## INTRODUCING

# Stephen Hawking

'An ideal introduction'

'Astonishingly comprehensive ... clearer than Hawking himself'



### INTRODUCING

## Stephen Hawking

'Simply written, with lucid explanations of the physics (and metaphysics) behind Hawking's main ideas ... an ideal introduction' *Independent* 

Stephen Hawking is a world-famous physicist, but few people outside his field know what he has done. To the public he is a figure of tragic dimensions – a brilliant scientist and author of the phenomenal best-seller A Brief History of Time, and yet confined to a wheelchair, unable to speak or write.

Hawking has mastered the two great theories of 20th-century physics – Einstein's General Theory of Relativity and Quantum Mechanics – and has made breathtaking discoveries about where they break down or overlap, such as on the edge of a Black Hole or at the Big Bang origin of the Universe.

Here is the perfect introduction to Hawking's work, brilliantly written by science journalist J.P. McEvoy, who was helped by several long discussions with Hawking in researching the book. It is superbly illustrated by awardwinning artist Oscar Zarate.

J.P. McEvoy is a science journalist and author who received his PhD in Physics from Imperial College, London. He is also the author of the bestselling Introducing Quantum Theory.

Oscar Zarate is one of the UK's leading graphic artists. He has illustrated numerous Introducing titles including Freud, Quantum Theory and Mind and Brain. His graphic novel A Small Killing won the Will Eisner Prize.

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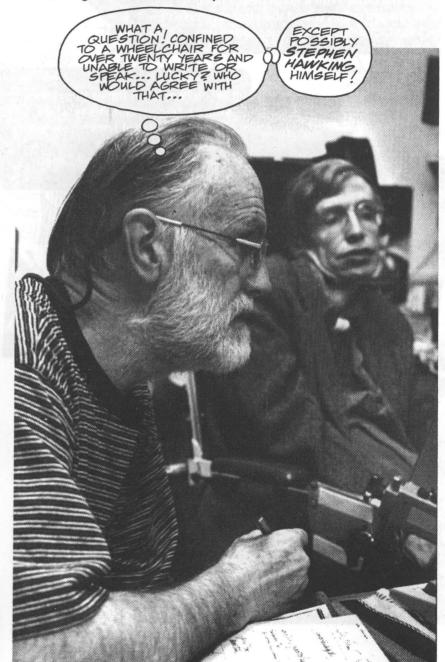
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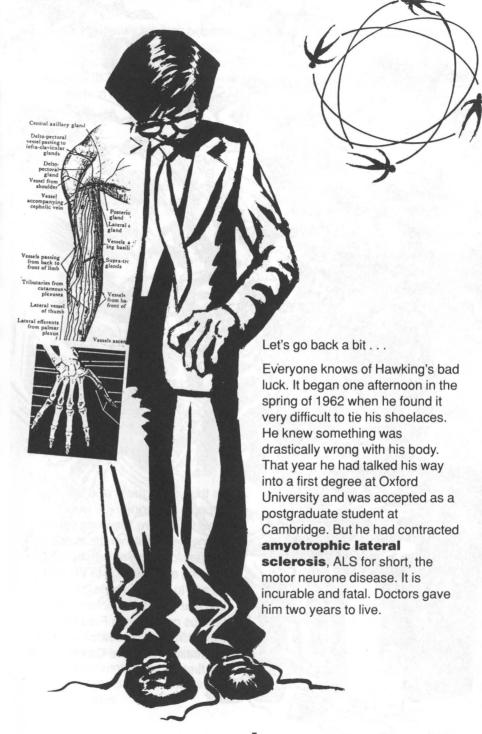
#### The Luckiest Man in the Universe

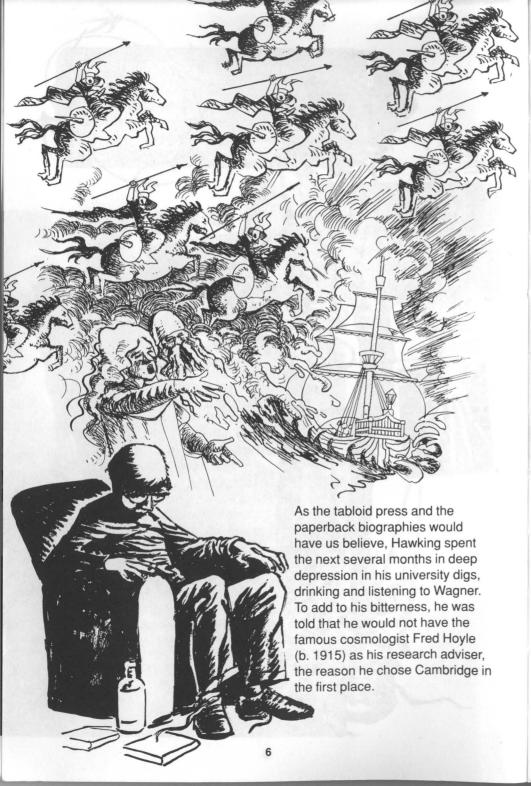
On 19 October 1994, the author of this book interviewed Stephen Hawking. He began with a question that might seem daring, if not impertinent. Did Hawking consider himself lucky?



I agree I have been very fortunate in everything except getting motor neurone disease. And even the disease has not been such a blow. With a lot of help, I have managed to get round the effects. I have the satisfaction in having succeeded in spite of it.

I'm really much happier than I was before it began. I can't say it has been a benefit, but I have been lucky that it has not been the disadvantage it could have been.





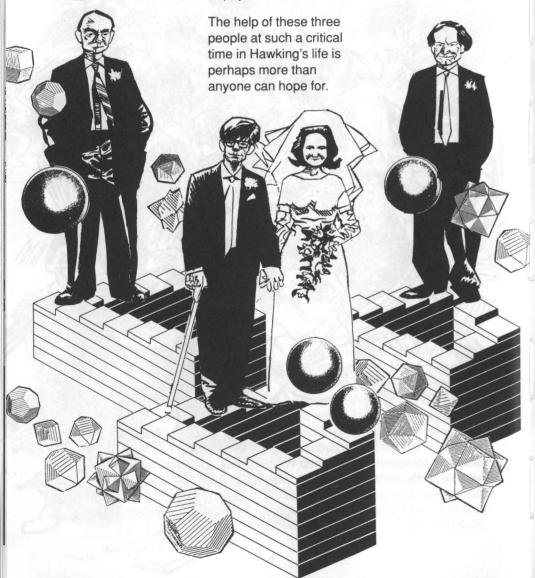
But immediately his luck began to change. A young woman, Jane Wilde, he met on New Year's Eve 1962 had taken a genuine interest in him, and the Cambridge Physics Department had assigned him to Dennis Sciama (b. 1926), one of the best-informed and most inspiring research advisers in the world of relativistic cosmology.



Once it is accepted that Stephen William Hawking's physical capabilities, were severely limited by the tragic disease of ALS, a whole series of fortunate events seemed to have taken place in the early 1960s which enabled him to fulfil his destiny as one of the leading cosmologists of modern times.

First of all, for the profession he had chosen – theoretical physics – the only facility he **absolutely** needed was his brain, which was completely unaffected by his illness. He had met a helpful partner in Jane Wilde and been presented with a sympathetic thesis adviser, Sciama.

Soon he would meet Roger Penrose (b. 1931), a brilliant mathematician working on black holes, who would teach him radically new analytical tools in physics. Penrose would help him solve a research problem that would not only save his doctoral dissertation but also bring him directly into mainstream theoretical physics.





He had another appointment with destiny at about the same time. A theory which had been developed almost fifty years earlier — Einstein's general theory of relativity — was only just being widely applied to practical problems in cosmology. It seems that predictions based on this theory were so bizarre that it had taken decades for it to be accepted. Now in the early 1960s, a golden age of research in cosmology based on general relativity was about to begin. Fate had waited for Stephen Hawking. The secretly ambitious — though by then slightly crippled — theoretical physicist was ready. He didn't know how long he had to live . . . but he was certainly in the right place at the right time.



Stephen Hawking is called a **relativistic cosmologist**. This means he studies the Universe as a whole (cosmologist) and uses mainly the theory of relativity (relativistic).

As Hawking has spent his entire career as a theoretical physicist – from the early 1960s to the mid 1990s – working with Einstein's general relativity, it might be a good idea to know what it's about.

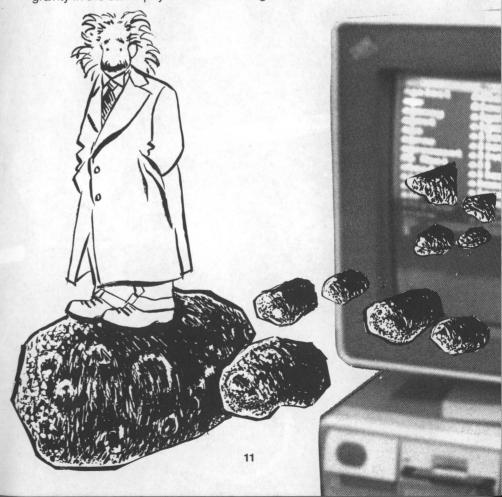


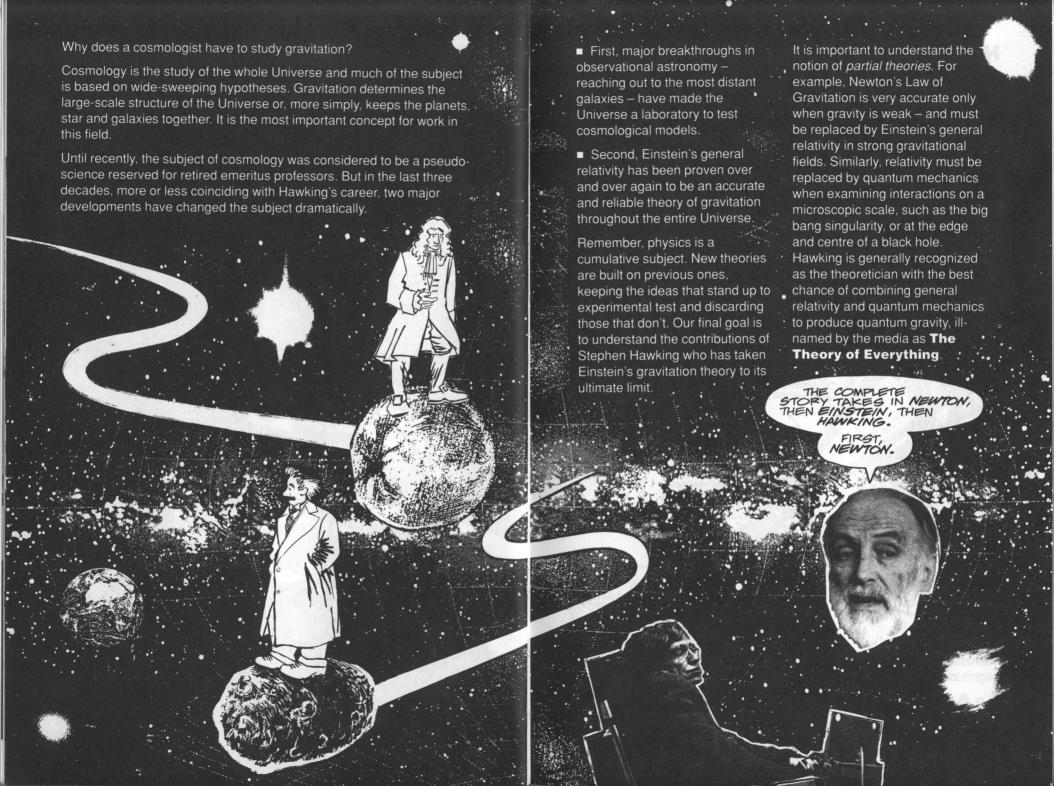
### **The General Theory of Relativity**

Berlin, November 1915. Albert Einstein (1879-1955) had just completed his theory of general relativity, a mathematical structure in which curved space and warped time are used to describe gravitation. All modern cosmology began two years later, when Einstein published a second paper called **Cosmological Considerations** in which he applied his new theory to the entire Universe.

General relativity is difficult to master, but the relatively few people who understand the theory agree it is an elegant, even beautiful theory of gravitation.

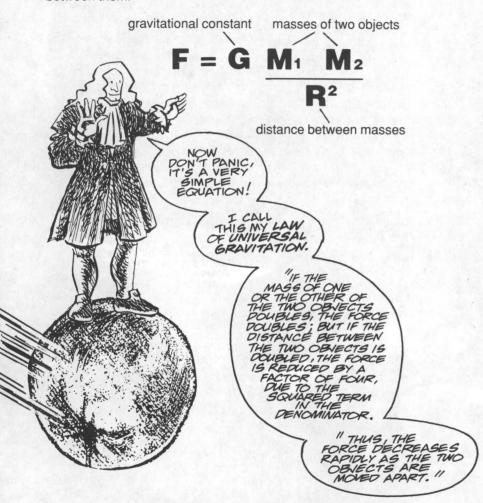
Describing a set of equations as beautiful doesn't help much in understanding how Einstein's theory differs from that of Isaac Newton (1642-1727). But an example of how each of the two theories describes gravity in the same physical situation might do the trick.





#### **Newton: The Concept of Force**

Newton introduced the concept of a gravitational *force* of attraction and stated that the mutual pull of attraction between two objects is proportional to the **mass** of each object (i.e. the amount of matter the object contains) and inversely proportional to the square of distance between them.



Gravitation is the weakest force in nature as seen by the magnitude of the gravitational constant G in practical units:

#### G = 6.67 x 10<sup>-11</sup> Newtons-metres<sup>2</sup> / kilograms<sup>2</sup>

A Newton is a scientific unit of force, equal to about a quarter of a pound.

**The Electromagnetic Force:** keeps atoms together and is the basis for all chemical reactions.

**The Strong Nuclear Force:** binds the neutrons and protons together in the nucleus. This force is important in nuclear reactions like fission and fusion.

**The Weak Nuclear Force:** determines radioactive decay, i.e. the spontaneous emission of alpha and beta particles from inside the nucleus.

**The Gravitational Force:** responsible for large-scale structure of the Universe, the formation of galaxies, stars, and planets.

The four known forces separate and become individually distinct during the earliest moments of the Universe.

HOME THOMACHETIC FOR

ELEUN. 10-10 WEAK NUCLEAR FORM

GRAVITATIONAL FORCE

When two Sumo wrestlers (mass about 135 kilograms) get close to each other in the ring (say a metre apart), the force pushing them **towards each other** is minuscule . . . about 10,000 times less than the pull necessary to pick up one square of toilet tissue! To convert the answer to pounds multiply Newtons by 0.225.

Fg =  $(6.67 \times 10^{-11}) (135) (135) = 0.000012$  Newtons  $(1 \text{ metre})^2$  (0.0000027 lb)

But the force pulling each of them **towards the floor** is much larger. That's because the other object attracting each **downwards** is the Earth, whose mass (5.98 x  $10^{24}$  kilograms) must be put in the numerator of Newton's equation. The Earth's radius (6.37 x  $10^6$  metres) goes in the denominator. Try the calculation yourself with an electronic calculator and don't forget the conversion factor to get your answer in pounds.

Fg = 298 lb (weight of Sumo)









## The Principia: Describing Newton's Universe

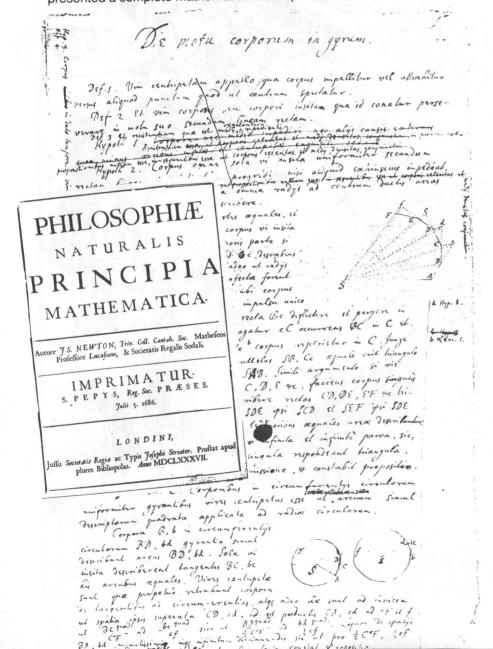
Newton was chiefly concerned with the force of gravity between the Sun and planets, i.e., the solar system. The immediate impetus for the publication of his theory of gravitation, the **Principia**, arose from a discussion at the Royal Society in 1684 between the astronomer Edmond Halley (1656-1742), the architect Sir Christopher Wren (1632-1723) and Newton's arch rival Robert Hooke (1635-1703).







Halley returned to London frustrated, but 3 months later he received a 9-page paper in Latin, **De Motu Corporum** or **On the Motion of Bodies in Orbit**, in which Newton described the elliptical paths of the planets in terms of his Law of Gravitation and his Laws of Motion. This was the precursor of his world-famous **Principia** (1687) which presented a complete mathematical description of his ideas.



#### **Newton and Hawking**

The media often compares Stephen Hawking with other famous physicists like Newton and Einstein, much to the alienation of scientists and, in particular, historians of science. No single individual will ever dominate his era as Newton did, whereas Hawking is one of a small group of élite scientists at the cutting-edge of today's cosmology.

Yet, some of these comparisons are very interesting.

Newton spent his entire scientific career at Cambridge with his residence and laboratories at Trinity College. Hawking has been at Cambridge since his postgraduate student days in 1962, except for a few sabbatical years abroad.

They have both attempted to explain the observable physical Universe using theories of gravity: Newton using his own theory, and Hawking using mainly Einstein's general relativity.

Both have held the same distinguished position at Cambridge, the Lucasian Chair of Mathematics.

The wide range of applications for the gravitation law which Newton presented in the **Principia** is quite extraordinary. The theory was an immediate success and found to be applicable to all motion in the solar system, including the Moon and comets as well as the planets. It was so accurate that it was used to discover the planet Neptune, which could not even be seen with the telescopes available at the time.

Except for one small problem. The orbit of Mercury wasn't quite right. But as Mercury is so close to the Sun and very difficult to view, the discrepancy was thought to be due to observational errors and excused by everyone in the 17th and 18th century. The orbits of Jupiter, Mars and Saturn were

spot on. No one was worried.

BUT I'M WORRIED

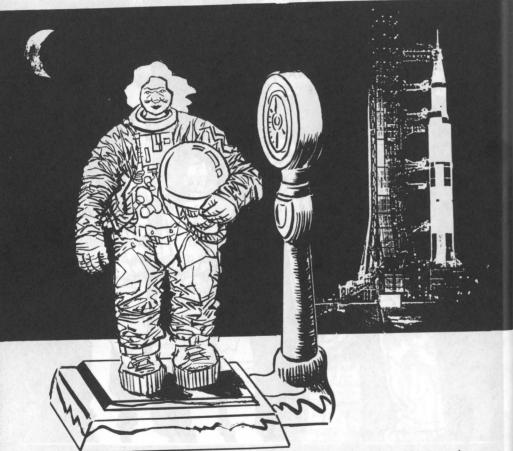
Many may find it surprising to learn that putting a man on the Moon, some half-century after Einstein, did not require any modification of Newton's theory. NASA engineers were using the **Principia** when they programmed their rockets at Cape Kennedy in 1969.



But the difference is negligible, unless measurements are being made very close to a massive gravitational object. For orbits around the Sun and the planets, in fact throughout most of the entire solar system, Einstein's relativistic effects can be ignored and Newton's theory is fine.

### **The Concept of Mass**

Consider the miracle method for losing weight: a trip to the Moon! When an object is transported in a spaceship to the Moon, its weight decreases by about a factor of 6! This weight loss can be demonstrated very simply, using Newton's gravitation formula to compare the force of gravity of a body at the surface of the Earth (i.e. its weight) with that on the surface of the Moon. Just plug the numbers into the equation and see the dramatic weight loss. But watch how you use mass.

