decreasing to 0  $\Omega$  in steps of about 500  $\Omega$  initially but decreasing the step size near where the current  $I_c$  begins to stabilise. Measure the value of  $V_{ce}$  at which the charging current  $I_c$  becomes fairly constant (should be approx 10 mA).

R <sub>c</sub>	$I_c$	R <sub>c</sub>	$I_c$	$R_c$	$I_c$

- 4. Write down an equation for the load line for this circuit.
- 5. Determine the x and y axes intercepts for selected load lines from your data (i.e., different values of  $R_c$ ) and indicate on a graph of  $I_c$  vs  $V_{ce}$  these load lines. Make sure you include some load lines which correspond to *the beginning* of a fall-off in collector current.
- 6. Comment on why there is this fall-off in  $I_c$  and the usefulness of the circuit as a constant current source.



7. In the analysis of this circuit, it was assumed that the base current was always much less than the collector current. However, this is an unusual circuit due to the inclusion of the resistor at the emitter together with the zener diode at the base. These two conditions impose a "feedback" effect on the circuit, the effect of which may be demonstrated by removing  $R_c$  from the circuit (or making it a very high value) and measuring either the base or the emitter current. Measure the emitter current at a high value of  $R_c$  (or simply remove it from the circuit and leave the collector at open circuit).

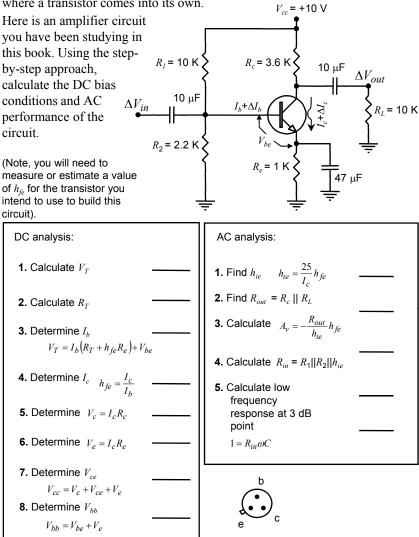
Your observation:

8. In the light of the above observation, it is evident that the base current does play an important role at very low values of  $I_c$ . With this in mind, examine the circuit again, and this time, develop a more accurate expression for the load line which includes the base current in the expression.

**9.** What does this mean about the slope and intercepts of the load line for this circuit when the transistor is saturated?

## 17.9 Transistor Amplifier

The transistor can be used as a switch, a source of constant current, and to amplify small signals. Ever tried connecting your headphones directly to the "line out" of your tuner or CD deck? You won't get much volume. The signal has to be amplified before it is large enough to drive a loudspeaker and this is where a transistor comes into its own.



1. Construct the circuit using a 10 k $\Omega$  resistor as  $R_L$  and measure the DC bias conditions ( $V_c$ ,  $V_{ce}$ ,  $V_e$ ,  $V_{bb}$ ,  $I_c$  and  $I_b$ ) and AC voltage gain  $A_v$  and enter measured values in the table. Summarise your readings and calculations in the table below and thus comment on any discrepancies you encounter.

	Calculated	Measured
$V_{cc}$ $I_b$		
$I_b$		
$I_c$		
$V_c$		
$V_e$		
$V_{ce}$		
$V_{bb}$ $A_y$		
$A_{v}$		

Note: do not measure the AC voltage gain at the 3 dB point frequency. Select a mid-range frequency and measure  $\Delta V_{in}$  and  $\Delta V_{out}$ . You decide a suitable input voltage  $\Delta V_{in}$ .

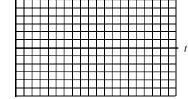


Comments & results:

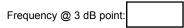


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2. Measure the frequency response of your circuit and check the 3 dB point. Do this by connecting channel 1 on the CRO to the input and channel 2 to the output. Decrease the frequency and note the frequency at which the signal on channel 2 becomes approx 70% of that of the mid-frequency response.



**3.** Remove the <u>bypass</u> capacitor and measure the AC voltage gain at a midrange frequency. Is this consistent with what you would calculate with no bypass capacitor?

With no bypass capacitor:

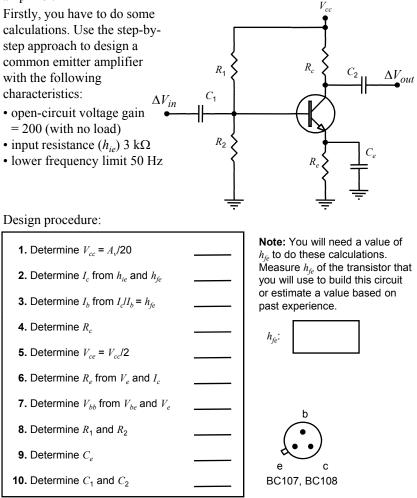
 $A_{v \text{ calculated}}$ :  $A_{v \text{ measured}}$ :

Comment on the effect of the bypass capacitor.

## 17. Laboratory

# 17.10 Amplifier Design

In the last experiment, you were given a circuit to build and analyse. How did the designer of the circuit know what values of resistances to use? How was the voltage gain decided? Here's your chance to design your own amplifier.



1. Construct the circuit and measure DC bias conditions, AC voltage gain and low frequency cut-off.

	Calculated	Measured
$V_{cc}$		
$I_b$		
$I_c$		
V <sub>c</sub>		
V <sub>ce</sub>		
V <sub>e</sub> V <sub>bb</sub> V <sub>be</sub>		
$V_{bb}$		
$V_{be}$		
$A_{\nu}$		

Resistors				
Used				

Capacitors

Calculated	Used
C <sub>1,2</sub>	
C <sub>e</sub>	

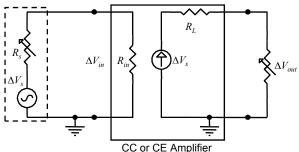
2. Examine the effects of increasing the input signal  $\Delta V_{in}$ . What is the maximum peak-to-peak input signal that may be tolerated before clipping appears on the output? Explain why this clipping occurs.

**3.** Examine the effect of heating the transistor on  $h_{fe}$ . Insert the transistor into the  $h_{fe}$  measurement instrument and measure  $h_{fe}$ . Then note any change in  $h_{fe}$  when touching (firmly) the case of the transistor. Is there any effect? Now insert the transistor into the amplifier circuit and determine whether there is any effect on the voltage gain of the circuit when the transistor is heated (use fingers again). Explain what you observe.

## 17. Laboratory

# 17.11 Impedance Matching

In previous experiments, you found that the voltage gain of a common emitter amplifier depended upon whether or not a "load" resistor (which might be, say, a loudspeaker) is connected at the output. To some extent, the voltage gain also depends on the internal resistance of the signal source. How can these effects be calculated and optimised?



The circuit shown above represents the equivalent circuit of an amplifier. The open-circuit gain is found from:  $A_{v} = \frac{\Delta V_{o}}{\Delta V_{i}}$ 

To measure the input and output resistances of the amplifier, the following approach is adopted:



BC107, BC108

## 1. Input resistance R<sub>in</sub>

With the output on open-circuit ( $R_L$  = infinity) and the variable resistance  $R_s = 0$ , measure the input voltage  $\Delta V_{in}$ . Gradually increase the variable resistance  $R_s$  until the value of  $\Delta V_{in}$  is halved. At this point,  $R_s = R_{in}$ .

# 2. Output resistance Rout

With the output on open-circuit ( $R_L$  = infinity) record the value of  $\Delta V_{out}$ and then decrease the value of  $R_L$  until the output voltage  $\Delta V_{out}$  is halved. At this point,  $R_L = R_{out}$ .

In this experiment, you will compare the input and output resistance and voltage gain of both common emitter and common collector circuits. The input and output resistances will be determined using the procedures 1 and 2 above for both circuits in turn. The calculated or expected values may be

found from:

For common emitter:  

$$h_{ie} = \frac{h_{fe} 25}{I_c}$$

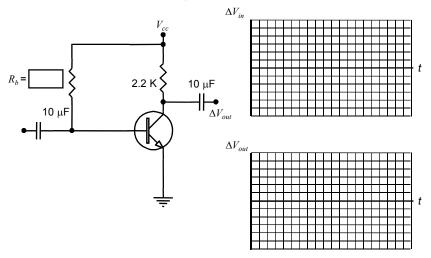
$$R_{out} = R_c ||R_L$$
For common collector:  

$$R_{in} = h_{ie} + h_{fe} R_e$$

$$R_{out} = \frac{R_s + h_{ie}}{h_{fe}}$$

#### Procedure: Part A. Common emitter circuit

1. Consider the circuit shown below. Assuming that  $V_{be} = 0.7$  and that  $V_{ce}$  is to be  $V_{cc}/2$ , determine an expression for  $R_b$  as a function of  $h_{fe}$ . Measure  $h_{fe}$  for the transistor that you will use in this laboratory session and thus calculate a suitable value of  $R_b$  to use in this experiment.