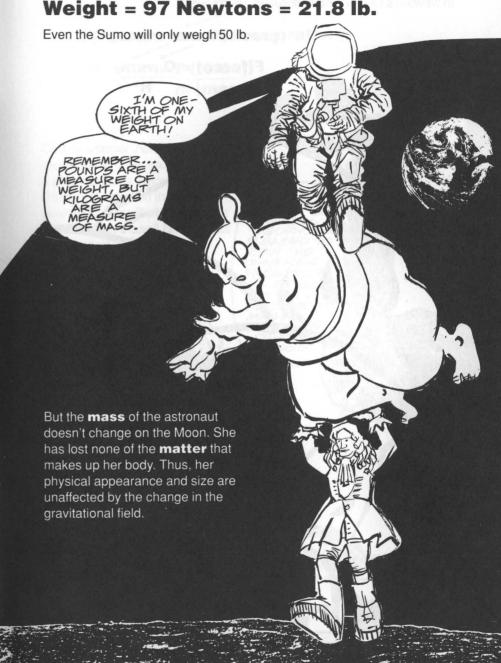


The mass of the astronaut is about 60 kilograms (determined by a scale balance and standard masses); the mass of the Earth is  $5.98 \times 10^{24} \, kg$ and the radius of the Earth is 6.37 x 106 metres. If we use these values in Newton's equation, we find her weight to be (with 1 Newton = 0.225 lb):

Weight = F<sub>q</sub> = 590 Newtons = 132 lb

Now what will she weigh on the Moon? Use the same method but this time use the mass of the Moon =  $7.34 \times 10^{22}$  kilograms and the radius of the Moon =  $1.74 \times 10^6$  metres

Weight = 97 Newtons = 21.8 lb.



Mass is a tricky concept. No doubt about it. It is not only difficult to understand, but, until Einstein, it was also horribly ambiguous. Think of that property of a body that causes it to be attracted by another body, as in Newton's Law of Gravitation.

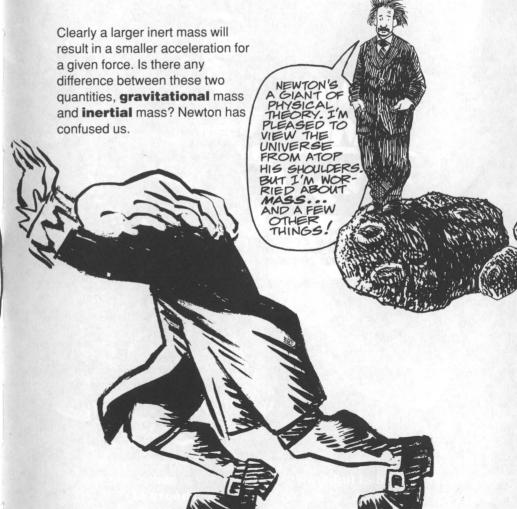


Then think of the property of a body which gives it resistance to a change in speed, as in Newton's second Law of Motion;



F(force) = m x a (acceleration)

or . . . a = F (force) m (mass)



# Albert Einstein, the Saviour of Classical Physics

It was left to a single man to clear up the leftover inconsistencies of classical physics, Albert Einstein. The great Victorian physicists had decided that only trivial problems remained. Yet, Einstein proceeded to turn Newtonian physics upside-down.

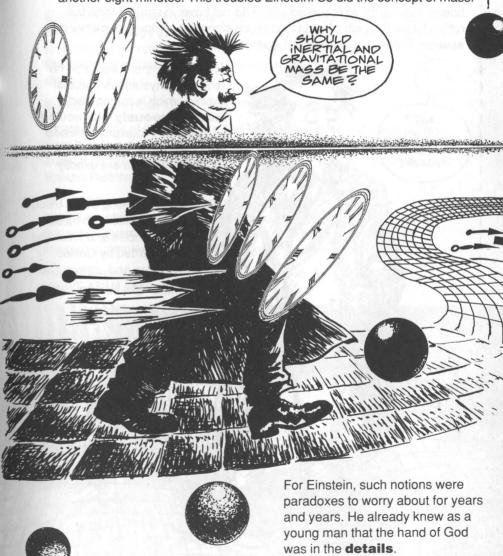
Imagine Newton's theoretical structure as a house of cards. It's true, Einstein only removed two of these cards. They just happened to be at the base of the structure.



To do this, it was necessary to postulate that nothing can travel faster than the **speed of light**, which Einstein said was always observed to be the same. This work he called the **Special Theory of Relativity**.

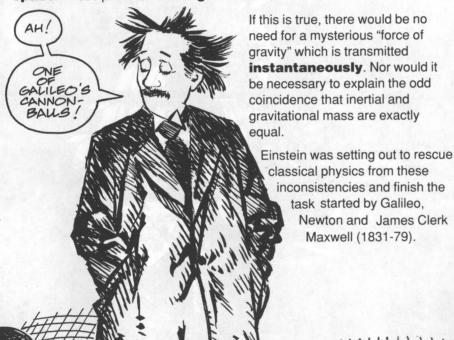
Einstein's first papers were about electrodynamics and concerned with light signals and moving clocks. But he soon began worrying about gravitation and was troubled by its bewildering property of **action at distance**.

According to Newton, if the Sun disappeared in an instant, so would its gravitational field at the Earth, millions of miles away. Yet light from the Sun, with its finite speed, would continue to travel towards the Earth for another eight minutes. This troubled Einstein. So did the concept of mass.



Einstein the Worrier began to consider if there might be another way to explain gravity. Maybe it is not a force at all. Since the motion of a freely falling object does not depend on the object's mass or composition (as Galileo discovered in the 15th century), gravitation might be due to certain properties of the medium it's falling in, that is, space itself.

By a series of remarkably creative and idiosyncratic steps, Einstein decided that space is not flat but curved, and the local curvature is produced by the presence of mass in the Universe. Consequently, bodies moving through curved space do not travel in straight lines but rather follow the path of least resistance along the contours of curved space. These paths are called geodesics.



inconsistencies and finish the Newton and James Clerk

#### **Einstein and Hawking**

Most great works in physics have come from those who combine miraculous physical intuition with sound mathematical skills. The former is far more important than the latter.

Einstein was not a pure mathematician and neither is Stephen Hawking. They both learned the mathematics they needed to do their physics, formulating their ideas in the most efficient way possible.

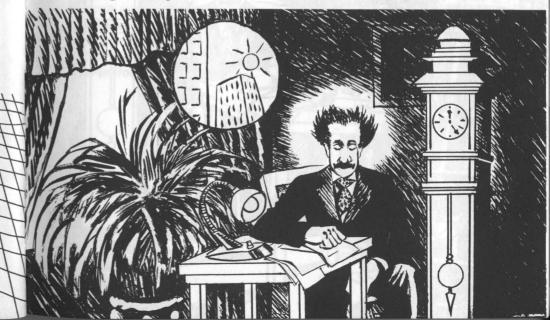
Einstein hassled his friend Marcel Grossman to learn the techniques of Riemann geometry in order to handle curved space. Hawking, anxious to probe the secrets of black holes in the early 60s, questioned Roger Penrose to exhaustion learning the new topological methods of singularity theory.

But both had a nose for the most interesting problems.

Einstein's idea of curved space had some plausibility, but it was not clear how to quantify such a new approach. So he started dreaming up more of his famous gedanken (thought) experiments, as he did with Special Relativity.

His sketchy qualitative ideas of curved space were to become a set of equations which gave the precise amount of curvature for a given amount of mass. This development is said to be one of the most creative examples ever of the power of pure abstract thought.

The main idea which got him started he called, The Happiest Thought of My Life.

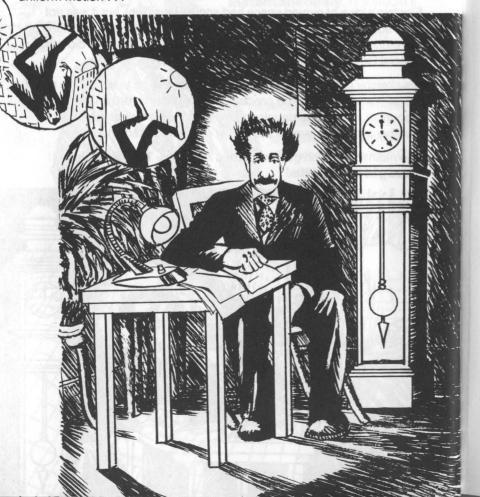


#### **Einstein's Happiest Thought**

Sitting in a chair in the Patent Office at Berne (in 1907), a sudden thought occurred to me. "If a person falls freely he will not feel his own weight." I was startled and this simple thought made a deep impression on me. It impelled me towards a theory of gravitation. It was the happiest thought of my life.

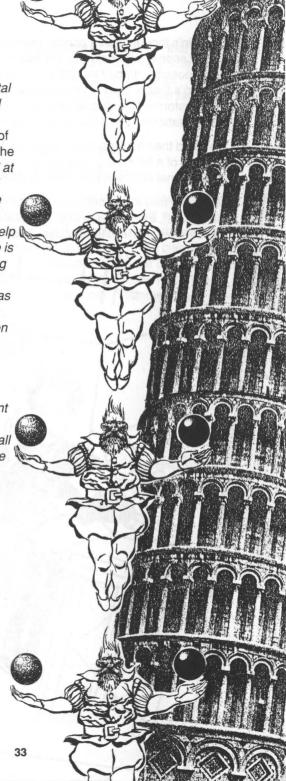
I realized that . . . for an observer falling freely from the roof of a house there exists – at least in his immediate surroundings – no gravitational field. If the one who is falling drops other bodies (e.g. Galileo's cannon balls), then these remain relative to him in a state of rest or of uniform motion independent of their particular chemical or physical nature. (Of course, we are ignoring the effect of air resistance.)

The observer therefore has the right to interpret his state as at rest or in uniform motion . . .



He continued . . .

Because of this idea, the uncommonly peculiar experimental law - that in the gravitational field all bodies fall with the same acceleration (this is another way of saying that gravitational mass is the same as inertial mass) - attained at once a deep physical meaning. If there were to exist just one single object that falls in a different way than all the others, then with its help the observer could realize that he is in a gravitational field and is falling in it. However, if such an object does not exist - as experience has shown with great accuracy starting with Galileo in 1590 - then the observer lacks any objective means of perceiving himself as falling in a gravitational field. He has the right to consider his state as one of rest and his environment as free of gravity. Therefore, the fact that the acceleration of free fall is independent of the nature of the material involved is a powerful argument that the relativity postulate can be extended to coordinate systems which are in non-uniform motion.



Einstein's thought that a person falling freely does not feel his own weight seems rather simple. Yet from this starting point, he squeezed every possible drop of insight, removing all the inconsistencies of Newton's theory that his intuition and the laws of physics would allow. He transformed the simple picture of someone falling through space into a small laboratory in which gravity did not exist.

He could then analyse the effect of gravity on such phenomena as the bending of a light beam or the slowing of a clock by simply replacing the gravitational field with simulated accelerated motion.

Simply by thinking about a man jumping off a roof in Berlin (or so the story goes), Einstein was able to replace gravity by acceleration and discover his **principle of equivalence**.

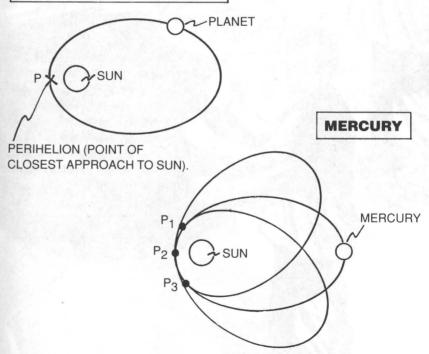


Einstein could now use the powerful principle of relativity – that the laws of physics should not depend on any particular reference frame – to test his new laws of space curvature. He also had the principle of equivalence (gravity equals acceleration) to get started. And he had one more useful bit of information, this one experimental.

## The Perihelion of Mercury: from a Problem to a Solution

Recall that scientists in Newton's time were not worried about the small discrepancy in Mercury's elliptical orbit, even though it did not return to the same starting point in each cycle. By Einstein's time, astronomers were more than worried, they needed an explanation. The discrepancy had been carefully measured to be 43 seconds of arc per century and it would not go away. Einstein could now use the perihelion result to test his curvature law. (Perihelion, from the Greek peri meaning close to and helios, sun).

#### **ALL THE OTHER PLANETS**



MERCURY'S PERIHELION ADVANCES 43 SECONDS OF ARC PER CENTURY.



Einstein used the "3 Ps" to test his equations . . .

Drinciple of Relativity Derihelion of Mercury rinciple of Equivalence

He went on producing sets of equations (mentally exhausted and trying to ignore the First World War)...

MY EQUATIONS FINALLY PRO-DUCED...

- **1.** the correct prediction for the shift of Mercury's perihelion
- **2.** incorporated the equivalence principle
- **3.** and obeyed the Principle of Relativity, i.e., they had the same form when expressed in each and every reference frame he could imagine.

These latest equations also predicted a deflection of 1.7 seconds of arc for starlight passing near the edge of the Sun and incorporated his earlier prediction of gravitational time dilation, the warping of time.

Einstein presented this final form of his general relativity law of curved space and warped time to the Prussian Academy on 25 November 1915.

Then he sat down and wrote a letter to a close friend, the Dutch physicist Paul Ehrenfest.

WAS BESIDE MYSELF WITH ECSTASY FOR DAYS.

MAGINE
MY VOY THAT THE
NEW LAW OF CURVATURE
OBEYS THE PRINCIPLE
OF RELATIVITY AND PREDICTS THE CORRECT
PERIHELION MOTION
OF MERCURY.

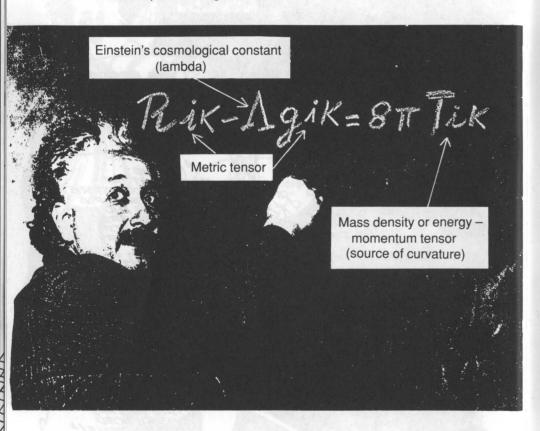
SINTHE YEARS
OF SEARCHING IN
THE DARK FOR A TRUTH
THAT ONE FEELS BUT
CANNOT EXPRESS - THE
INTENSE DESIRE AND THE
INTENSE DESIRE AND THE
INTERATIONS OF CONFIDENCE AND MISGIVING
UNTIL ONE BREAKS
THROUGH TO CLARITY
AND UNDERSTANDINGARE KNOWN ONLY
TO HIM WHO HAS
EXPERIED
THEM HIMSELF/

HUPPELD



## The Field Equations – What do they mean?

The 36-year old professor had produced a set of mathematical equations which gave the details of the relationship between the curvature of space and the distribution of mass in the Universe. Einstein found that matter tells space *how to curve* and then space tells matter *how to move* – a new way to describe gravitation. **No forces.** A mind flip is necessary to jump between the two pictures of gravitation.

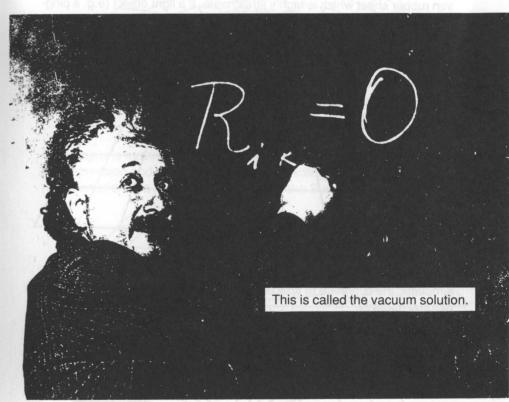


Contained within these miraculous equations is the explanation of the perihelion shift of Mercury, the degree of bending of starlight, the existence of gravitational waves, information on the singularities of space time, the description of the formation of neutron stars and black holes, even the prediction of the expansion of the Universe.

That's the good news.

The bad news is that the mathematics is extremely difficult. There are some 20 simultaneous equations with 10 unknown quantities. The equations are almost impossible to solve except in situations where symmetry or energy considerations reduce them to simpler forms.

If we ignore the cosmological constant *lambda* (which doesn't belong there anyway) and consider free space where the mass tensor is zero, the equations can be written very simply . . .

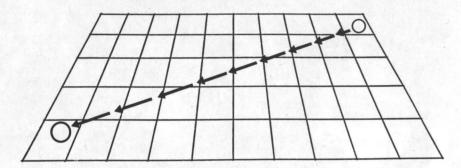


This form was made famous by a well-known photograph of Einstein lecturing on the theory in the 1920s. Looks easy!

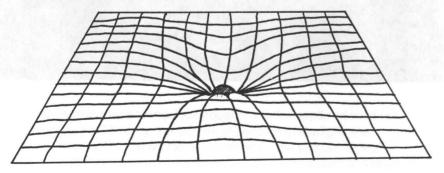
## Visualising Curved Space: the Rubber Sheet Model

Einstein's gravitation is quite unusual, compared to other field theories like electricity or magnetism, in that the description of motion (i.e. how an object moves) is already built into the field equations (how space time is curved. This can be understood with the help of a simple model – call it the rubber sheet picture.

Consider a billiard table with the slate top and felt cover replaced by a taut thin rubber sheet which is highly stretchable. If a light object (e.g. a pingpong ball) is rolled across the sheet, it will move more or less in a straight line. This simulates *flat* space and the ping-pong ball's path corresponds to the straight line motion of *special* relativity.

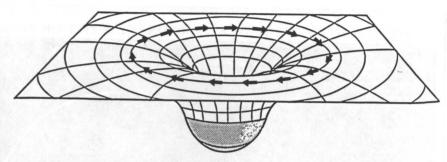


Now place a heavy billiard ball in the centre of the sheet, causing it to become curved with a depression at the centre. The model now simulates the curvature of space near a central mass as described by general relativity.

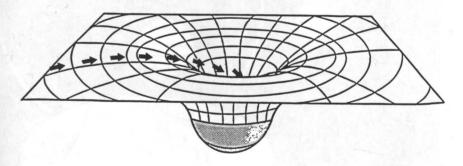


The simplest case (other than a straight line) is when the depression just captures the moving object to produce a circular orbit. Note this occurs without the need of any *centripetal force* to keep the object in orbit, as in Newton's picture.

The object would like to move in a straight line, but the space is curved, so it moves in a circle around the centre. It is simply moving along a path of least resistance in the curved space. This is general relativity's representation of how a planet is captured in an orbit around the sun.



If the object is moving on a line directly towards the centre, it falls right into the depression and accelerates into the attracting centre. This is a representation of a meteorite crashing into the Sun or the Earth.

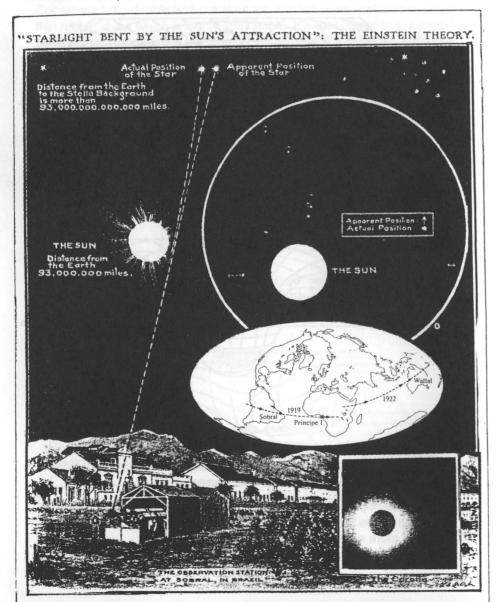


With such diagrams it is now possible to visualize the distinct and utter difference between Newton and Einstein. Einstein has replaced Newton's **gravitational force** with **curved space**.

At the time of publication, the new theory met with scepticism. Many did not wish to see the Newtonian scheme abandoned. These sceptics needed more evidence.

## The Bending of Starlight: Eclipse of 29 May 1919

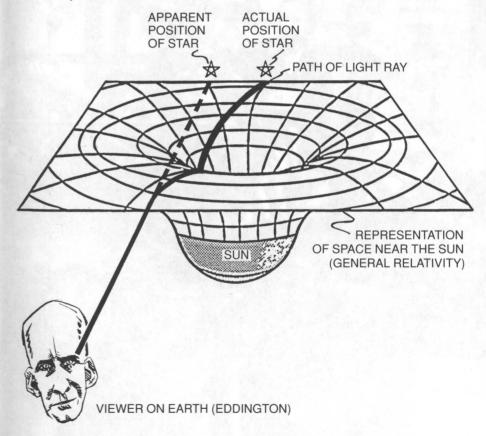
Four years later, the scientific world awaited the verdict of an experiment which Einstein himself had suggested in the original paper, the bending of starlight during a solar eclipse. The theory predicted that starlight passing just at the edge of the Sun would be displaced by 1.7 seconds of arc from its true position. It was the first real test of the theory.