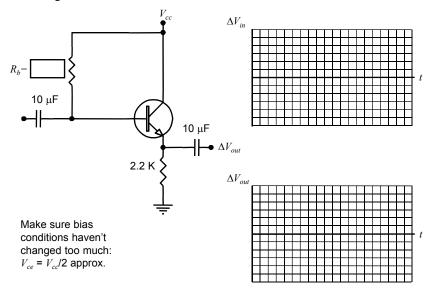


- 2. Construct the circuit and measure the open-circuit gain at 5 kHz using an input signal in the vicinity of 30 mV peak-to-peak with  $V_{cc} = +10$  V. Make sure that there is no saturation on the output (clipping).
- 3. Insert a variable resistor  $R_s$  between the signal generator and the amplifier input. Measure and record the input resistance using the method described on the previous page.
- 4. Disconnect the variable resistor from the input and connect it to the output terminal. Measure the output resistance of the amplifier using the method described on the previous page.  $R_{out}$
- Calculate the expected R<sub>in</sub> and R<sub>out</sub> and compare with experimental readings.
   Expected values:

R<sub>in</sub>

#### Procedure: Part B. Common collector circuit

1. Using the same components as above, construct a common collector configuration as shown:



- **2.** Using a 30 mV peak-to-peak input signal, measure the AC gain at  $V_{cc} = +10$
- **3.** Measure the input and output resistances of this circuit using the same method as used for the CE amplifier circuit.
- 4. Determine the expected values and compare with measured values.







5. Make a comment on the significance of  $R_{in}$  and  $R_{out}$  for the two circuits you have examined in this experiment.

# 17.12 FET

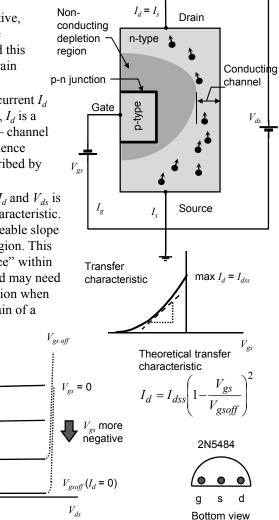
So far we have concentrated on the use of a **bipolar junction transistor** - a current-controlled device in which the collector current is controlled by the base current. Now we will have a look at a **field effect transistor** where the current is controlled by a voltage signal rather than a current. This leads to certain advantages when one requires a high impedance input.

How does it work?

As  $V_{gs}$  is made more negative, the channel narrows as the depletion layer widens and this constriction reduces the drain current  $I_d$ .

For a given  $V_{ds}$ , the drain current  $I_d$ depends on  $V_{gs}$ . At  $V_{gs} = 0$ ,  $I_d$  is a max (no depletion region – channel is widest). The correspondence between  $V_{gs}$  and  $I_d$  is described by the transfer characteristic.

The relationship between  $I_d$  and  $V_{ds}$  is shown on the transistor characteristic. For FET's, there is a noticeable slope in the normal operating region. This corresponds to a "resistance" within the conducting channel and may need to be taken into consideration when determining the voltage gain of a circuit employing an FET.



 $I_d$ 

mA

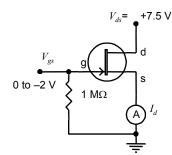
2.0

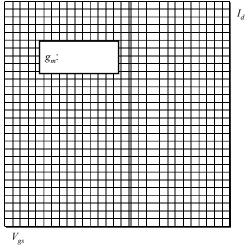
1.5

1.0 0.5

### Procedure: Part A. Transfer characteristic

- 1. Construct the circuit shown below (read the warning message below before applying power to circuit).
- 2. Measure the drain current  $I_d$  in mA as a function of the gate-source voltage  $V_{gs}$  from  $V_{gs} = 0$  V to -1.4 V in steps of -0.1 V (or until  $I_d < 0.1$  mA).
- **3.** Plot  $I_d$  against  $V_{gs}$  and identify the range in  $V_{gs}$  over which  $I_d$  is approximately linear.
- 4. Determine the mutual transconductance  $g_m$  in mS in the linear region of the characteristic.
- 5. Estimate values of  $V_{gsoff}$  and  $I_{dss}$  and plot the theoretical transfer characteristic.





**WARNING!** It is very easy to burn out the JFET in this experiment. DO NOT MAKE  $V_{es}$  +ve.

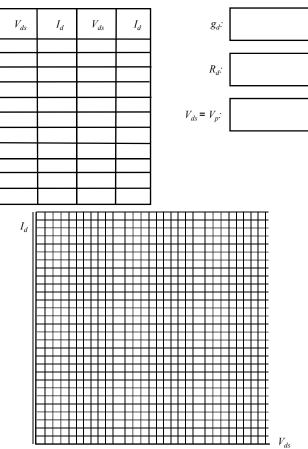
$V_{gs}$	$I_d$	$V_{gs}$	$I_d$

Questions:

- 1. Why is the drain current a maximum when  $V_{gs} = 0$ ?
- 2. Analysis of the theoretical transfer characteristic shows that  $g_m$  is a function of  $I_d$ . Does it matter which value of  $I_d$  is used to determine  $g_m$ ? Why?

#### Procedure: Part B. Drain conductance and pinch-off voltage

- 1. With the gate-source voltage  $V_{gs}$  set at approximately -0.3 V, measure and record the variation of  $I_d$  against  $V_{ds}$  from  $V_{ds} = 0$  V to 10 V. Use small steps in  $V_{ds}$  at low values for  $V_{ds}$ .
- 2. Plot these results and measure the drain conductance  $g_d = dI_d/dV_{ds}$  and the corresponding drain "resistance"  $R_d = dV_{ds}/dI_d$ .
- 3. At what value of  $V_{ds}$  does the normal operating region start (i.e., the pinch-off voltage)?
- 4. Compare this pinch-off voltage with  $V_{gsoff}$  from Part A and comment on what these two voltages actually signify.

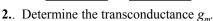


# 17.13 Common Source Amplifier

The extremely high input impedance of an FET makes it ideal for a **preamp**. That is, an amplifier which has a modest gain and whose output feeds into the input of a power amp.

We are going to design an amplifier with an AC gain of about 20 which can operate down to about 600 Hz. The circuit is shown at the right. When choosing the bias voltage  $V_{as}$ , we must ensure that it corresponds to the linear region of the characteristic curve; otherwise the output may become distorted.

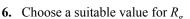
1. The transfer characteristic for the 2N5484 FET is shown at the right. Choose a region of the characteristic where the slope is approximately linear and estimate values of  $V_{gs}$  and  $I_d$  for a point in the centre of this "linear" region.



 $I_d$ :

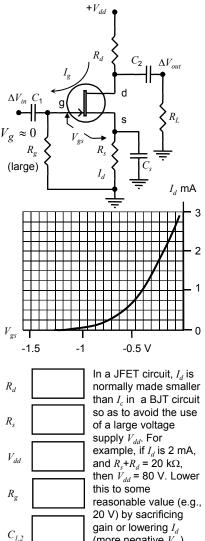
 $V_{gs}$ :

- **3.** Assume that  $g_d$  is very small, say 40 µS, and calculate a value for  $R_d$  using:  $R_d$  using: (use gain  $A_v = -20$   $A_v = -\frac{g_m R_d}{1 + g_d R_d}$ in this formula)
- 4. Calculate  $R_s$  from:  $R_s = \frac{-V_{gs}}{I}$ .
- 5. Let  $V_{ds} = V_{dd}/2$  and thus calculate  $V_{dd}$  from:  $\frac{V_{dd}}{2} = I_d R_d - V_{gs}$



7. Choose  $C_1$  and  $C_2$  so that  $R_g \omega C = 1$ and  $C_s$  so that  $1/\omega C_s \ll R_s$ 

 $C_{s}$ 

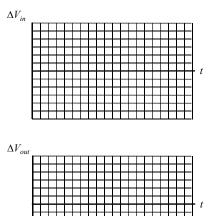


(more negative  $V_{os}$ ) and accepting more distortion.

 Construct the amplifier circuit and measure DC bias conditions, AC voltage gain and frequency response. Compare with calculated values. Comment on any interesting observations (such as phase differences, distortions, clipping, etc.).

	-	
	Calculated	Measured
$V_{gs}$		
$I_d$		
$R_g$		
$egin{array}{c} R_g \ V_{ds} \ R_d \ R_s \ V_{dd} \end{array}$		
$R_d$		
$R_s$		
$V_{dd}$		
$A_v$ $f_o$		
$f_o$		





Questions:

- 1. Did you have to recompute a value of  $V_{dd}$ ? If so, why did you select the value you did and what effect did this have on the expected voltage gain?
- **2.** Explain why the voltage measured from  $V_g$  to earth is about 0 V.