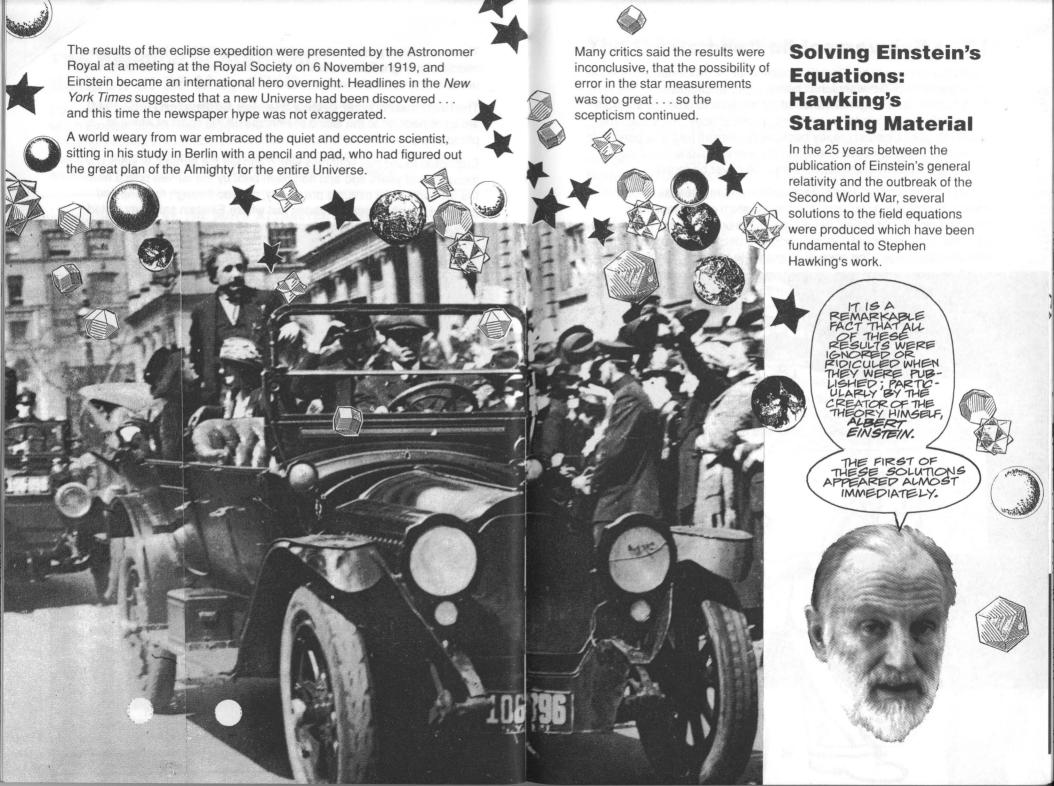
There was to be a total eclipse of the Sun on 29 May 1919, smack in the middle of a bright field of stars in the cluster Hyades. These were most unusual and optimal conditions for such an experiment.

The English astronomer **Arthur Stanley Eddington** (1882-1944) led an expedition to the island of Principe off the coast of Africa to photograph the eclipse.

Eddington found that light rays which had left the surface of stars thousands of years ago and had been bent by the curved space near the Sun only eight minutes previously, passed through the lens and exposed the photographic plates just where Einstein said they would. One of the most remarkable experiments in scientific history had been completed.



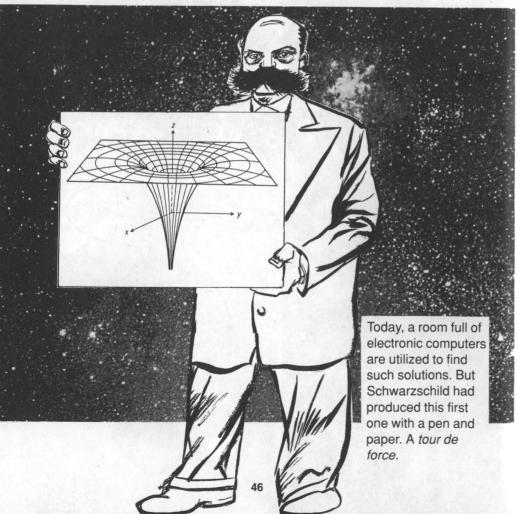
The two dimensional rubber sheet drawing of the star displacement makes it look so very simple.



### 1) The Schwarzschild Geometry

In 1915, the same year as Einstein's publication, the German mathematician Karl Schwarzschild sent a paper to Einstein. Schwarzschild used elegant mathematical analysis to produce an exact solution to the equations for an arbitrary spherical body, like a star. The solution intrigued Einstein greatly because he himself had only been able to arrive at an **approximate** solution to his own equations and thought that an **exact** solution of the equations would never be found.

Schwarzschild's solution was quite an achievement because of the technical manipulation required to solve a system of ten equations connecting twenty quantities, resulting in hundreds of terms. These are not simple algebraic equations, but second order, non-linear, partial differential equations – the bane of all graduate students in physics.



#### **The Critical Radius**

Schwarzschild's mathematics showed how the space curvature around an object of any arbitrary mass varied as a function of the distance from the centre of the object, i.e. along a **radial line.** 

His results produced a very strange geometry. There seemed to exist a critical point at which the curvature was so strong that matter could not escape. This critical point is now known as the **Schwarzschild Radius** and depends only on the mass of the object. (G is the gravitational constant; c is the speed of light)

 $\mathbf{R} = \frac{\mathbf{2GM}}{\mathbf{C}^2}$  (Schwarzschild Radius)

There was no immediate concern about this critical point, since the interior of stars and planets could not be investigated anyway. But there was speculation as to what might happen if a star or planet existed which satisfied this equation. The gravitational forces would be so great that the object would collapse indefinitely and **nothing** would be able to resist the self-gravity caused by the extreme space curvature. All the matter would be compressed to a singularity – a single point at the centre.

Planets as massive as the Earth would have to be compressed to absurd dimensions – to the size of a garden pea or the Sun to a diameter of about 3 kilometres. Ridiculous, they said. The calculation was a mathematical fluke. In any case, nobody wanted to think about it. Least of all, Einstein.



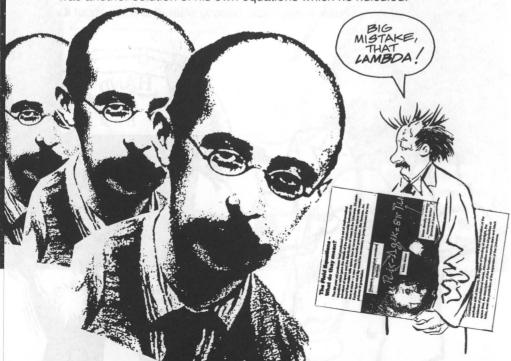
# 2) Friedmann: the Expanding Universe

Some years after Schwarzschild, another controversial solution to Einstein's equations appeared. In 1922, the Russian Alexander Friedmann (1888-1925) made the simplifying assumption that the Universe was **uniformly** filled with a thin soup of matter. (Modern measurements have shown this assumption of uniformity to be quite reasonable in spite of the formation of stars and galaxies.)

Friedmann found that general relativity predicted the Universe to be unstable and the slightest perturbation would cause it to expand or contract. He corrected a mistake in Einstein's 1917 paper on cosmology to reach this result. (Any wonder Einstein didn't like **this** prediction.)

Recall that Einstein had introduced an artificial term (*lambda*, the cosmological constant) into his field equations essentially to "stop the expansion". At the time, astronomers were telling him that the Universe was static, so he wanted to guarantee the theory would agree with observations. Later, he called this "cosmological constant" the biggest mistake of his life.

Friedmann dropped the *lambda* from the equations and got an **expanding universe**, which, of course, Einstein did not like. This was another solution of his own equations which he ridiculed.

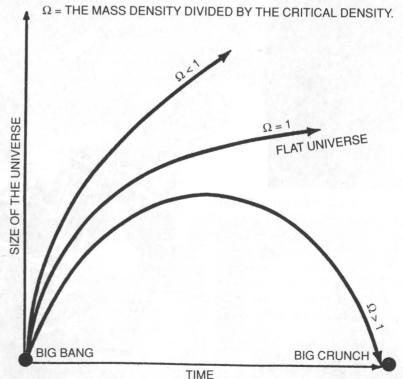


Friedmann's predictions for the expansion of the Universe can be summarized by considering three different values for the mass of the Universe in terms of a ratio  $\Omega$  (omega).

### Mass density of the Universe is greater than the critical value

In this case, the expansion rate is slow enough and the mass great enough for gravity to stop the expansion and reverse it. A Big Crunch would eventually occur with all the matter in the Universe pulled back to a single point.  $\Omega > 1$  (greater than . . . )

- Mass density of Universe is less than the critical value The Universe expands much more rapidly. Gravity can't stop it, but does slow the rate of expansion somewhat.  $\Omega$  < 1 (less than . . . )
- Mass density of the Universe is equal to the critical value The Universe expands just fast enough not to collapse. The speed at which the galaxies recede from each other gradually decreases, but galaxies always move apart.  $\Omega = 1$  (equal)



IIIVIL

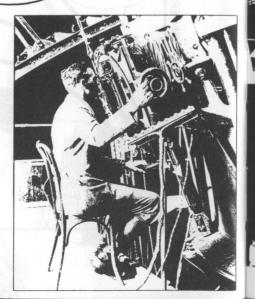
### Precursor to the Big Bang: Lemaître's Primordial Aim

The Belgian cosmologist **Abbé Georges Lemaître** (1894-1966)

was the first to use Friedmann-type solutions to formulate a model for the beginning of the Universe which he called the Primordial Atom or Cosmic Egg.

Lemaître was a visionary. Not only did he anticipate that the expanding Universe would be confirmed by looking for red shifts in the spectra of galaxies, but he even suggested that it might be possible to detect remnant radiation from the primordial atom. These two ideas dominate contemporary Big Bang cosmology in this last decade of the 20th century.

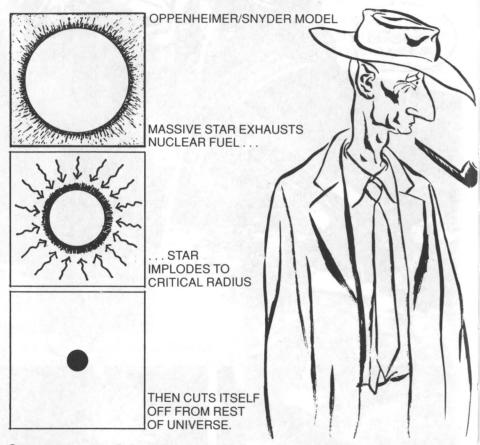
By 1929, the astronomer **Edwin Hubble** (1889-1953) had used the 100-inch Hooker telescope at the Mount Wilson Observatory in California to discover galaxies and confirm that the Universe **is** expanding. But he knew nothing of Einstein's theory or Lemaître's cosmology.



At last in 1931, Lemaître cornered Hubble and Einstein at Caltech and gave a seminar on his model Universe. ISSTILL EXPANDING TODAY/ THIS THE MOST

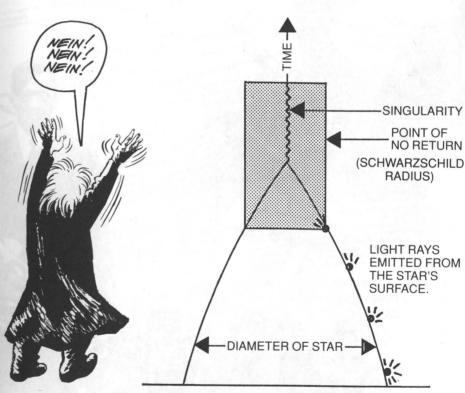
# 3) Oppenheimer: on Continued Gravitational Collapse, 1939

The third solution of Einstein's equations, important to modern cosmology and Stephen Hawking, was published by the American physicist J. Robert Oppenheimer (1904-1967) and one of his students, Hartland Snyder in 1939. They took up the problem of the Schwarzschild geometry in spite of the criticism by Einstein, Eddington and just about everybody else. The paper, which was published in *The Physical Review* was titled, "On Continued Gravitational Collapse".



Stars may eventually burn out and begin to collapse under gravitational contraction. In the idealized model of a spherical contracting star, a squeezing phenomenon can occur which could bring the star to the critical radius  $R_{\rm c}$ . Catastrophic gravitational collapse would take place for the critically collapsed star.

- Space curvature would be so severe that light rays emitted from the star's surface would bend into the star's interior, sealing off events from external observers.
- Light rays at the surface would be infinitely red-shifted, i.e., the light would have no energy.
- A one-way event horizon would form in which particles, radiation, etc. could enter the star, but nothing could be emitted.
- A space-time singularity would ultimately form, not at the critical radius, but at the centre of the star. All the physics is continuous for an observer falling in with the collapsing star's surface.

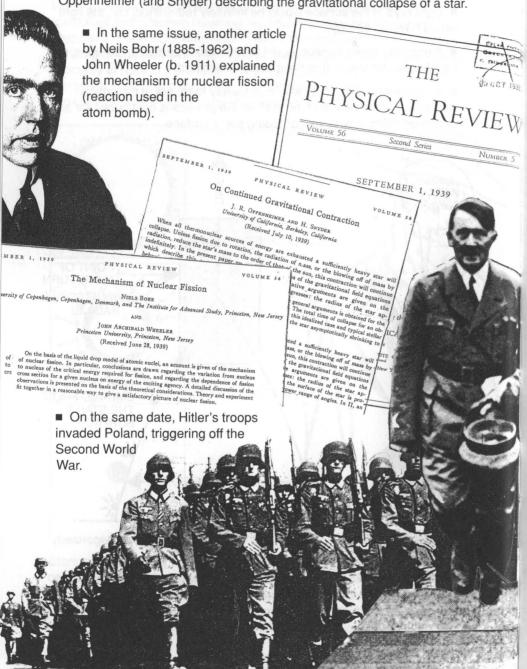


Einstein again resisted. He ridiculed the Oppenheimer result vigorously in print.

He even refused to accept that relativity could describe collapsed stars which did **not** become critical – called neutron stars – in spite of independent predictions by the eccentric Fritz Zwicky (1898-1974) at Caltech and the highly respected Lev Landau (1908-68) in Moscow.



■ Publication date for the **Physical Review** issue containing article by Oppenheimer (and Snyder) describing the gravitational collapse of a star.



When nuclear fission was discovered by the Germans Otto Hahn (1879-1968) and Fritz Strassman (b. 1902), physicists and politicians in Western democracies became alarmed that the Germans were developing an atom bomb to turn the entire world into a Nazi empire, a Third Reich ruling with the threat of nuclear devastation.

It is easy to see why work on cosmology was postponed.
Contemplating the mysteries of the physical Universe in such severe political crisis was a luxury the free world could not afford.



In addition, the originator of the general theory had opposed all the radical cosmological predictions of his own equations as developed by Schwarzschild, Friedmann and Oppenheimer. It would be 20 years before this work was resumed and the consequences of these solutions appreciated.

#### 1942 . . . A Turning Point in the Story

In 1942, physicists began to focus on deadly practical projects. Oppenheimer, one of the heroes of early cosmological research, left the heady intellectual climate of Berkeley for the barren flats of Los Alamos and the Manhattan Project. In December 1942, the Italian Enrico Fermi (1901-54) and his team at the University of Chicago achieved the first controlled nuclear chain reaction.

And at the beginning of that same year, on 8 January, Stephen William Hawking was born in Oxford. His mother had just moved from London to escape the nightly pounding by the German Luftwaffe.



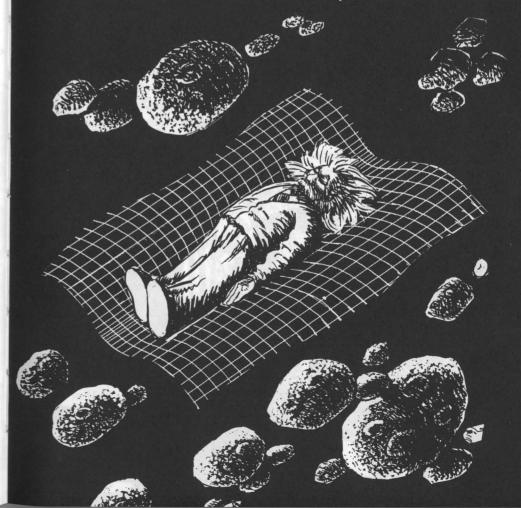
Research on collapsing stars was abandoned for over twenty years, enough time for Stephen Hawking to grow to maturity, finish his degree at Oxford and enrol as a postgraduate student at Cambridge University.

#### The Death of Einstein

Albert Einstein died on 18 April 1955 in Princeton, a small college town in New Jersey, USA. His wish was to cremated so that "no one will worship at my bones". In spite of his wish, unethical doctors performed an unnecessary autopsy and made off with his brain and his eyes – an insidious invasion of privacy.

Einstein had left Europe for the USA in 1933 with his real creative work behind him. During the last 22 years of his life, he did not work on any of the important cosmological questions which came out of his general relativity theory. For years he stuck slavishly to the task of trying to unite the field equations of general relativity with Maxwell's equations for the electromagnetic field and ignored quantum mechanics.

His unified field theory calculations were found by his bedside.

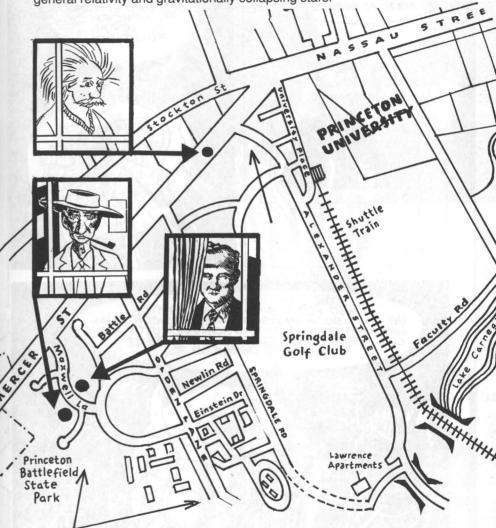




Two other physicists who also lived in Princeton mourned the death of the great scientist. Oppenheimer, no longer affiliated with the war effort, was director of the Institute of Advanced Studies (where Einstein had an honorary position) and John Wheeler was Professor of Physics at Princeton University. Wheeler had recently finished critical years of development on the hydrogen bomb and was now returning to basic research in cosmology, with particular interest in collapsing stars.



How fitting that these two physicists should live on **opposite** sides of the same street in this small academic community. They had vastly different views of the Universe **and** of American political life which placed them on opposite sides of controversial issues, like national security and nuclear weapons. Soon they would confront each other again on the question of general relativity and gravitationally collapsing stars.



In 1958, three years after Einstein's death, they both travelled from Princeton to attend an international conference in Brussels on modern cosmology. Wheeler had been invited to give a talk reviewing the current state of research.

OF ALL THE
IMPLICATIONS OF GENERAL
RELATIVITY, THE QUESTION OF
THE FATE OF GREAT MASSIVE
STARS IS ONE OF THE MOST
CHALLENGING. BUT IMPLOSION
AS CALCULATED BY OPPENHEIMER IN 1939 DOES
NOT GIVE AN ACCEPTABLE ANSWER.











A few years later, Edward Teller phones Wheeler from the Livermore Radiation Labs in California.