## 17. Laboratory

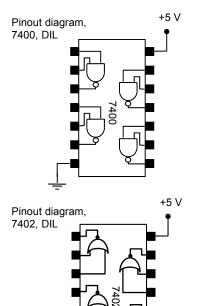
# 17.14 Logic Gates

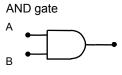
Basically there are two types of electrical signals: analogue and digital. The foundation of all digital circuits is the logic levels 0 and 1, represented electrically by voltage levels 0 V and 5 V (or sometimes 0 V and -5 V). In this experiment, we introduce some basic digital integrated circuits and how they might be used to construct a digital circuit.

**Logic gates** are used to represent logic elements of a logic circuit. A logic circuit employs **Boolean algebra** to implement the desired operation. The most useful Boolean expression is perhaps De Morgan's theorem:

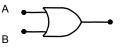
$$\overline{(A + B)} = \overline{A} \cdot \overline{B}$$
$$(A \cdot B) = \overline{A} + \overline{B}$$

Logic gates are usually supplied on an IC as a series of four on the one chip.









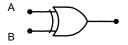




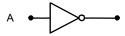




XOR gate



NOT gate



### Procedure: Part A. Logic gates

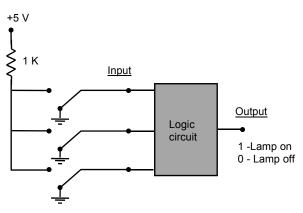
1. Using only 2-input NAND gates, construct a logic circuit that operates as a 2-input OR gate. (Use an LED in series with a 200  $\Omega$  resistor to indicate the output state of the circuit.)

Α	В	Out
0	0	
0	1	
1	0	
1	1	

**2.** Using only 2-input NOR gates, construct a circuit that operates as a 2-input NAND gate.

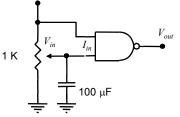
Α	В	Out
0	0	
0	1	
1	0	
1	1	

**3.** In the circuit below, the output controls a light which is to change state (off to on, or on to off) whenever any one of the three switches changes state. When all switches are earthed, the light is to be off. Construct a truth table for this operation and design and build a logic circuit using 2-or 3-input gates.



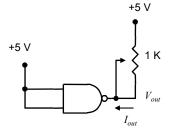
#### Procedure: Part B. Logic gate characteristics

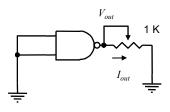
- **1.** Construct the circuit shown with a  $+5 \vee$  TTL NAND gate and set  $V_{in}$  to 0 V.
- 2. Gradually increase  $V_{in}$  until  $V_{out}$  goes low. Measure the input current  $I_{in}$  and the output voltage  $V_{out}$  and  $V_{in}$ .
- **3.** Repeat the above measurements with a CMOS NAND gate. Tabulate all results.



	V <sub>in</sub>	I <sub>in</sub>	Vout
TTL			
CMOS			

- 4. Now construct the circuit so as to measure the output voltage  $V_{out}$  and current  $I_{out}$  for both the TTL and CMOS gates as shown.
- 5. With both inputs at +5 V, determine the current in mA at which the output voltage is lifted above the maximum value for a low output (0.4 V).
- 6. With both inputs tied low (to 0 V), determine the output current in  $\mu$ A required to sustain the output high (> 2.4 V).
- 7. Compare your results to those which you would expect for each type of gate construction.





# 17.15 Logic Circuits

Logic circuits are an art. However, there is a systematic way in which a complicated logical function can be designed using the minimum of gates. In this experiment, we use the **Karnaugh mapping** technique to minimise a logic circuit.

1. Draw up a truth table and circle min terms.

Α	В	С	Out Min terms	Pin connections of some common logic gate chips.
0	0	0	$0  \overline{\overline{A}} \cdot \overline{\overline{B}} \cdot \overline{\overline{C}}$	
0	0	1	1 $\overline{A} \cdot \overline{B} \cdot C$	
0	1	0	$0  \overbrace{\overline{A} \cdot B \cdot \overline{C}}^{\bullet}$	
0	1	1	$1$ $\overline{A} \cdot B \cdot C$	
1	0	0	$0  A \cdot \overline{B} \cdot \overline{C}$	▏ <u>╃</u> Ѻ <sup>┉</sup> ┎╤ <u></u> ݠ╉ <sub>┙</sub> ╴ <sup>╸</sup> ╘ <u></u> ┢╉ <sub>┪</sub> ╜┍─╄
1	0	1	1 $\overline{\mathbf{A} \cdot \mathbf{B} \cdot \mathbf{C}}$	
1	1	0	$1$ $A \cdot B \cdot C$	
1	1	1	$1  A \cdot B \cdot C$	Þ

## 2. Construct map as follows:

	С	Ē
AB	1	1
ĀB	1	
ĀB	1	
AB	1	

In a Karnaugh map: Groups can only be of 1, 2, 4, 8, 16 etc. The larger the group, the better. Diagonal groups are not allowed. Groups can wrap around from edge to edge. The four corners can form one group. Don't care states are marked with an X and may be grouped if desired.

- (a) Arrange rows and columns with every combination of input, changing only one variable at a time.
- (b) Put 1's in boxes corresponding to circled min terms.
- (c) Draw boxes around groups of 1's. Boxes can only go vertically and horizontally. Boxes can also wrap around. Can only box even groups (powers of 2). Boxes of 3, 5 and 6, etc. are not permitted.
- (d) Group contents of boxes by ANDs and join together with Ors.

```
Output = A \not \!\!\! D C \ \overline{A} \not \!\!\! B C \ \overline{A} \overline{B} C \ \overline{A} \overline{B} C + AB \not \!\! C \ AB \not \!\! C
= C + A · B
```

1. A comparator tests the value of a pair of two-bit binary numbers A and B. It returns a logic 1 if A is greater than B and a low if otherwise. Complete the truth table for all possible values of A and B and the expected output  $Q_{exp}$ .

2. Construct a Karnaugh map from the truth table and derive a Boolean expression which implements the desired logic function of the comparator.

	B <sub>1</sub> B <sub>0</sub>	$\overline{B_1}B_0$	$\overline{B_1}\overline{B_0}$	$B_1\overline{B_0}$
$A_1A_0$				
$\overline{A}_1 A_0$				
$\overline{A}_1\overline{A}_0$				
$A_1\overline{A}_0$				

- **3.** Draw a logic diagram to produce the Boolean expression. You should be able to do this using 2 inverters, 4 AND gates and 4 OR gates.
- 4. Construct the circuit and test its operation using a resistor and an LED on the output. Enter the measured output  $Q_m$  in the table above.

CLK1

S1

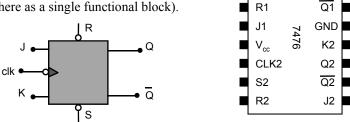
K1

Q1

# 17.16 Counters and Flip-Flops

A bistable **multivibrator** circuit is stable in two states which are called "Set" and "Reset." The stability of such a circuit element is the basis behind digital memory and counters, registers and other sequential control logic circuits. In this experiment, we see how a flip-flop can be used as a binary counter.

The most popular flip-flop configuration is the J-K type which contains "master" and "slave" RS flip-flops in series (although the flip-flop itself is shown here as a single functional block).



The **asynchronous** inputs S and R are used to set (Q = 1) or reset (Q = 0) the outputs and they override the action table for the J-K inputs. Note, R and S are active low and are thus normally kept high during normal operation. Setting S to 0 sets the Q output (keeping R high) and setting R to 0 with S high resets the flip-flop irrespective of the signals on J and K.

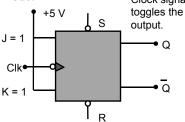
Action table:

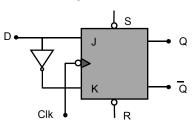
R	S	Q Q
1	1	no change
1	0	1 0
0	1	0 1

J	К	Clock pulse 1 to 0
0	0	no change, Q <sub>n+1</sub> =Q <sub>n</sub>
0	1	Q <sub>n+1</sub> = 0 (RESET)
1	0	Q <sub>n+1</sub> = <u>1</u> (SET)
1	1	$Q_{n+1} = \overline{Q}_n$ toggle

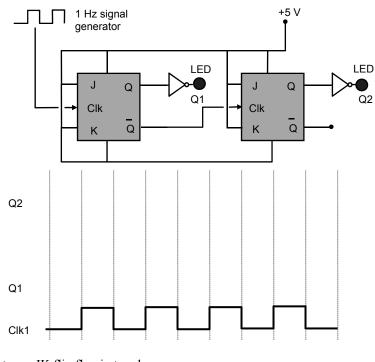
If the inputs of a J-K flip-flop are held at 1, then the flip-flop is placed in "Toggle mode." Clock signal

J-K flip-flop as a D-type latch: Clock signal transfers data from D to Q.