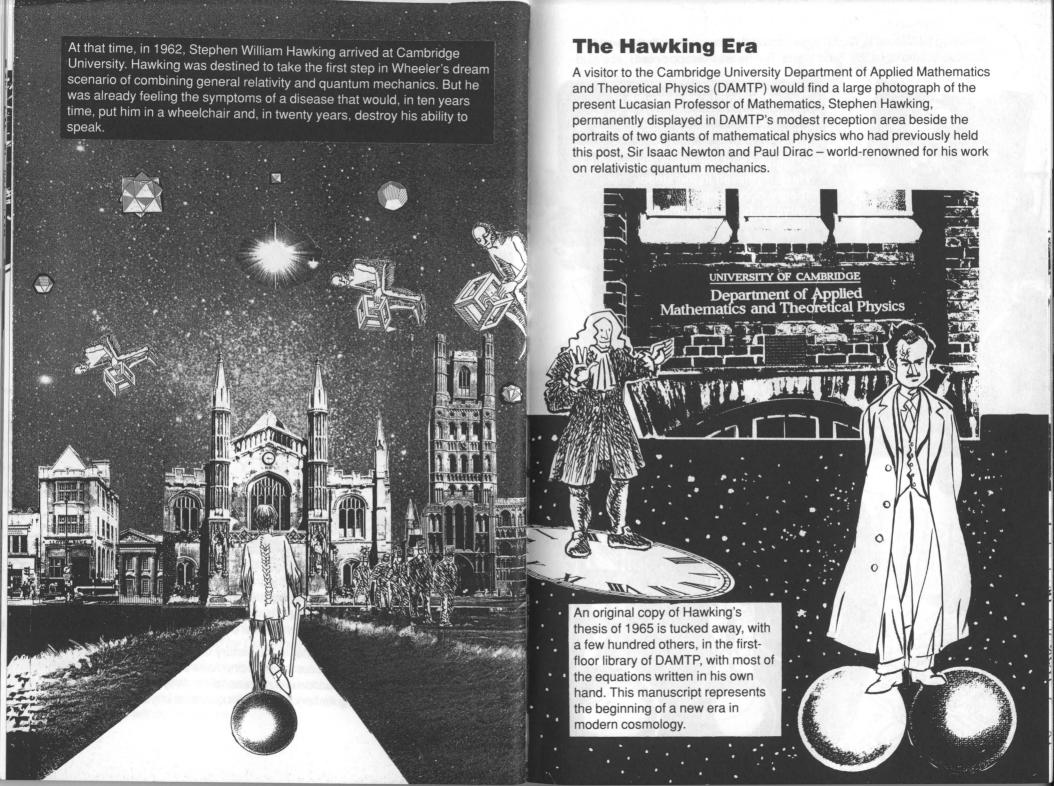
Five years later, Wheeler lectured at a special meeting in Dallas, marking the discovery of quasars. "Computer simulation shows that the collapse of a burnt-out star is remarkably similar to the highly idealized one computed by Oppenheimer and Snyder."

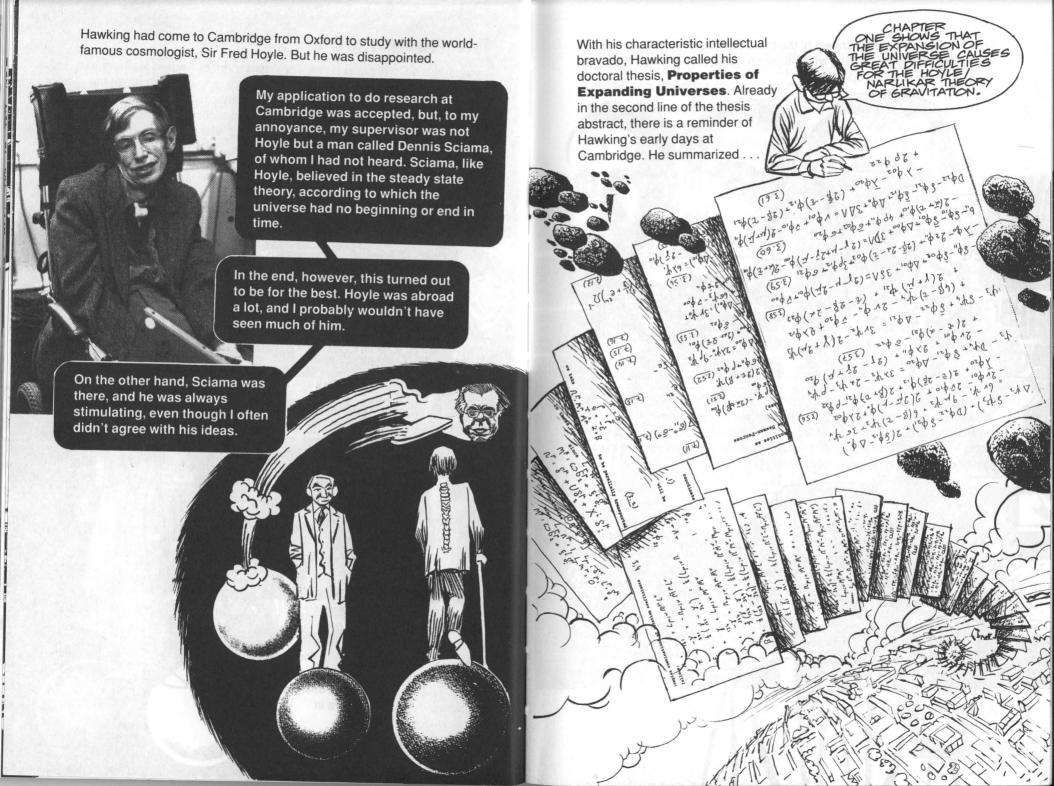
As seen by an outside observer, the collapse slows down and becomes frozen at the critical radius. But as seen by an observer moving with the star's surface, the collapse is continuous right through the critical radius and on inward without hesitation.



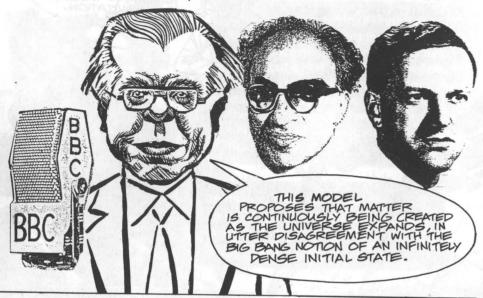
Wheeler was heartsick that Oppenheimer had lost interest in collapsing stars. But Oppie was worn out by years of political intrigue – directing the Manhattan Project, dealing with the tragedy of Hiroshima and Nagasaki, accusations of disloyalty to his country, and ignominiously losing his security clearance. Like a burnt-out star, the former **wunderkind** was himself collapsing into his own world, cut off from the rest of the Universe.

But for Wheeler, a new chapter in the history of physics had begun. "Whatever the outcome of our studies, one feels that at last in stellar implosion we have a situation where general relativity dramatically comes into its own and where its fiery merge with quantum physics will be consummated."





Fred Hoyle was the best-known of the three authors of the steady state theory of the Universe, along with Hermann Bondi and Thomas Gold, two refugees from Nazi Europe.



In the early 60s, the steady state model was probably accepted by more astrophysicists and cosmologists than the big bang. Hoyle was particularly upset by aspects of the opposing model. On a BBC radio show in 1950, he had the ignominious distinction of being the first to call it the **Big Bang** – in derision, of course.



Twelve years after this jibe, Hoyle was still developing aspects of gravitation theory at DAMTP, with a postgraduate student named Jayant Narlikar, to support the steady state model.

Hawking, who was floundering with his own research in his first months at Cambridge, became interested in Narlikar's calculations and began hanging around his office in the spirit of DAMTP's policy of free inquiry, open discussion and sharing of ideas. Hoyle knew nothing of this.





Hawking had become more and more involved in Narlikar's difficulties with the project Hoyle had assigned.

An experienced publicist, Hoyle would often present his ideas in advance of publication, before the work was refereed, in order to keep his name in the newspapers and the research grants coming in. He scheduled a talk at the prestigious Royal Society to discuss his latest ideas based on Narlikar's calculations.





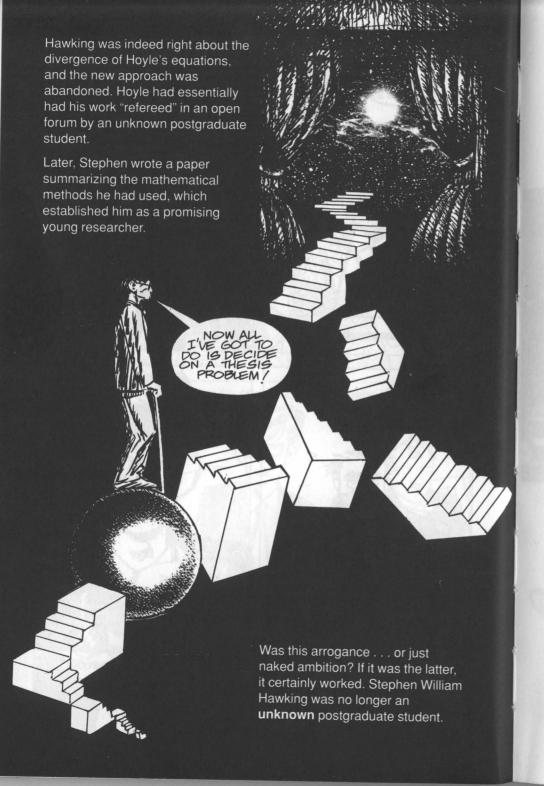








Hoyle was furious, as an embarrassed laugh passed through the room. It was a dramatic confrontation between one of the world's best-known cosmologists and the student he had rejected. The session was quickly adjourned.



## **The Unselfish Thesis Supervisor**

Dennis Sciama turned out to be a committed thesis supervisor, in the true tradition of the unselfish tutor who stimulates his charges to look for ways to increase their experience.



He refused to speed up Hawking's doctoral programme, even when pressured by Stephen's persuasive father.



Sciama developed a unique style of supervising his postgraduate students. He would not share in their work, as many other professors did around the world (he has hardly ever written any joint papers). He does not even choose their topics.

If one wishes to study the big bang origin of the Universe with the cosmic radiation background, then cosmology is only understandable with general relativity. So, naturally when I set up a research school in Cambridge in the 1960s with students who seemed gifted enough to work in these difficult areas, I suggested general relativity.

Yet nearly all the students Sciama took on in those early days have had outstanding careers in cosmology: ■ George Ellis is a Professor of Physics in South Africa. (Ellis wrote a book with Hawking entitled Large Scale Structure of Space Time, considered the Bible for research in relativistic cosmology. It is dedicated to D.W. Sciama.)

Martin Rees, currently the Director of the Institute of Astronomy in Cambridge. cosmology. It is dedicated to D.W. Sciama.)

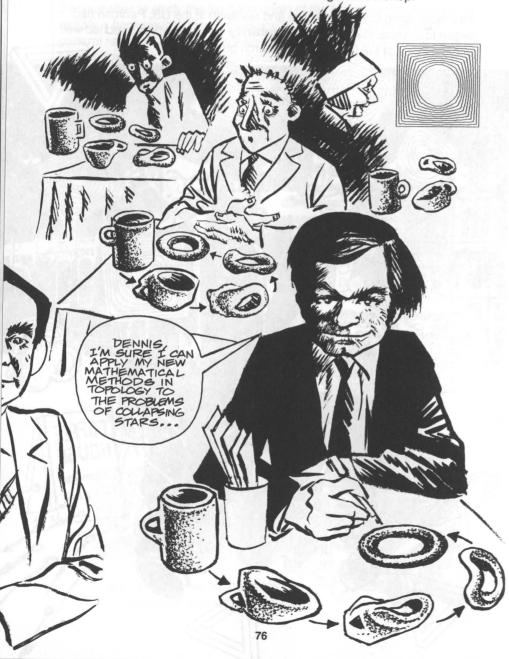
Brandon Carter is currently Director of Research at the Observatory in Paris.

And, of course, Stephen Hawking, Lucasian Professor at Cambridge. One of Sciama's important activities was to arrange for his students to attend important seminars. He always seemed to know what was going on. In the mid 60s, the Cambridge group became interested in the work of a young applied mathematician, Roger Penrose, then based at Birkbeck College in London.

After graduating from Cambridge and research in the US, Penrose had begun to develop ideas about **singularity theory**, which matched well with the ideas of the Cambridge research group.



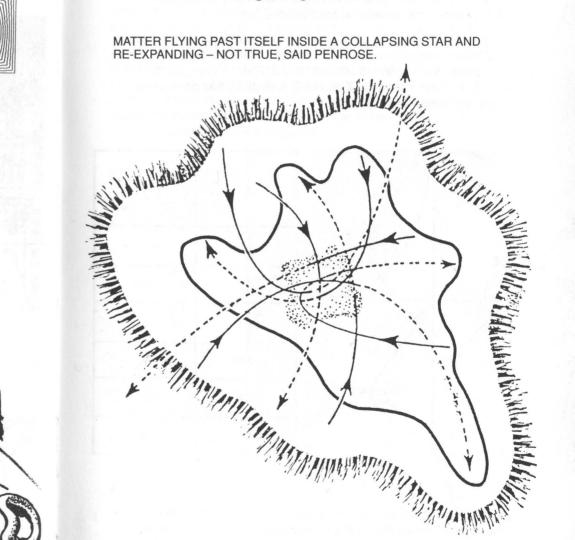
It was only a few years after John Wheeler had accepted Oppenheimer's solution and the existence of black holes, that Sciama started sharing his enthusiasm with some of his colleagues and students. Penrose, already one of the world's top mathematicians, got a flash of inspiration about these exotic objects from Sciama in a Cambridge coffee shop.



Penrose was soon able to show that if a star collapses beyond a certain point, it could not re-expand. Within the framework of general relativity, the star could not avoid becoming infinitely dense, i.e. it would form a singularity at its centre.

It was **not** true – as many insisted – that the matter of that star would "fly past itself" and expand again. Instead, a singularity of space-time would occur, a point at which time came to an end and the laws of physics broke down. It was the first singularity theorem.

MATTER FLYING PAST ITSELF INSIDE A COLLAPSING STAR AND

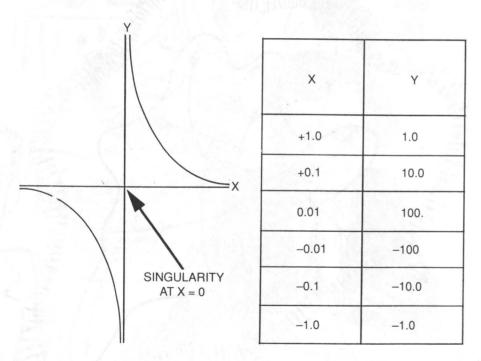


# Something You Need to Know: What is a Singularity?

Generally speaking, a singularity is a point at which a mathematical function cannot be defined. The function is seen to diverge to infinitely large values.

For example, the simple algebraic equation Y = 1/X has a singularity for value X = 0. If we make positive values of X arbitrarily small, then Y is arbitrarily large in the vertical (or positive) direction.

If we then plug in arbitrarily small negative values of X, we find Y has an arbitrarily large negative value. Thus, for the smallest change imaginable in the variable X, say from +0.000001 to -0.000001, Y changes from +1 million to -1 million. Clearly at X equals 0, something has gone wrong. This is a mathematical singularity.

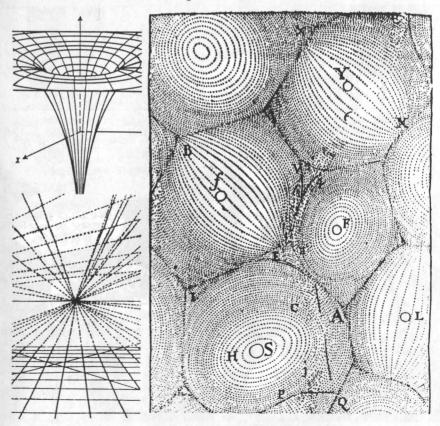


In general relativity, a singularity is a region of space—time in which the curvature becomes so strong that the general relativistic laws break down, and presumably the laws of quantum gravity take over.

If an attempt is made to describe a singularity using general relativity alone, an incorrect result is obtained: mainly that the curvature and the tidal gravity is infinite at that point. Quantum gravity probably replaces these infinities with "quantum foam" – and merges with the laws of general relativity.

But this does not mean that singularity points cannot be studied and the physics near these points understood. There are certain singularity theorems that yield important qualitative information under certain conditions. For example, if the mathematics are handled carefully, the proof of the existence of a true singularity can be a result with physical meaning. Thus, the singularity theorems of Penrose and, later, Hawking.

In the Schwarzschild solution of Einstein's field equations, the critical radius is not a real singularity (in spite of its early description as the Schwarzschild singularity). The physical processes are continuous across the boundary, and a simple change in the mathematical coordinates removes the divergence.





SEMINAR TODAY ROGER PENROSE: Topological Methods in Singularity Theorems

A group of Sciama's students were at Penrose's London seminar when he announced that he had proved that a singularity definitely exists when a star collapses to form a black hole.

Stephen Hawking was not at Penrose's seminar that day. But the news reached him immediately and made a deep impression.



SEMINAR TODAY ROGER PENROSE:



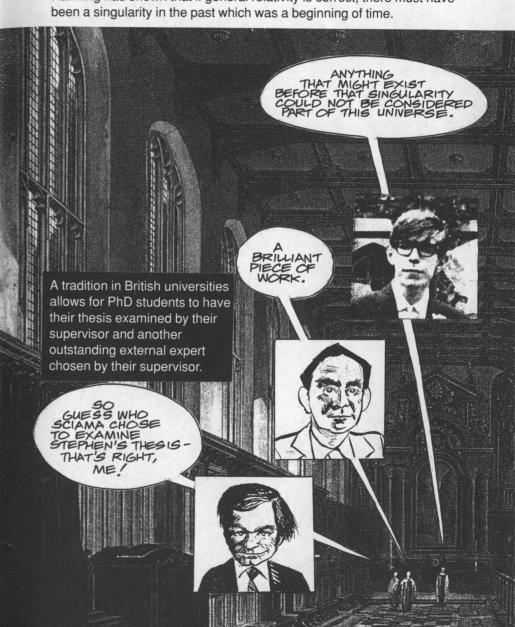
PENROSE'S RESULTS ARE VERY INTERESTING. I WONDER IF THEY COULD BE ADAPTED TO UNDERSTANDING THE ORIGIN OF THE UNIVERSE; THE EXPANDING UNIVERSE AS A GIANT COULD SING STAR IN REVERSE.



YES. MAYBE THE SAME CON-SIDERATION APPLIES AS IN HIS THEOREM FOR STARS. I'M GOING TO TRY TO ADAPT HIS RESULT TO THE WHOLE UNIVERSE AND SEE WHAT HAPPENS. SHOULD BE VERY INTER-ESTING.

Hawking had just one year left as a research student, and only now did he have a challenging problem. To adapt Penrose's method, he had to work hard, learn the mathematics involved and write it up as the last chapter in his thesis - his first singularity theorem for the beginning of the Universe.

Hawking had shown that if general relativity is correct, there must have been a singularity in the past which was a beginning of time.

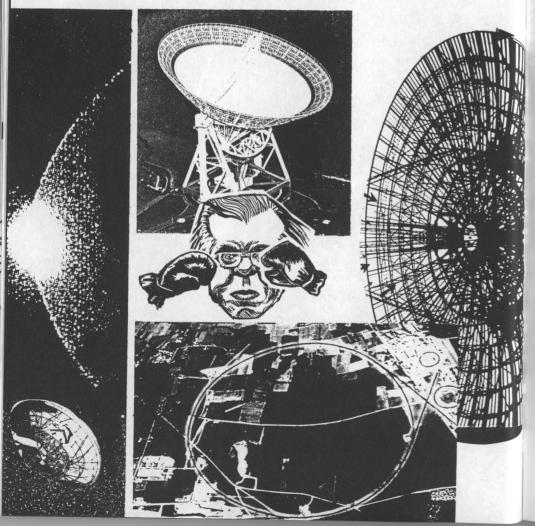


This has become generally accepted and today everyone assumes that Hawking passed and received his PhD in 1965. There were some the Universe started with a big bang – a highly dense and hot initial state. complications - like infinite and non-infinite universes - but over the next This is Hawking's major contribution to big bang cosmology, a major few years he developed new techniques to remove these problems. result for which he was to become known worldwide. Thus by 1970, five years after receiving his PhD, Stephen Hawking was an internationally known cosmologist. HUBBLE **DISCOVERS UNIVERSE IS EXPANDING** 1929 **BIG BANG** 15 BILLION YEARS AGO **FORMATION OF** THE SOLAR SYSTEM 4.5 BILLION YEARS AGO

Stephen Hawking has been a proponent of the big bang model since his early days as a postgraduate student. His PhD thesis which criticized Hoyle's steady state model and his proof of a big bang singularity link his name with the success of the latter for all time.

It is interesting to imagine the recent history of cosmology (or at least the recent history of Stephen Hawking), if his application to study with Hoyle at Cambridge had been approved.

Today, Hoyle and his former student of 30 years ago, Jay Narlikar, are still patching up the steady state model. But it is a dead duck. The world of cosmology has moved on. Perhaps this is best shown by the **Scientific American** article in the October 1994 special issue on the Universe, which promises to become the accepted description of our understanding of the Universe into the next millennium.

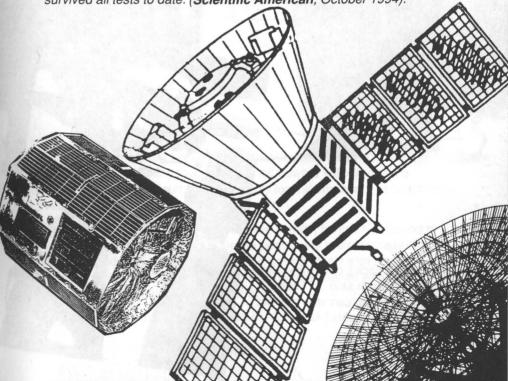


#### The Evolution of the Universe

Understanding of the evolution of the Universe is one of the great achievements of 20th-century science. This knowledge comes from decades of innovative experiments and theories. Modern telescopes on the ground and in space detect the light from galaxies billions of light-years away, showing us what the Universe looked like when it was young. Particle accelerators probe the basic physics of the high energy environment of the early Universe. Satellites detect the cosmic background radiation left over from the early stages of expansion, providing an image of the Universe on the largest scales we can observe.