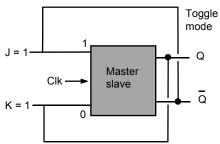




1. The cascaded flip-flop circuit shown can be used as a **counter**. The type of connection shown here produces a ripple (or **asynchronous**) counter. Construct the circuit using a 7476 dual chip and fill in the timing diagram.



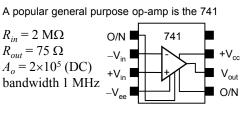
 Set up a JK flip flop in toggle mode and apply a 100 kHz signal to the Clk input. Display the Clk input and the Q output on an oscilloscope. Measure the time from the trailing edge of the clock pulse to the rising edge of the Q output pulse. Compare with book value.



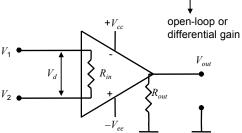
# 17.17 Op-Amps

Having an amplifier in a single package makes it easy to build a variety of circuits. In this experiment, we build an inverting and non-inverting amplifier using an **op-amp**. These two amplifiers form the basis of larger instrumentation and audio amplifiers.

An operational amplifier is a difference amplifier with a very high open-loop gain. The connection of external components enables the device to act as an **inverting** or **non-inverting** amplifier. The basic configuration of the



The basic configuration of the op-amp is as follows:

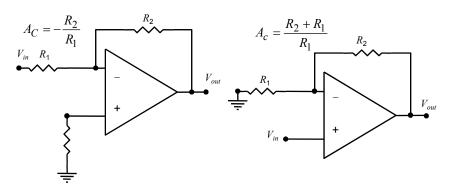


 $A_o = \frac{V_{out}}{V_d}$ en-loop or rerential gain

Connection of **feedback resistors** permits the construction of:

(a) inverting amplifier

(b) non-inverting amplifier



- 1. Design and construct an inverting amplifier which will convert a 50 mV peak-to-peak 1 kHz sine wave into a 2 V peak-to-peak sine wave. Use  $V_{cc}$  +10, -10 V.
- **2.** Measure the range of peak-to-peak amplitudes of input signal for which the voltage gain is a constant (i.e., the output voltage is linearly related to the amplitude of the input signal).

$\Delta V_{in}$	50 mV	100 mV	200 mV	300 mV	400 mV
$\Delta V_{out}$					
Gain					

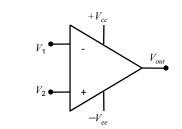
- **3.** Design and construct a non-inverting amplifier which will convert a 100 mV peak-to-peak 1 kHz sine wave into a 4 V peak-to-peak sine wave. (Use  $R_1$ = 1 k $\Omega$ .) Compare the measured gain of the circuit with that expected.
- **4.** Measure the gain of the non-inverting amplifier circuit with 3 different values of feedback resistor as shown in the table. (Change the amplitude of the input voltage if necessary.)

R <sub>2</sub>	$\Delta V_{in}$	$\Delta V_{out}$	Gain	β	Expected Gain

# 17.18 Comparator

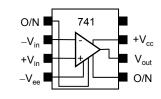
The basic ingredient of an op-amp is a high gain **differential amplifier**. This high gain feature of an op-amp allows it to be used as a comparison detection circuit. A comparator compares two voltages and provides an output (either  $+V_{cc}$  or  $-V_{ee}$ ) depending on the relative difference between the two inputs.

Comparator circuits:

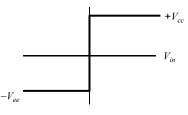


 $+V_{cc}$ 

 $-V_{ee}$ 



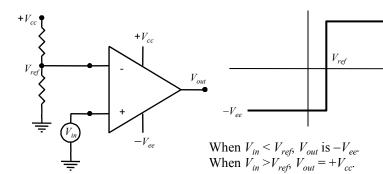
When  $V_2 > V_1$ ,  $V_d > 0$ ,  $V_{out} = +V_{cc}$ When  $V_2 < V_1$ ,  $V_d < 0$ ,  $V_{out} = -V_{ee}$ 



When input signal  $V_{in}$  is +ve,  $V_{out}$  is + $V_{cc.}$ When  $V_{in}$  is negative,  $V_{out}$  is - $V_{cc.}$ 

 $+V_{cc}$ 

 $V_{in}$ 



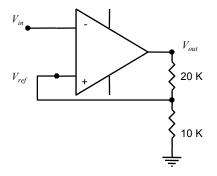
Vout

1. Design a circuit using a transistor (as a switch) and an op-amp which will turn on an LED when a resistor *R* with a value less than 1 k $\Omega$  is connected across the input. If no resistor is connected, or the resistance is greater than 1 k $\Omega$ , then the LED is to be off.