Our best efforts to explain this wealth of data are embodied in a theory known as the standard cosmological model or the big bang cosmology. The major claim of the theory is that in the large-scale average the Universe is expanding in a nearly homogeneous way from a dense early state.

At present, there are no fundamental challenges to the big bang theory, although there are certainly unresolved issues within the theory itself. Astronomers are not sure, for example, how the galaxies were formed, but there is no reason to think the process did not occur within the framework of the big bang. Indeed, the predictions of the theory have survived all tests to date. (Scientific American, October 1994).



### 1965: a Big Year for Hawking

Hawking married his sweetheart Jane Wilde in Trinity Chapel at Cambridge in July 1965. Though he was now hobbling more and more on his cane, he had his PhD, a devoted and intelligent wife and new mathematical skills to use in cosmology. He also received a fellowship at Caius College to continue work at DAMTP. He was no longer depressed.

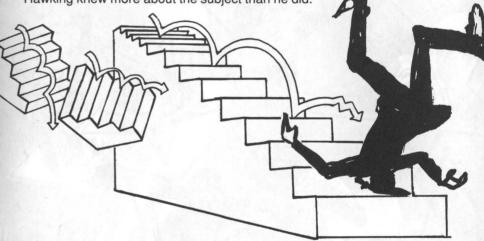


#### **An Unstoppable Mind**

Stories abound of Hawking's prodigious mental abilities, already apparent in his Oxford undergraduate years.

Several fellow students had spent weeks on a major assignment, some thirteen problems from a difficult text, *Electricity and Magnetism* by Bleaney & Bleaney. They were told to do as many as possible. Most managed to complete only one or two in the time allotted. Characteristically, Hawking left it to the last day. After spending the morning in his room, he emerged to say he was only able to complete the first **ten** of the problems!

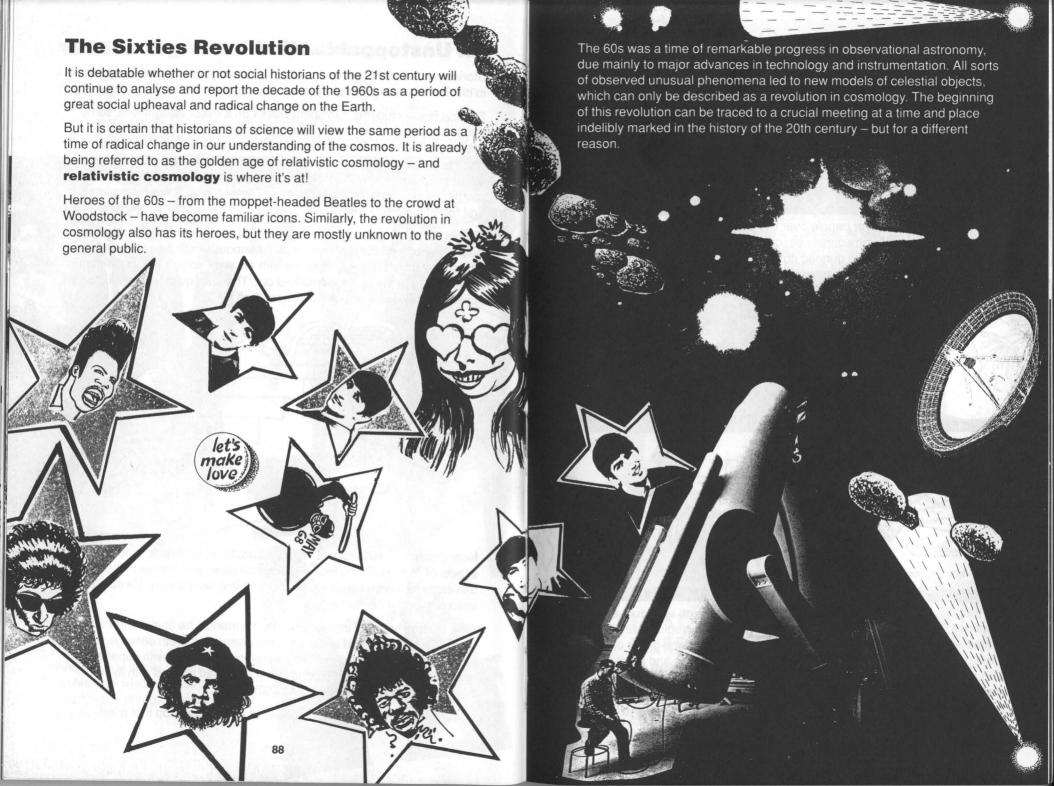
One of the Oxford tutors supervising Hawking's work in statistical physics had assigned several problems from a textbook which Stephen disliked. At the next tutorial he returned, not with the work completed, but with all the mistakes in the textbook marked out. The tutor quickly realized that Hawking knew more about the subject than he did.



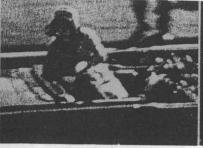
Near the end of his term at Oxford and no doubt beginning to feel the effects of ALS, Hawking took a terrible fall down a staircase in the university hall. As a result, he temporarily lost his memory. He could not even remember his name.

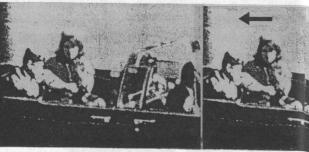
After several hours of interrogation by his friends, he finally returned to normal but was worried about possible permanent brain damage. To be sure, he decided to take the Mensa test for individuals with superior intelligence. He was delighted to find that he had passed with flying colours, scoring between 200 and 250!

Nothing, not even the dreadful illness of ALS, could stop that mind.

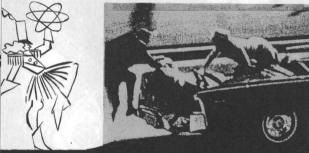


#### Dallas 1963





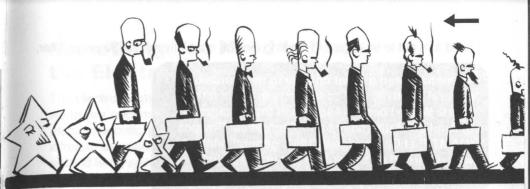
If you ask a sample of over people over fifty years old if they remember **Dallas 1963**, most will immediately describe exactly what they were doing when John F. Kennedy was gunned down in Dallas on 22 November.







But perhaps one small subset of that group might give an ambiguous response. Of course, they would remember Kennedy's tragic death. But **Dallas 1963** would have another *special* connotation for the group of three hundred astronomers, astrophysicists, cosmologists and relativists who attended the **First Texas Symposium on Relativistic Astrophysics** to mark the discovery of quasars. The symposium was held in Dallas, 16–18 December 1963, only three weeks after JFK's assassination.



The **relativists**, odd-ball specialists who spent their working lives playing around with Einstein's equations, had been invited to join real astronomers and astrophysicists in a dialogue. At last, 25 years after the famous Oppenheimer and Snyder paper on collapsing stars, general relativity was being suggested as a possible explanation for a new physical phenomenon that **had actually been observed by practical working astronomers**.

It was thought that gravitationally collapsed stars (soon to be called black holes) might be producing the massive energy necessary to explain observations on the new and exciting objects called quasars.



Thomas Gold, one of the developers of the Steady State Universe, gave the after-dinner speech at the Dallas Symposium.

THE DISCOVERY
OF THE QUAGARS ALLOWS
ONE TO SUGGEST THAT THE
RELATIVIETS AND THEIR SOPHISTIR
CATED WORK ARE NOT ONLY
MAGNIFICENT CULTURAL ORNAMENTS BUT MIGHT ACTUALLY
BE USEFUL TO
SCIENCE



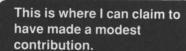
FIRST
TEXAS
SYMPOSIUM
ON
RELATIVISTIC
ASTROPHYSICS

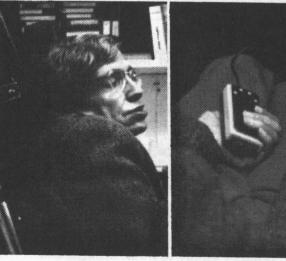
EVERYONE IS
PLEASED; THE RELATIVISTS—
WHO FEEL THAT THEY ARE BEING
APPRECIATED AND ARE EXPERTS
IN A FIELD THEY HARDLY KNEW
EXISTED - AND THE ASTRO—
PHYSICISTS WHO HAVE ENLARGED THEIR EMPIRE BY
THE ANNEXATION OF ANO—
THER SUBJECT—
GENERAL RELATIVITY.

PLEASING, SO LET US AU HOPE THAT IT IS RIGHT. It did turn out to be right, as Hawking himself modestly admits 30 years later.

There has been a great change in the status of general relativity and cosmology in the last thirty years. When I began research in the Department of Applied Mathematics and Theoretical Physics (DAMTP) at Cambridge in 1962, general relativity was regarded as a beautiful but impossibly complicated theory that had practically no contact with the real world. Cosmology was thought of as a pseudo-science where wild speculation was unconstrained by any possible observations.

The position today is very different, partly due to the great expansion in the range of observations made possible by modern technology, but also because we have made tremendous progress on the theoretical side.





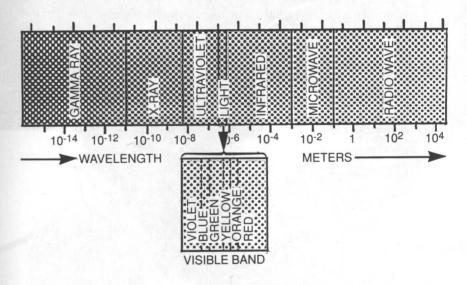


But observations on quasars required completely new observational techniques. So before describing the excitement about quasars, it might be a good idea to review *something you need to know.* 

# Something You Need to Know: the Electro Magnetic Spectrum

The **electromagnetic spectrum** sounds very technical because the two words are seldom used outside physical science. The first term, *electromagnetic*, just means that the waves we will speak of (light, radio, infrared) are made up of vibrating electric and magnetic fields. The second term, *spectrum*, refers to the range of sizes of the waves, i.e. their wavelengths.

The EM spectrum refers to all the possible wavelengths of radiation existing in nature. Different-sized waves have different properties and are generated by different physical processes. Furthermore, they must be detected by completely different equipment. The invisible radiation coming from stars and galaxies (in addition to the visible or optical band) gives useful information, though it can't be seen with the unaided eye.



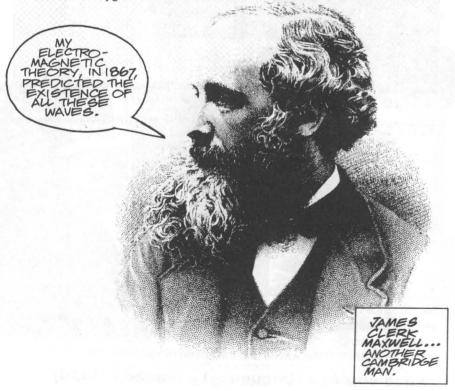
The wavelengths cover a wide range of values from X-rays (smaller than the distance between atoms) to radio waves (several kilometres in length). The waves all travel at the same speed as light and there is a remarkably simple relationship between the wavelength, the frequency of the source emitting the waves and the speed of transmission:

(wavelength) x (frequency) = (speed of light)

Before the 1960s, observational astronomy meant optical (or visible) astronomy only – looking through telescopes composed of glass lenses or reflecting mirrors and observing with the eye or with very sensitive cameras. Special films did extend measurements into the invisible infrared band with longer wavelengths than visible light.

But during the late 1950s and 1960s, nearly the **whole** electromagnetic band became detectable to observational astronomers, such that now we have *radio* astronomy, *microwave* astronomy, *infrared* astronomy, *optical* astronomy, *ultraviolet* astronomy, *X-ray* astronomy and even *gamma-ray* astronomy.

The great discoveries of the 1960s came from these extensions of observations outside the visible range, particularly to the longer wavelength microwave and radio bands. **Quasars** and **pulsars** were discovered in the **radio frequency band** and the **cosmic background radiation** was detected in the **microwave band**. And in the 1970s, **X-ray astronomy**, at the other end of the spectrum, produced the first evidence for the existence of black holes from observations of the constellation Cygnus X-1.



#### 1963: Quasars

Careful observations by radio and optical astronomers in the years 1960 to 1962 showed that there were over a half-dozen bright objects in the sky which were small enough to be stars but had a weird light spectrum – not like any star seen before.

Everyone was puzzled until 5 February 1963 when astronomers Maartin Schmidt and Jesse Greenstein at Caltech made a discovery.

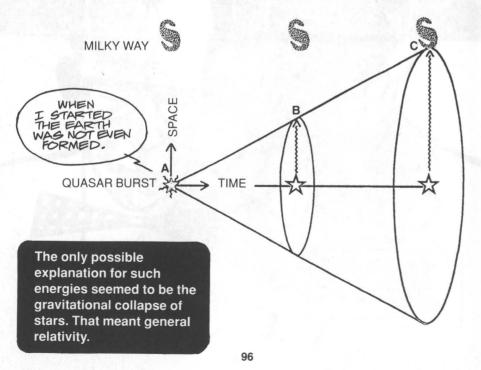


Measurements indicated that these *quasi-stellar objects* (later to be named *quasars*) were moving away from the Earth at enormous speeds and therefore must be very, very far away.



They were first thought to be stars in the Milky Way galaxy, but their discoverers soon argued that these objects were moving away from the Earth as a result of the Universe's expansion. At the enormous distances calculated, their brightness implied they were radiating 100 times more energy than the **most luminous galaxy ever seen**.

QUASARS. LIGHT LEAVES THE QUASAR AT POINT **A**. BILLIONS OF YEARS LATER, AT POINT **B**, THE LIGHT HAS STILL NOT REACHED THE MILKY WAY. WHEN THE LIGHT FINALLY REACHES US AT POINT **C**, WE DETECT IT AS IT WAS ALL THE WAY BACK AT POINT **A**.

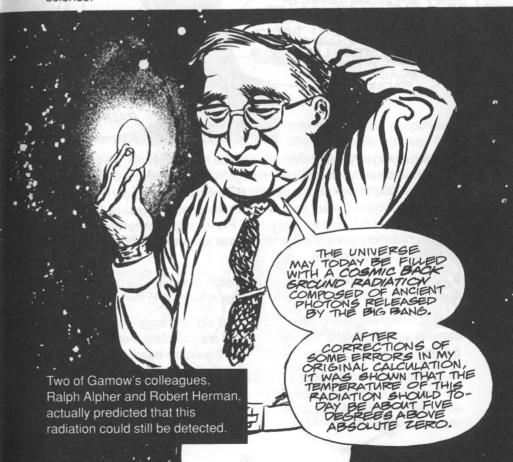


# 1965: the Cosmic Background Radiation

In 1965, an accidental discovery of mysterious microwaves from outer space turned out to be the first experimental indication that the Big Bang model might be correct. Until that time the model was thought to be something of a joke. Here's how it happened . . .

The picture of the Universe as a primordial atom ("cosmic egg") by Abbé Georges Lemaître in 1927 led some cosmologists to picture the early universe as a hot, dense, rapidly evolving plasma. One of the more imaginative of these theorists, a free-thinking Russian émigré to the USA named George Gamow, considered the effect of the cooling of this plasma as the Universe expanded.

He then made one of the most important predictions in the history of science.



All hot bodies (i.e. any object which has a temperature) give off continuous electromagnetic waves called thermal radiation, **even** if the temperature is only 5 degrees above absolute zero. The question was how to measure the radiation – which wavelength band to search.

To follow this part of the story, there is **Something Else You Really Need** to **Know!** 

# Something You Need to Know — Thermal Radiation

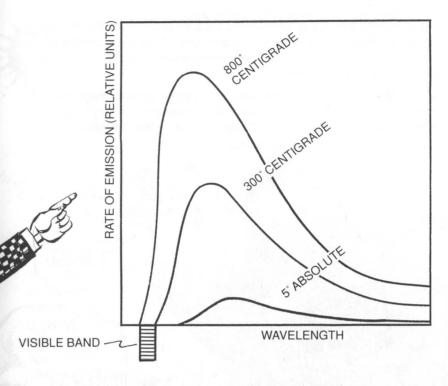
PHYSICS TEXTBOOKS DEVOTE HARDLY MORE THAN ONE OR TWO PAGES TO IT.

VERY IMPORTANT ASPECTS
OF MODERN COSMOLOGY REQUIRE AN UNDERSTANDING OF
THERMAL RADIATION: THE
COSMIC BACKGROUND RADIATION AND STEPHEN HAWKING'S
MOST IMPORTANT DISCOVERY,
BLACK HOLE
RADIATION.

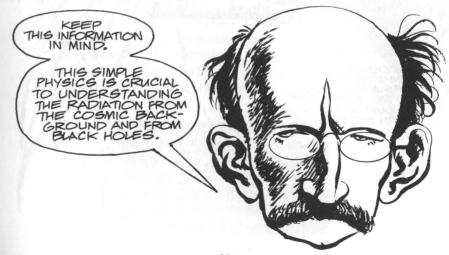
YOU MUST UNDER-STAND THERMAL RADIATION.

The underlying physics of thermal radiation is quite simple, although it did require a radical hypothesis (which began the quantum theory) by Max Planck in 1900 to explain the details. His theory showed how the relative rate of emission of radiant energy (electromagnetic waves) depends on wavelengths at different temperatures. Planck's theoretical curves show that the radiation spreads out and the peak shifts to **longer** wavelengths as the temperature **drops**.

- At 800 degrees centigrade, enough visible radiation is emitted to appear red hot, though most of the energy emitted is in the infrared band.
- At 300 degrees centigrade practically all of the energy emitted is carried by waves longer than red light and are called infrared, meaning beyond the red. No radiation is emitted in the visible band.
- At 5 degrees above absolute zero (or minus 268 degrees centigrade) the radiation is completely beyond the infrared in the microwave band and special microwave receivers are required to make the measurements.

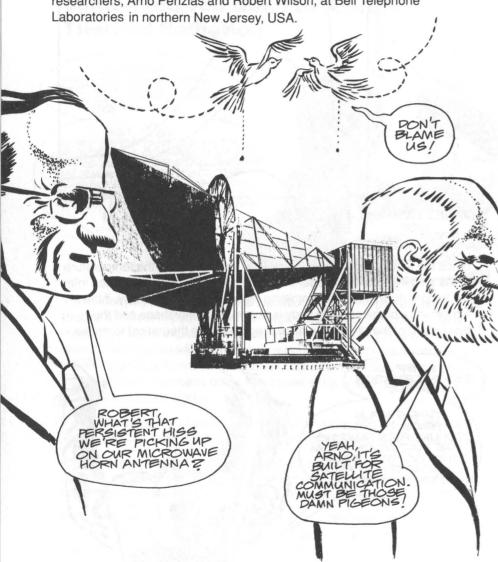


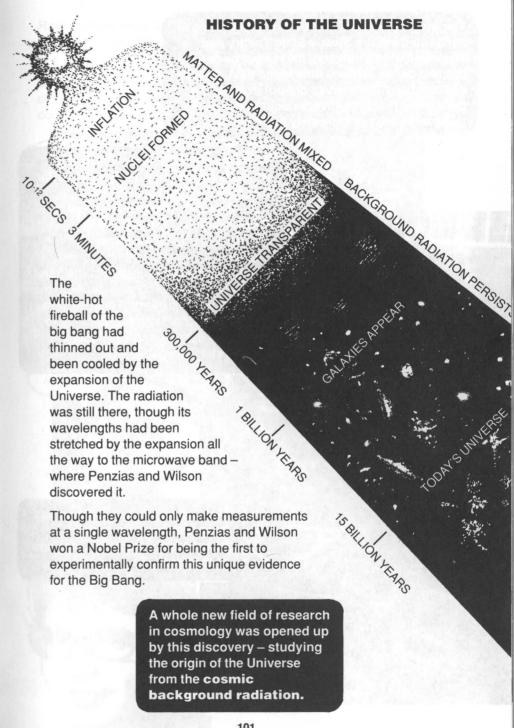
Since the shape of the curve is uniquely determined by the temperature of the emitting bodies, measurements at different wavelengths can infer the temperature of the body emitting the radiation. Conversely, if the temperature of the emitting body is known, then the shape and the distribution of the radiation can be predicted from theoretical formulae.



Returning to Gamow's prediction, the theoretical curve for the thermal radiation distribution at 5 degrees above absolute zero indicated that the peak radiation should be in the microwave region of the electromagnetic spectrum.

While other groups were in the process of planning experiments to look for Gamow's microwaves, they were discovered accidentally by two researchers, Arno Penzias and Robert Wilson, at Bell Telephone





The discovery of the microwave background in 1965 ruled out the Steady State Theory and showed that the Universe must have been very hot and dense at some time in the past. But the observations themselves did not exclude the possibility that the Universe bounced at some fairly large but not extremely high density.

This was ruled out on theoretical grounds by the singularity theorems that Penrose and I proved. We published The Singularities of **Gravitational Collapse and** Cosmology, an all-purpose singularity theorem which showed that the classical concept of time must have a beginning at a singularity in the past (i.e. the Big Bang). This theorem also implied that time would come to an end for at least part of spacetime when a star collapsed. Most of my work since then has been concerned with the consequences and implications of these results.

Radio astronomers continued finding many more radio galaxies (i.e. galaxies emitting electromagnetic waves primarily in the radio waveband).

Then in 1967, a Cambridge postgraduate student named Jocelyn Bell detected highly regular sharp pulses at 3.7 metres wavelength from one of these galaxies. The Cambridge radio astronomers thought they had contacted an extra-terrestrial civilization!





The pulses were very narrow. This meant that the emitter had to be very small, because you can't have a large body emitting short, sharp pulses. The travel time of the radiation from its different parts would smear out the signal. It had to be something highly compact; an object smaller than a few thousand kilometres in size, yet at the distance of a star.

JOCELYN BELL





# Black Holes — Wheeler Gives the Media a Buzz Word

As the 1960s were coming to a close, everyone was talking about gravitationally collapsed stars. The **partially** collapsed stars – white dwarfs and neutron stars – had become everyday objects to astronomers. But John Wheeler was interested in **massive stars** which collapse **completely** 

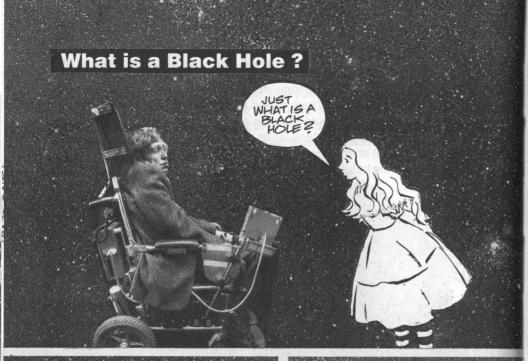
collapse completely.

It had a magic effect. Everybody immediately began using the term. Even specialists could now know they were speaking about the same thing. In Moscow, Pasadena, Princeton and Cambridge, black holes replaced "gravitationally completely collapsed stars".

### The Age of Black Holes

The media went nuts. At least they could encapsulate all this new complicated physics and astronomy in two simple words which fell easily into newspaper columns. Writers picked up on the new buzz word and books appeared on the popular science and sci-fi shelves. On TV, *Star Trek* had exotic new destinations for its space ships. At dinner parties, scientists were put on the spot to explain black holes to friends. Black holes had become household words . . . but did anyone really know what they were?





This was not a simple question. Imagine explaining Schwarzschild's and Oppenheimer's solutions to Einstein's equations, then reviewing how nature squeezes these heavenly bodies until space folds up around them and they disappear . . . all without the use of my hands.



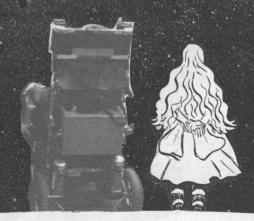


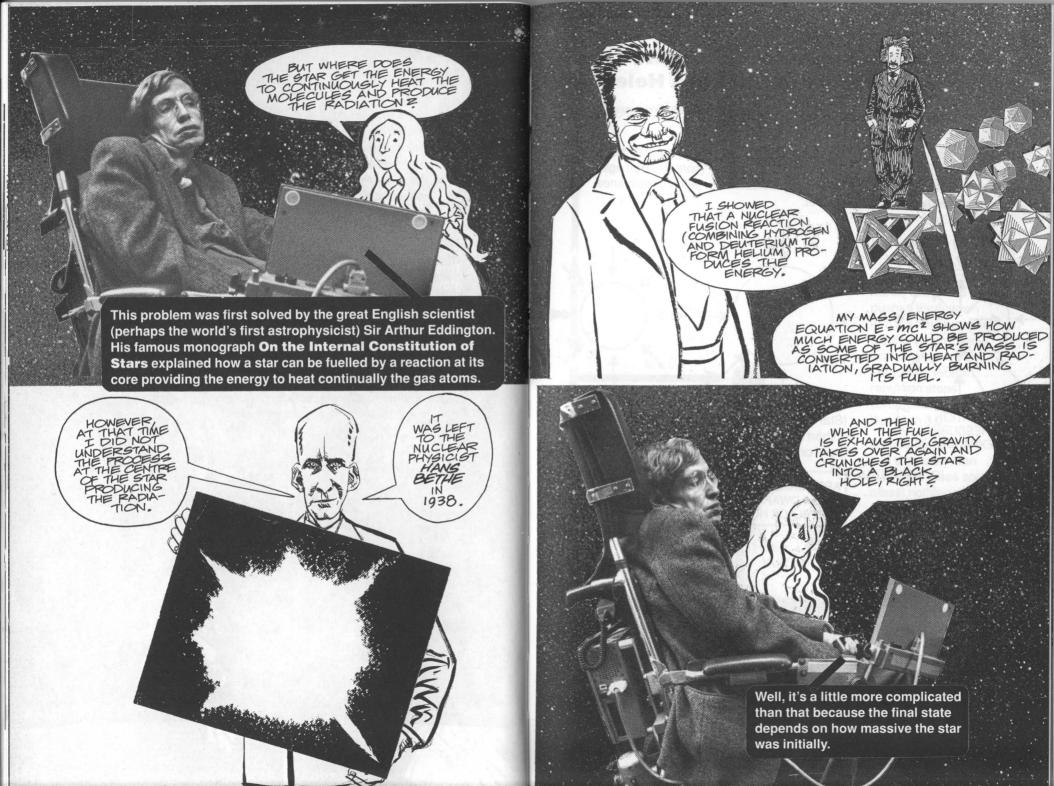
### The Birth and Death of Stars

Stars are formed when the mutual gravitational attraction between molecules floating in space, mostly hydrogen gas, causes lumps to form. As these aggregates coalesce, gravity presses the molecules closer and closer together until they interact under high pressure causing an increase in temperature.

This process continues until the gas begins to glow and produce EM radiation of all different wavelengths. As the compression increases, the interaction intensifies until the radiation pressure is great enough to stop further gravitational contraction.

The star then reaches a dynamic equilibrium and shines brightly for several billion years.





# **How Stars Collapse to Form White Dwarfs, Neutron Stars & Black Holes**

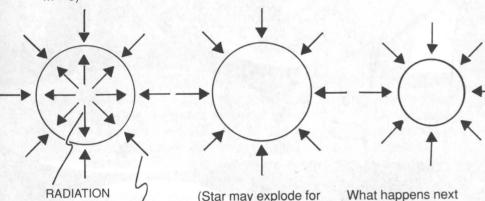
Mass of star = M in units of solar mass. (If star is 5 times as massive as the Sun. M = 5

Star burns up all its fuel, hydrogen into helium, and radiation dies out.

Then gravity begins compression again, without resistance.

depends on the initial

mass of the star.



a short time to a "red

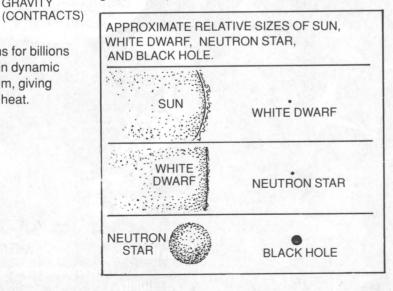
giant" or "supernova".)

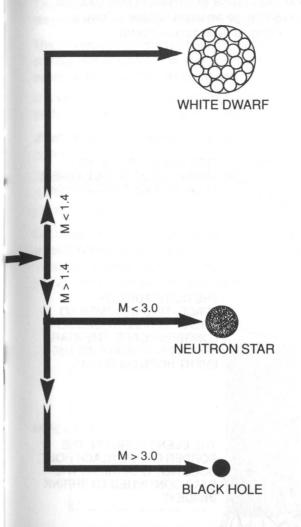
Star burns for billions of years in dynamic equilibrium, giving light and heat.

**GRAVITY** 

**PRESSURE** 

(EXPANDS)





In the black hole case, the space curvature is so extreme that, at a particular radius (called the event horizon), the light from the star's surface is bent in on itself, i.e. the rays actually go into the star instead of away from it. The star disappears from view to an outside observer.

#### **White Dwarf**

(radius - 1,600 miles)

If M is less than 1.4. star contracts until gas atoms overlap. Electron repulsion force is enough to stop contraction.

#### **Neutron Star**

(radius-16 kilometres)

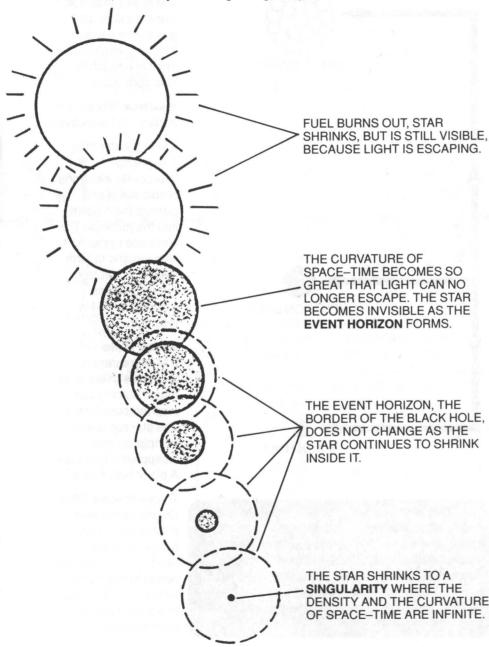
If M is greater than 1.4, gravity overcomes electrons' heroic stand and pushes them down into the nucleus. The electrons combine with protons to form neutrons. Neutron repulsion stops contraction if M is less than 3.0.

#### **Black Hole**

If M is greater than 3.0 (three times solar mass) nothing can stop the contraction. The star collapses completely and disappears from view. A black hole forms.

Traces of some White Dwarfs have been photographed and blips of rotating Neutron Stars can be detected with radio telescopes. But black holes will never be seen directly.

These circles of decreasing size show how a very massive burnt-out star, as its diameter decreases, passes through an event horizon to form a black hole, ultimately becoming a singularity at its own centre.



The illustration below presents the same information in a 3-dimensional diagram which includes **time increasing** in the vertical direction.

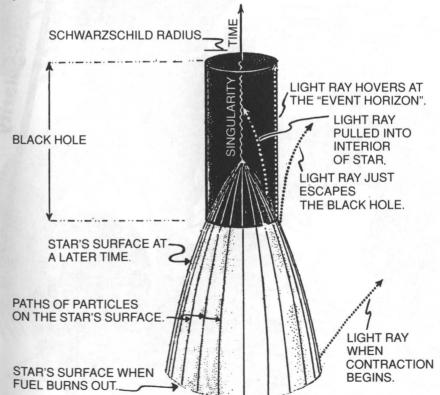
This shows the bending of the light paths and indicates how the star's surface has shrunk all the way down to the singularity (right through the event horizon) as the star collapsed.

It is very important to understand the **path** of the light rays from the surface of the star as it passes through the event horizon.

**Just before the horizon forms**, light rays are bent strongly by gravity and only just leave the star's surface.

A few moments later, when the star is **just inside the event horizon**, the light rays are pulled into the interior of the star towards the singularity at the centre.

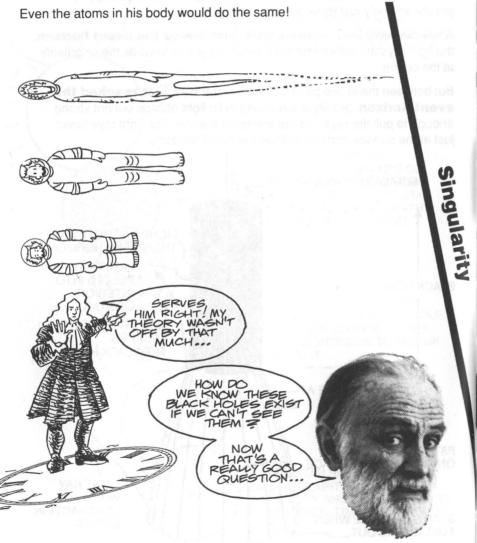
But between these two points, when the star **has just reached the event horizon**, gravity is too strong to let light escape but not strong enough to pull the rays into the interior of the star. The light rays hover just at the surface and this defines the event horizon.



What would happen if someone flew into a black hole?

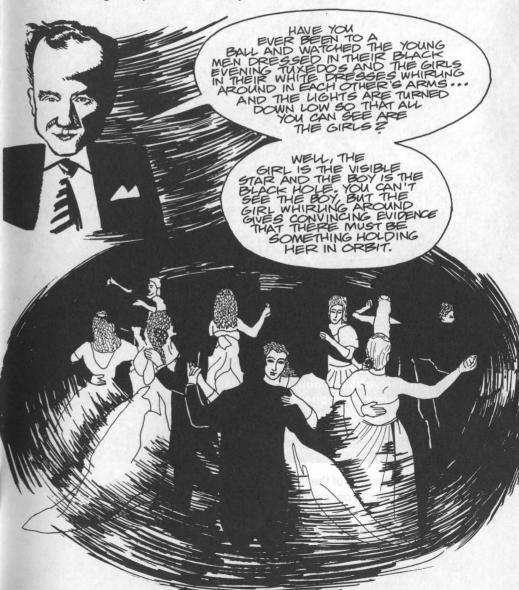
Einstein and the relativists have an answer that outdoes science fiction. According to the Oppenheimer and Snyder solution, anyone who goes through the event horizon must eventually hit the singularity with disastrous results.

He will be pulled and squeezed – until, at the centre of the black hole, his body would be stretched infinitely long and his width squashed to zero like a length of spaghetti!



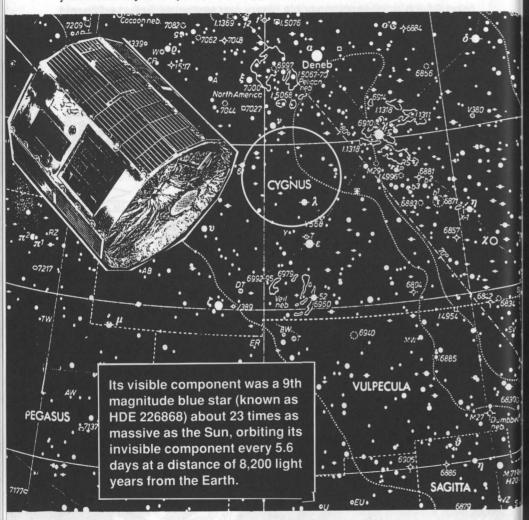
### Observational Evidence for Black Holes

Stephen Hawking says there are thousands and thousands of black holes in the Milky Way galaxy alone. But until the day an astronomer is lucky enough to see a well-known star disappear, indirect methods must be used – such as observations on a binary star system with one visible and one invisible (i.e. the black hole) component. John Wheeler has an interesting metaphor for such a system.



In December 1970, the X-ray satellite *Uhuru* was launched from the coast of Kenya. Astronomers were about to use still another part of the EM spectrum – X-rays – to probe the heavens.

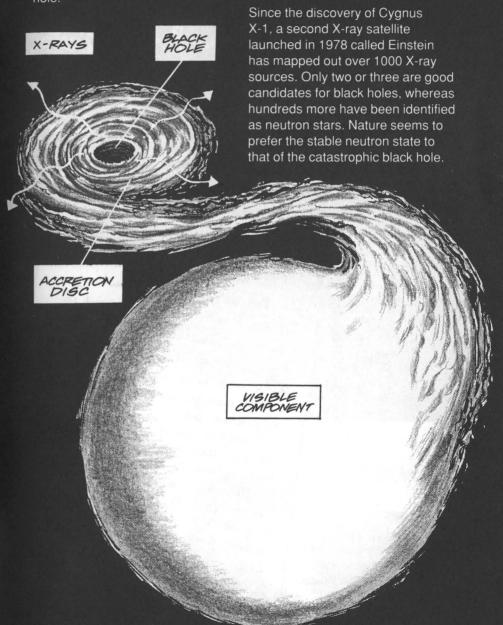
Within two years, over 300 sources of X-rays were detected. One of these in the constellation Cygnus (now called Cygnus X-1) looked like just the binary-star system the black hole enthusiasts were waiting for.



With good estimates of the mass of HDE 226868 and reliable observations of the period of revolution, astronomers could calculate the mass of the invisible component – 10 times as massive as the Sun. **Too big to be a neutron star, it had to be a black hole.** 

Theorists quickly developed a model to explain the X-rays. They believe that the black hole is sucking off matter from its visible partner, forming an accretion disk around itself. The hot inner regions, moving close to the speed of light, produce intense

bursts of X-rays shortly before the spiralling matter disappears down the hole.

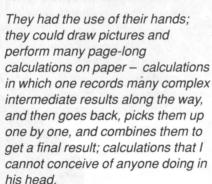


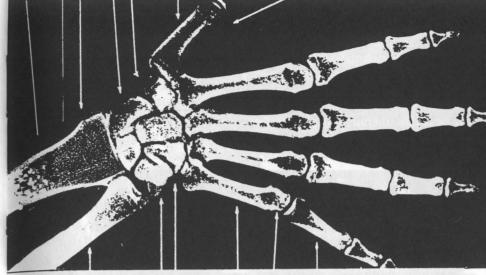


Thorne became a close friend of Stephen and watched his development very closely.



In November 1970, Stephen Hawking was just beginning to reach full stride as a physicist. He had made several important discoveries already, but he was not yet a dominant figure. As the 70s began we watched him become dominant. With his severe disability, how has Hawking been able to outthink and out-intuit his leading colleagues/competitors, people like Roger Penrose, Werner Israel, and Yakov Borisovich Zeldovich?

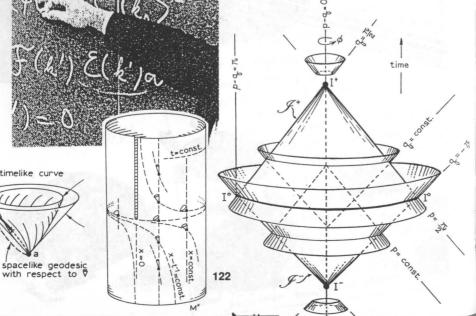


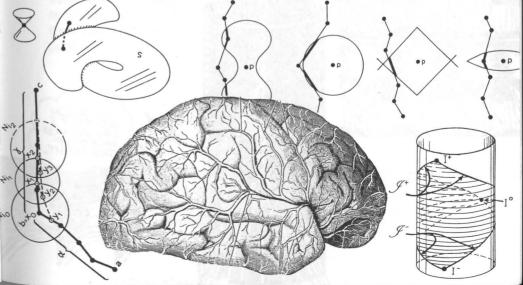


Hawking's mental pictures and mental equations have turned out to be more powerful, for some kinds of problems, than the old paperand-pens ones, and less powerful for others, and he has gradually learned to concentrate on problems for which his new methods give greater power, a power that nobody else can begin to match.

By the early 1970s, Hawking's hands were largely paralyzed; he could neither draw pictures nor

write down equations. His research had to be done entirely in his head. But because the loss of control over his hands was so gradual, Hawking has had plenty of time to adapt. He has gradually trained his mind to think in a manner different from that of the minds of other physicists. He thinks in new types of intuitive mental pictures and mental equations that, for him, have replaced paper-and-pen drawings and written equations.





### **Hawking's Eureka Moment**

One of the problems on which Hawking has used mental pictures to gain insight was his study of the surface area of black holes. What started as a rather esoteric problem in black hole dynamics, eventually led to his greatest discovery in physics.

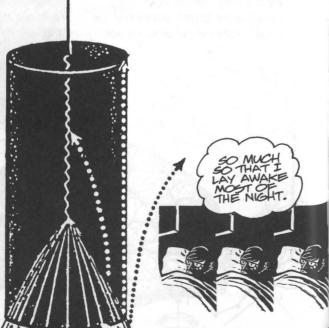
As with Einstein's "happiest thought", Hawking too can remember exactly what he was doing when the germ of his best idea came to him.