Draw your circuit and explain its operation.

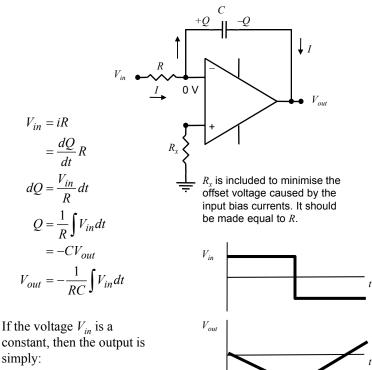
2. Construct the Schmitt trigger circuit shown and measure the DC input voltages at which the output changes state (use  $V_{cc} = +12, -12$ V). Compare with expected voltages.



# 17.19 Integrator

Why is an integrator useful? Many physical measurements involve the integration of a quantity with respect to time. An integrating circuit gives an output whose amplitude is the integration of the input voltage w.r.t. time. The circuit does this integration instantly and does not care how complicated the input signal is. Many electrical measurements involve the integrated output and such circuits are very common in scientific instrumentation.

### Integrator



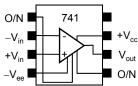
$$V_{out} = -\frac{V_{in}}{RC}t$$

- 1. We wish to convert a 1 V peak-to-peak square wave to a 2 V peak-to-peak triangle wave. Using a 741 op-amp, design such a circuit. (Let  $R_x = R$ .)
- 2. Construct the circuit but connect both inputs to earth (0 V). Connect a voltmeter to the output and determine whether or not the output changes with time (drift). Measure the drift ( $V_{out}$  per second).

If there is drift, then connect a 1 or 2 M $\Omega$  resistor across the capacitor. If the output of the circuit is "stuck" on +15 or -15, then discharge the capacitor with a piece of wire before taking measurements of drift.

How does the 1  $\ensuremath{\text{M}\Omega}$  resistor reduce drift?

- **3.** Disconnect inputs from 0 V and then connect to square wave oscillator. Make sure that the peak-to-peak input voltage is exactly 1 V and tune the circuit to obtain exactly a 2 V peak-to-peak output signal.
- **4.** Test the circuit at increasing frequencies and record and comment on your observations.



# 17.20 Component Values

## Resistors

Resistors used in electronic circuits are colour-coded to indicate their resistance (in ohms) and the tolerance. The tolerance indicates by how much the actual resistance of the device may differ from its nominal value. Usually, a tolerance of 1 to 5% is acceptable.

Colour	1st band 1st figure	2nd band 2nd figure	3rd band multiplier	4th band tolerance
Black	0		1	
Brown	1	1	10	1%
Red	2	2	10 <sup>2</sup>	2%
Orange	3	3	10 <sup>3</sup>	
Yellow	4	4	10 <sup>4</sup>	
Green	5	5	10 <sup>5</sup>	
Blue	6	6	10 <sup>6</sup>	
Violet	7	7	10 <sup>7</sup>	
Grey	8	8	10 <sup>8</sup>	
White	9	9	10 <sup>9</sup>	
	1	1		
Silver			10 <sup>-2</sup>	10%
Gold			10 <sup>-1</sup>	5%
L		-		
		$\rightarrow\rightarrow \checkmark \land \land$		
	—			lue green violet = $\Omega$ 5% tolerance

Resistors are also manufactured to a maximum power dissipation rating. However, the power rating is usually not specified on the resistor itself, but a good estimate may be made from the physical size of the component. Most resistors in electronic circuits have a 0.25 to 1 W power rating.

## Capacitor markings:

1st figure 2nd figure number of zeros (for pF) Letter: tolerance Example: 104 K

 $1\ 0\ 0000\ pF = 0.1\ \mu F$ No. zeros 1st figure 2nd figure

### Physics

Updated and expanded with new topics, **The Electronics Companion: Devices and Circuits for Physicists and Engineers, 2nd Edition** presents a full course in introductory electronics using a unique and educational presentation technique that is the signature style of the author's companion books. This concise yet detailed book covers introductory electrical principles (DC and AC circuits), the physics of electronics components, circuits involving diodes and transistors, transistors amplifiers, filtering, operational amplifiers, digital electronics, transformers, instrumentation, and power supplies.

The level of coverage is introductory but at enough depth to enable you to undertake simple circuit design and construction. The book includes tutorial problems and a comprehensive set of laboratory experiments requiring conventional components and test equipment.

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