One evening in November 1970, shortly after the birth of my daughter Lucy, I started to think about black holes as I was getting into bed. My disability makes this rather a slow process, so I had plenty of time.

He saw in a flash that **the surface area of a black hole can never decrease**, by considering the paths of light rays hovering just at the event horizon of two black holes. He did not need paper and pen, nor a computer – the pictures were in his head.





The rays of light that form the event horizon, the boundary of the black hole, can never approach each other.
Consequently, the area of the event horizon (i.e. the black hole surface) might stay the same or increase with time, but it could never decrease.

Otherwise, it would mean that at least some of the rays of light in the boundary would have to be approaching each other... which is not possible!

This statement may not seem so remarkable. Since nothing can get out of a black hole and **anything** can go in, how could a black hole get smaller anyway? But Hawking's idea was more general. Even if **two** black holes combine, the total surface area will always be equal to or greater than the sum of the two. It can never decrease. He published his result.

A<sub>3</sub> > A<sub>1</sub> + A<sub>2</sub>

COMBINED
BLACK HOLES
AT LATER TIME.

TWO SEPARATE
BLACK HOLES
AREA 'A'
AT TIME 1.

The surface area of a black hole can only stay the same or increase, but can never decrease.

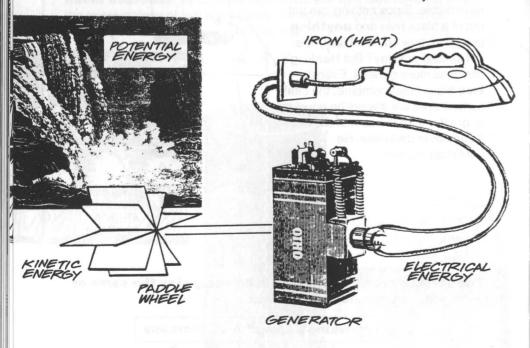
Hawking's Law of Area Increase

Such a statement . . . can never decrease . . . immediately gets scientists thinking about the quantity called **entropy** which appears in the second law of thermodynamics: **The entropy** (disorder) of a system can only stay the same or increase but never decrease (if the system is isolated and left to reach equilibrium).

THIS SECOND LAW
OF THERMODYNAMICS HAS
A VERY INTERESTING HISTORY
AND IS CERTAINLY SOMETHING
YOU NEED TO KNOW.

# **The Laws of Thermodynamics**

During the 19th century, a set of mathematical relationships were developed by chemists, geologists and physicists which combined several seemingly disparate concepts into a few powerful laws. Such quantities as heat and the energy of motion were shown to be different forms of the same thing – namely energy – which had already been used to describe electrical, chemical and magnetic effects. **The total energy available in the Universe (the ultimate isolated system) was a constant and one form could be transformed into another.** This became known as the 1st Law of Thermodynamics.

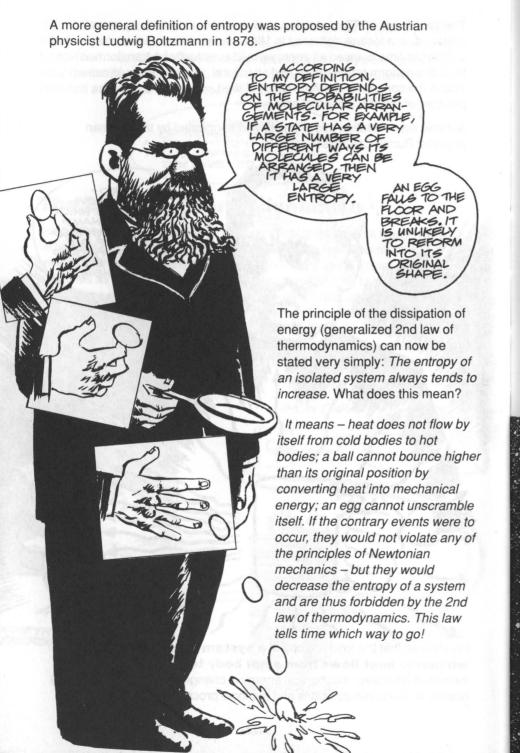


The **2nd Law of Thermodynamics** is more subtle but just as profound. In a lecture delivered in 1854, Hermann von Helmholtz pointed out that as time elapsed all energy would eventually be transformed into heat at a uniform temperature and all natural processes would cease. This is the concept of the *heat death* of the Universe based on the principle of the *dissipation of energy*.

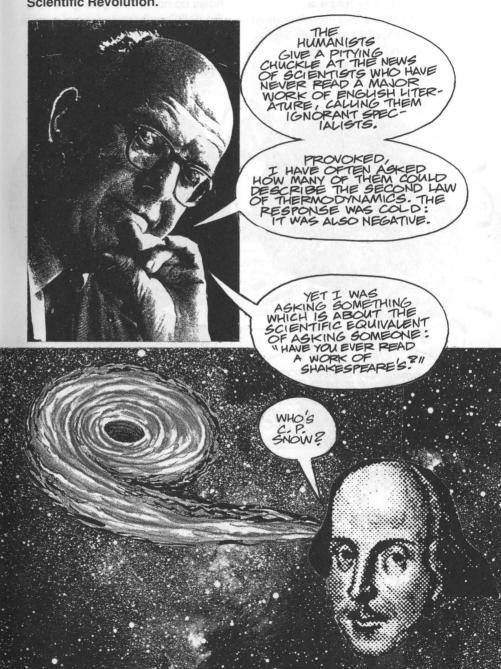
Another way of stating this principle was suggested by the German physicist Rudolf Clausius in 1865.



He showed that the total entropy of a system always increases whenever heat flows from a hot body to a cold body It also increases whenever mechanical energy is changed into internal (thermal) energy, as in certain collisions and frictional processes.



How important is this 2nd law of thermodynamics? It should be no less familiar to us than any of the works of Shakespeare, as the writer C.P. Snow remarked in his famous book, **The Two Cultures and the Scientific Revolution.** 

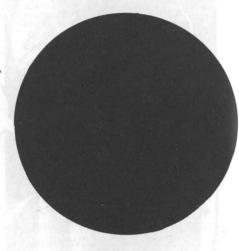


#### Now Back to Black Holes . . .

When bodies reach thermal equilibrium, they have a temperature and therefore must emit thermal radiation, exchanging energy with their surroundings as described on pages 98 and 99

But everyone knows that black holes do not emit anything – this is the defining characteristic of a black hole. Though anything can fall *into* a black hole, nothing gets out – not even light or any other radiation.





GENERALLY UNDERSTOOD
BY EVERYONE THAT IF BLACK
HOLES DON'T RADIATE, THEY
CANNOT HAVE A TEMPERATURE,
AND THUS CANNOT HAVE ENTROPY.
BLACK HOLES ARE CUT OFF
FROM THE UNIVERSE AND
ARE MOT IN THERMAL
EQUILIBRIUM...

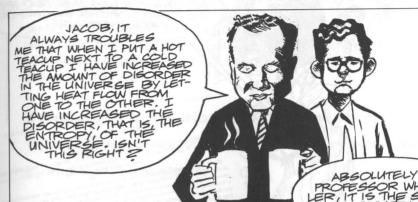
OR SO EVERYONE THOUGHT.



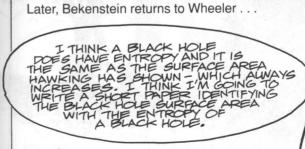
That is, until a physics postgraduate student working with John Wheeler in Princeton began to cause trouble.

#### **Controversial Birth of a New Idea**

Princeton New Jersey: John Wheeler and postgraduate student Jacob Bekenstein.

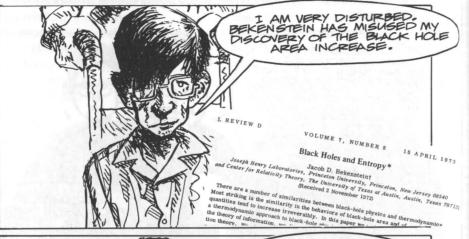


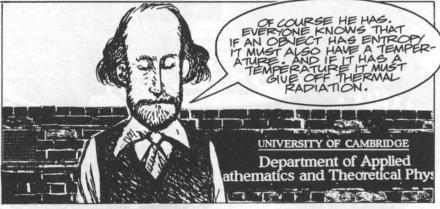






Meanwhile back at DAMTP, Stephen Hawking and Brandon Carter are talking about Bekenstein's paper.







## August 1972, Les Houches Summer School on Black Hole Physics

High up on a hillside in the French Alps, Stephen Hawking, James Bardeen and Brandon Carter joined forces to deduce from Einstein's general relativity equations the full set of laws that govern the evolution of black holes. When they were finished, they had produced a set of **laws of black-hole mechanics** that bore an amazing resemblance to the laws of thermodynamics.

S (entropy) =  $k_1A$  (surface area of black hole) T (temperature) =  $k_2G$  (surface gravity of black hole)  $k_1$  and  $k_2$  are constants



Meanwhile, Jacob Bekenstein was a student attending the summer school, still convinced that black holes have entropy.

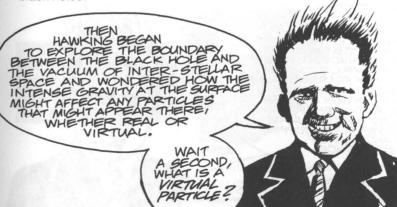


After the summer school, Bekenstein continued to identify the black hole surface area with entropy in the technical journals. Yet he did not assert that a black hole **has a temperature or that it must emit radiation**. Bekenstein was being inconsistent with the laws of thermodynamics.

Hawking, on the other hand, continued to attack Bekenstein's conclusions, but was becoming increasingly troubled.



All the calculations on black holes had been carried out using approximations based on general relativity theory, correct for macroscopic, i.e. large bodies. These approximations ignored any quantum effects, which surely would seem to be negligible in the case of black holes.

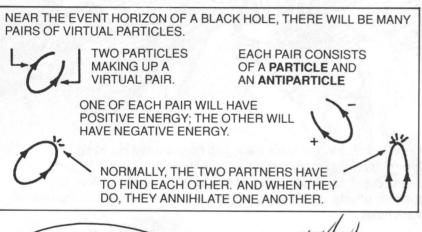


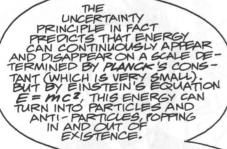
Time out for Something You Need to Know.

# The Uncertainty Principle & Virtual Particles

The uncertainty principle, as elucidated by Werner Heisenberg in 1927, states that there are limits on how accurately we can observe certain physical quantities, such as position, momentum, energy and even time. This is not a limit on our measuring instruments but an inherent characteristic of the Universe, which does not reveal **any** quantity with absolute precision.

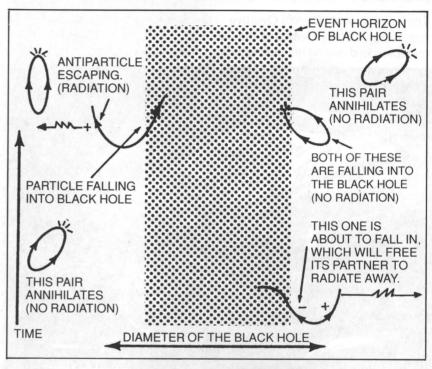
Think about the vacuum in outer space. We assume it contains absolutely nothing and thus has zero energy. But we can't be sure of this zero energy because of the same argument. Maybe if we look closely enough we can find *some* energy – at least for a short time.





THESE
ARE CALLED
VIRTUAL PARTICLES
FLICKERING EVERYWHERE
JUST BEING THE THRESHOLD OF OBSERVABLE
REALITY.

Hawking considered what might happen at the surface of a black hole (i.e. at the event horizon), where the intense gravitational field interacts with these virtual pairs. He was in effect combining quantum mechanics and general relativity in a single calculation for the very first time. What he found seemed quite remarkable.



I found that black holes are not completely black. They give off radiation.



It seems the intense gravity at the surface of the black hole can attract one of the particles of the virtual pair into the hole (negative energy), reducing the mass of the black hole, while the other unpaired particle (positive energy) escapes in the form of radiation and can be detected by an outside observer, i.e. an observer not falling into the black hole.

The most remarkable aspect of this result was the nature of the radiation. It had a perfect *thermal radiation* spectrum which meant that black holes were just like any other body in the Universe. It was now clear that black holes not only have entropy but a temperature as well and obey the classic laws of thermodynamics laid down in the late 19th century.

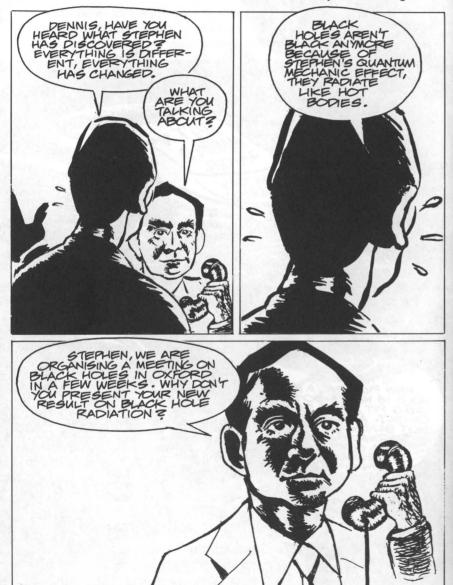
The science writer Dennis Overbye in his classic book on modern cosmology, **Lonely Hearts of the Cosmos**, produced a wonderful metaphor to describe his feelings about Hawking's discovery.

It was as if Hawking had popped the hood on a Ferrari and found an antique steam engine chugging away inside. Freeman Dyson, one of the world's top mathematical physicists, was enchanted with the new theory and wrote a popular essay after Hawking visited the Institute of Advanced Study in Princeton.



Hawking was reluctant to publish and had only shared his new results with a few close associates.

Dennis Sciama, visiting Cambridge from Oxford where he had taken an appointment in the physics department, met another of his former students, Martin Rees, then at the Institute of Astronomy in Cambridge.



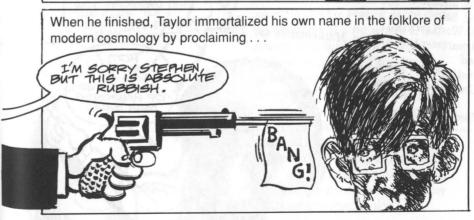
## February 1974, The Rutherford-Appleton Laboratory, Oxford

The chairman, John Taylor, a well-known mathematics professor and writer of a popular book on black holes, introduces Hawking.



Fifteen minutes later . . .

. . . so black holes are really not black after all. They have a temperature, an entropy and produce radiation just like any other thermodynamic body. Eventually they explode.



Taylor then stormed out of the session. Hawking sat in shocked silence. He knew his talk would be controversial, but he never expected anything like this.

A month after the meeting at Oxford, Hawking published a paper on the new radiation entitled Black Hole Explosions? in the journal Nature. The paper became the topic of discussion in physics departments everywhere and many were sceptical.

Four months later, Taylor and Paul Davies, a colleague at King's College, London, published a retort in the same journal, Do Black Holes Really Explode?

## Black hole explosions?

QUANTUM gravitational effects are usually ignored in calculations of the formation and evolution of black QUANTUM gravitation and evolution of black lations of the formation and evolution of curvatur justification for this is that the radius of curvatur justification for curvatur justification for curvatur justification for curvatur justification for curvatur justification justification for this is that the radius very large  $^{\rm CC}$  The creation of particles out of the very large  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time out of the very large  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2} \approx 10^{-33}$  cm, the len regions of space-time  $^{\rm CC}$  (c<sup>3</sup>) $^{1/2$ time outside the event horizon is very time outside the event horizon is very time outside the event horizon of the very regions of space-time where the metric are a Theoretical discussions where the metric which quantum Austrations of the metric are

$$b_i = \sum_{i} \left\{ \bar{\alpha}_{i,i} a_i - \beta_{i,i} a_i \right\}$$

$$p_i = \sum_i \{\alpha_{ij}f_i + \beta_{ij}\}$$

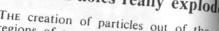
The author is very grateful to G. W. Gibb King's College London, Strand,

and help. S. W. HAWKING

Department of Applied Mathematics and Theor

and Institute of Astronomy University of Cambridge

Received January 17, 1974



Theoretical discussions of this process enco tational difficulties, however, because the is only well understood in Minkowski spa some simple cases, for example with the met cosmologies, or of black holes of the Kerr type, the existence of a global timelike Kill very plausible extension of the Minkowski particle. A number of exact results may then these results (ref. 1, and C. J. Isham and J.

P. C. W. DAVIES J. G. TAYLOR

Department of Mathematics, London WC2, UK

Received March 5, 1974.



Freeman Dyson compares Hawking's formulas to the epoch-making theory of Max Planck in 1900 which led to the quantum theory.





Now Hawking has written down an equation which looks rather like Planck's equation. Hawking's equation is S = kA, where S is the entropy of a black hole. A is the area of its surface, and k is a constant. But what does it really mean to say that entropy and area are the same thing? We are as far away from understanding this now as Planck was from understanding quantum mechanics in 1900. All that we can say for certain is that Hawking's equation is a clue to the riddle of black holes. Somehow, we can be sure, this equation will emerge as a central feature of the still unborn theory which will tie together gravitation and quantum mechanics and thermodynamics.

Perhaps the best way to look at Hawking's discovery is to use another historical analogy. In the year 1900, Max Planck wrote down an equation, E = hv, where E is the energy of a light wave, v is its frequency, and h is a constant which we now call Planck's constant. This equation was the beginning of quantum theory, but in the year 1900 this made no physical sense. It only began to become clear twenty-five years later, when Planck's equation was built into the theory which we now call quantum mechanics.

It is unlikely there has ever been a more powerful demonstration of the self-consistency of physics - a first step towards quantum gravity. It is the unification of three distinct theories of physics which makes Hawking's Radiation so important.



Heisenberg & Schrödinger

**QUANTUM MECHANICS** 

1927

UNCERTAINTY PRINCIPLE



**THERMODYNAMICS** 

2nd LAW OF **THERMODYNAMICS** (ENTROPY)

**BLACK HOLE RADIATION** 

(HAWKING 1974)



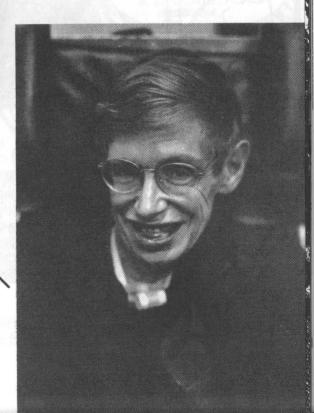
**BLACK HOLE** 

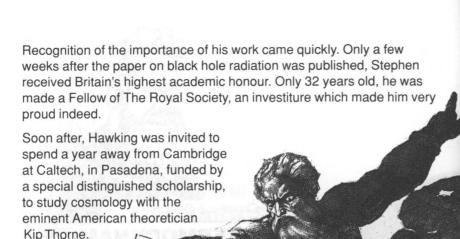
Einstein & Oppenheimer

**GENERAL** 



1915





CADEMIA CIENTIARVM

During my stay in California, I received word from the Vatican in Rome that I had been chosen by the Pontifical Academy of Science to receive the Pope Pius XI Medal.

In a strange way, this award began a shift in his research from black holes to the beginning of the Universe, a subject of great interest to the Roman Catholic Church.

## Hawking and the Vatican – a Modern Day Galileo

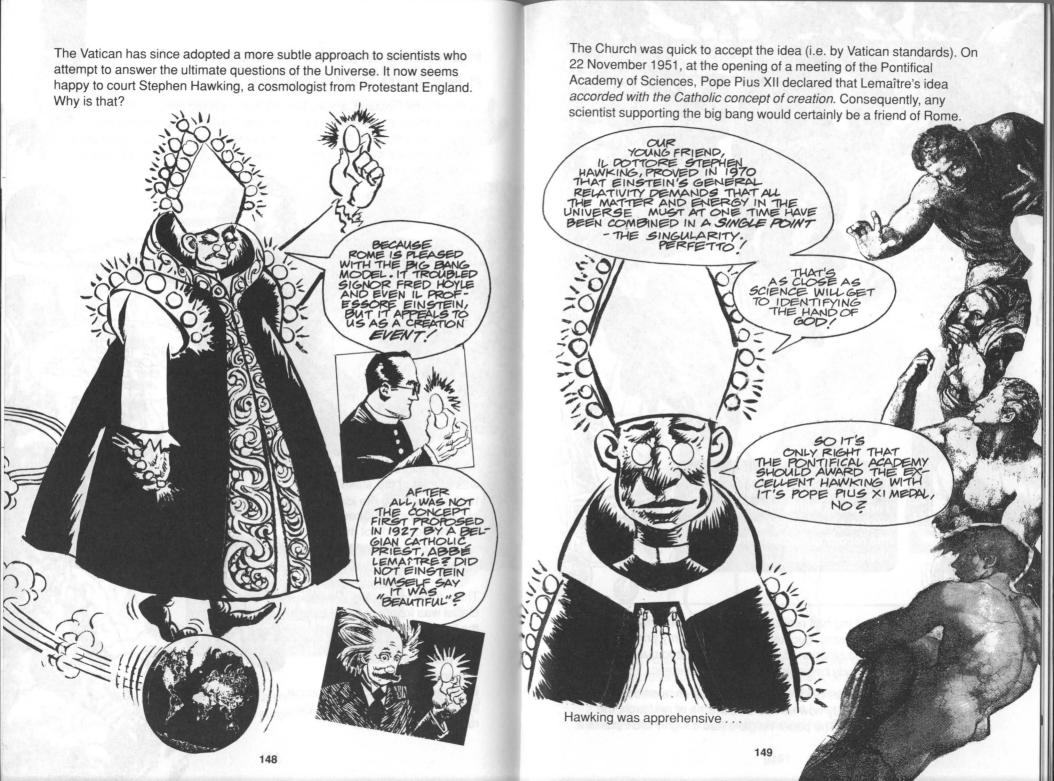
The powerful Roman Catholic Church has a vested interest in scientific theories about the heavens. For centuries the Church promoted the scientific teachings of Aristotle (a good philosopher but a poor physicist) and the celestial system of Ptolemy which both placed the Earth and Man at the centre of the Universe.

To safeguard the church's teaching, Giordano Bruno was burned at the stake in 1600 for teaching the ideas of Copernicus' heliocentrism that the Sun and not the Earth is at the centre of the solar system.

Thirty-three years later, Galileo Galilei was forced to kneel before the Inquisition, with chains of torture rattling in the background, and recant his belief in Copernicanism.

Later, he was placed under house arrest in his villa at Arcetri for the remainder of his days.

147





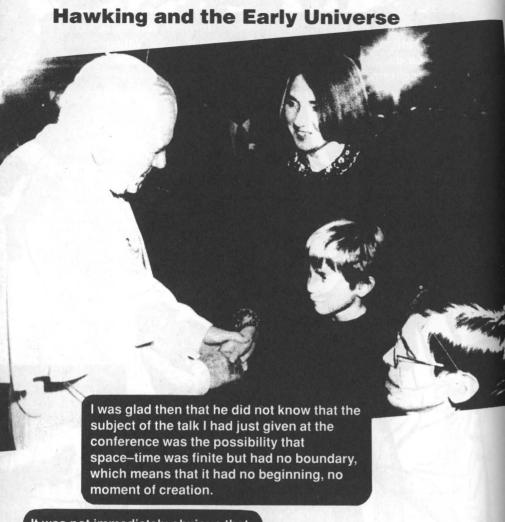
By the late 1970s, Hawking had realized that general relativity is not valid at the moment of the big bang, because of the uncertainty principle, and he was exploring the combination of general relativity and quantum mechanics. He was already beginning to think like a heretic.

But he was back in Rome in 1981, invited to a conference on cosmology organized by the Vatican. By now he had a new area of research, the beginning of the Universe. The paper he gave had a highly technical title.

My interest in the origin and fate of the Universe was reawakened when I attended a conference on cosmology in the Vatican in 1981. Afterwards, we were granted an audience with the Pope, who was just recovering from an attempt on his life.



In his talk, Hawking suggested that space and time were finite in extent but were closed up on themselves without boundaries or edges. This has become known as the **No Boundary Proposal**. If this theory is correct, there would be no singularities and the laws of science would hold **everywhere**, including at the beginning of the Universe.



It was not immediately obvious that my paper had implications about the origin of the Universe, because it was rather technical and had the forbidding title, 'The Boundary Conditions of the Universe'.

Hawking had begun to work seriously on the early Universe, a subject which has dominated his thinking to the present day. In the paper he gave at the Vatican, he introduced the **No Boundary Proposal**, his latest and most radical idea. It was an attempt to apply quantum theory to the singularity at the beginning of the Universe.

### Why Do We Need Quantum Theory?

In the big bang model of the Universe, the general theory of relativity provides a reliable programme for describing the evolution of our Universe from just moments after time = 0 to the present day. However, thanks to Hawking, we now know that, at the starting point, general relativity predicts a singularity and the theory breaks down. It is a *classical theory* and time and space cannot be described by Einstein's equations when matter is crunched together at such unbelievable densities.

How can physics predict the beginning of the Universe if all the laws break down at the big bang? Quantum theory must be used.

PRESENT ERA.
HUMAN LIFE EVOLVES.

10 BILLION YEARS
AFTER THE BIG BANG,
SOLAR SYSTEM FORMS.

•5 BILLION YEARS AFTER THE BIG BANG, MILKY WAY GALAXY EVOLVES.

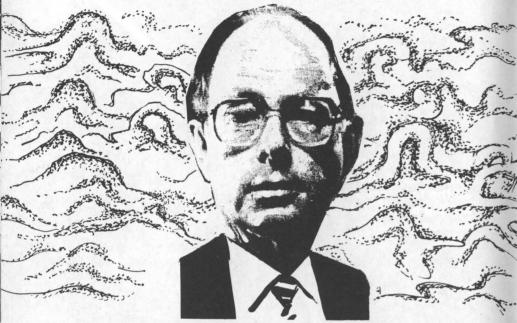
300.000 YEARS
AFTER THE BIG BANG
MATTER AND RADIATION
SEPARATE, COSMIC
BACKGROUND RADIATION
FIRST APPEARS.

BIG BANG EXPANSION
OF THE UNIVERSE BEGINS
15 BILLION YEARS AGO

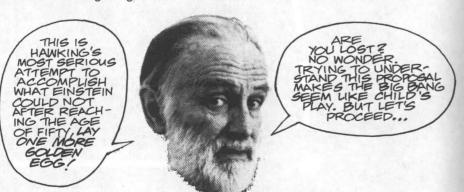
5 10 15 BILLIONS OF YEARS AFTER BIG BANG.

#### **Quantum Cosmology**

Starting with this question, Hawking and his collaborator, Jim Hartle of the University of California, have used the No Boundary Proposal to develop a new idea in **quantum cosmology**. Unlike previous approaches, Hawking and Hartle (hereafter H & H) have used imaginary time to study the singularity at the big bang.

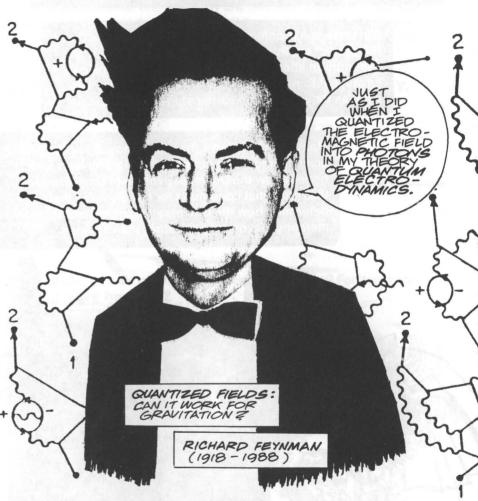


The reasoning goes like this. At its birth, the Universe is entirely within the quantum state. So H & H treat the Universe as a single quantum system and try to determine its **wave function**. In other words, they are applying standard quantum mechanical principles to the whole Universe "before" the big bang starts.



### **Quantum Gravity or TOE**

The search is called *quantum gravity*, or TOE, the *theory of everything* – a term irritating to most physicists. Attempts so far, by particle physicists and relativists, have yielded few results.

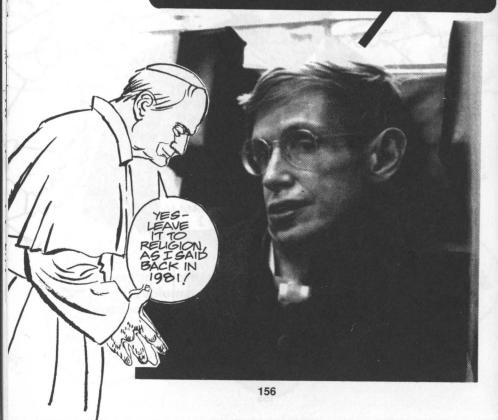


As usual, Hawking is taking a different approach to the problem. Not **quantum gravity**, but his own **quantum cosmology**, finding the wave function for the Universe. This is based on his No Boundary Proposal.

It has always profoundly disturbed me that if the laws of physics could break down at the beginning of the Universe, they could also break down anywhere else. That's why we have developed the No Boundary Proposal which removes the singularity at the beginning of the Universe.

But there is a problem with cosmology because it can not predict anything about the Universe without an assumption about the initial conditions. All one can say is that things are as they are *now* because they were as they were at an earlier stage.

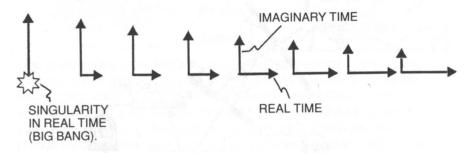
Many people believe that this is how it should be and science should be concerned only with laws which govern how the Universe evolves in time. They feel that the initial conditions for the universe that determine how the Universe *began* is a question for metaphysics or religion rather than science.



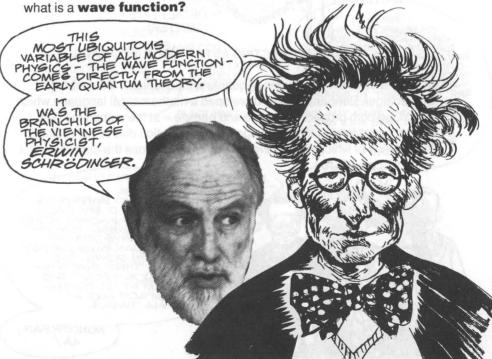
### **Quantum Cosmology and Complex Time**

So what's new about Quantum Cosmology? Well, H & H have used the mathematical trick of complex time to examine **all possible** universes that might form from the initial quantum state. Time is divided into two separate components, one imaginary and one real. Unlike real time, the imaginary component does not vanish at the big bang and the theory is thus useful **at** the singularity. Standard quantum mechanical procedures are then used to arrive at a wave function for the Universe.

#### COMPLEX TIME NEAR THE BIG BANG SINGULARITY.

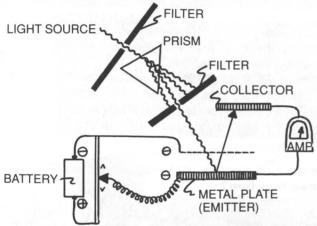


But what are standard quantum mechanical procedures? For that matter,



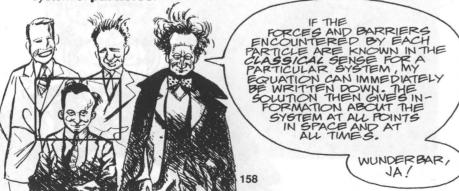
### Waves and Particles: Nature's Joke on the Physicists

Experiments have shown that a wave/particle duality exists in Nature. For example, a light beam produces interference effects (acts like a wave) but also kicks electrons out of the surface of a metal (acts like a particle). Similarly, electrons exhibit all sorts of particle properties, yet a beam of electrons produces a diffraction pattern (waves) when sent through a fine comb-like grating. This duality is a basic fact of the physical world and we must live with it. It is a consequence of the well-known *uncertainty principle*... or vice-versa.



LIGHT WAVES ACTING AS PARTICLES (PHOTONS).

In the 1920s, the early heroes of quantum mechanics – Heisenberg, Schrödinger, Bohr and Born – developed a mathematical language which described both properties – wave and particle – at the same time. The most elegant form of this language was an equation due to Schrödinger, the solution of which – the wave function – determines the behaviour of a system of **particles**.



## The Strange World of Quantum Mechanics

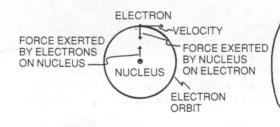
But what is a wave function? What exactly is waving?

Here is what Max Born proposed (ironically, following an idea of Einstein's).



One of the simplest problems to solve using quantum mechanics is the hydrogen atom. When the Schrödinger equation is solved for this case, the resulting wave function determines the probability of each energy state of the atom since it gives the probability of finding the electron at various distances from the nucleus. The nucleus is enveloped in a probability cloud, instead of precise planetary-type electron orbits of the classical atom.

CLASSICAL PICTURE OF HYDROGEN ATOM.



WHERE
THE PROBABILITY
CLOUD SURROUNDING
THE HYDROGEN ATOMIC
NUCLEUS IS DENSE, ONE
IS MORE LIKELY TO FIND
THE ELECTRON, BUT ONE
CAN NEVER SAY EXACTLY
WHERE IN THE ATOM THE
ELECTRON IS LOCATED
AT ANY ONE INSTANT. ALL
ONE CAN SPECIFY IS THE
PROBABILITY THAT IT
WILL BE IN VARIOUS
PLACES.

#### QUANTUM PICTURE OF HYDROGEN ATOM.

THE ELECTRON
IS MOST LIKELY
HERE.

FOR HERE.

NUCLEUS

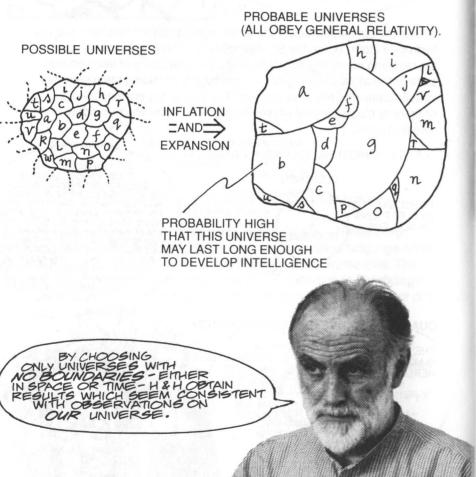




# Quantum Cosmology: Applying Schrödinger's Equation to the Universe

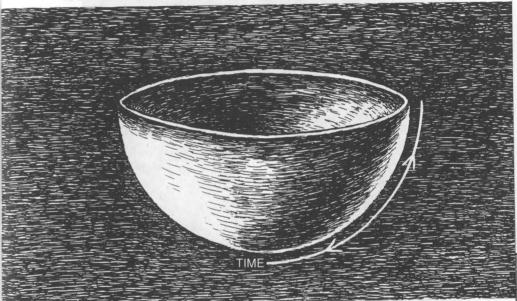
Is Hawking a bold thinker? Instead of **electron orbits** in the atom, think of **cosmological models** of the Universe. General relativity allows a variety of models: some expand from a point to a maximum size, then back to a point again; others expand forever; others expand differently in different directions. Yet all satisfy Einstein's equations.

Just as Schrödinger replaced classical electron orbits with wave functions that described the probability of an electron doing one thing or another, so Hawking and Hartle assign individual cosmological models a wave function that indicates the probability of the Universe having one particular geometry or another.

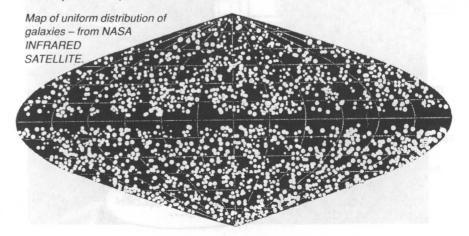


**Closed** universes satisfy this restriction. They are finite but have no edges, something like the two-dimensional surface of the Earth. They expand, come to a halt, then fall back to the same state like the points on the rim of the bowl shown in the sketch.

Depicted in this way, **closed** universes would have a beginning and an end, and would therefore have boundaries only in **real** time. The imaginary component, however, is continuous. So, H & H make the initial and final singularities of the closed Universe disappear.



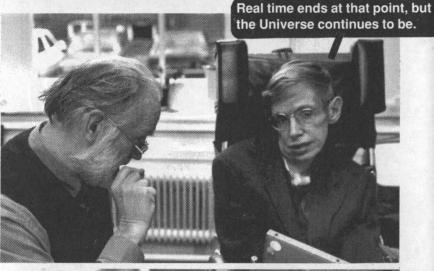
They also demonstrate that **uniform** universes are the most probable and end up predicting that our Universe is both **closed** and **uniform** – a finite sphere of space—time with no edges.



### **DAMTP: 17 February 1995**

As Hawking told the author only six weeks before this book was published . . .

The No Boundary Proposal predicts a Universe that starts out in a very smooth and ordered way. It expands by *inflation* first, then goes over to the standard *hot big bang* model, further expanding to a maximum radius before collapsing to a *big crunch* singularity in a disordered and irregular way.



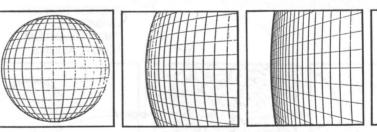


Calculations carried out so far on simple models indicate that a No Boundary Proposal Universe would be very much like our own. In addition, it would incorporate certain important ideas from contemporary cosmology – such as **inflation** and **quantum fluctuations**. Even the **anthropic principle** seems to fit. If you can understand these last three concepts, you should have a very good picture of Stephen Hawking's Universe. Not bad for a beginner!

#### **Inflation**

In the late 1970s, a new concept of **inflation** was introduced which proposed that the Universe expanded from an initial state smaller than a proton to a macroscopic size about ten metres across in only a fraction of a second. The rate of expansion was enormous. The idea solved two problems which had been nagging cosmologists for years.

- 1. Why is the Universe so flat, i.e. shows no evidence of curvature?
- 2. Why is the cosmic background radiation so uniform?
- **1.** The first of these questions implies that the mass density of the Universe is perfectly tuned to the critical value from its earliest expansion, a mind-boggling proposition (see page 49). But a rapid expansion at the beginning would flatten out the Universe to the critical mass density as a simple diagram can show.



FLATTENING OF THE UNIVERSE BY INFLATION

**2.** Inflation can also explain why the background radiation is so uniform. When the Universe was of infinitesimal size, all matter and energy was homogeneous, since everything was connected to everything else. As inflation took place, the homogeneity that existed at that early instant was spread across the much larger Universe, which continued to expand. Thus, when matter and radiation de-coupled about 300,000 years later, the Universe was still amazingly uniform.

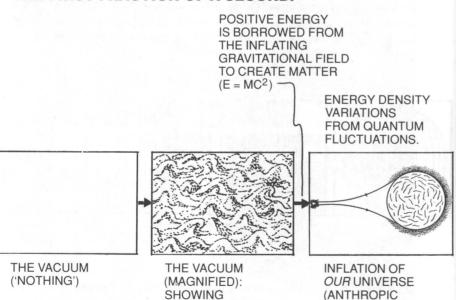
#### **Inflation and Quantum Fluctuations**

The inflation that smoothed out the early Universe could also produce small density variations which might explain galaxy formation. Recall from our discussion of virtual particles on page 136 that if we look closely enough at any physical system — even a vacuum — we observe the effects of **quantum fluctuations.** 

Inflation does not **erase** these quantum fluctuations but establishes them as **density variations** which appear as ripples of matter—energy across space—time. These ripples should then be imprinted on the background radiation as tiny temperature variations.

These temperature variations are precisely what George Smoot and his Berkeley–NASA team were looking for with the Cosmic Background Explorer Satellite (COBE) experiment launched in 1989. We need one more bold concept . . .

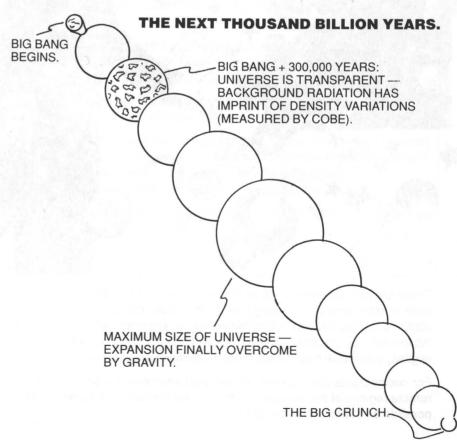
#### THE FIRST FRACTION OF A SECOND.



### **The Anthropic Principle**

The anthropic principle is a quasi-metaphysical notion which implies that, if a particular universe does not take on fundamental constants of Nature which allow for the existence of life and the development of intelligence, there will never be anyone to report on its properties. That is why our Universe seems so right to us, it's tuned perfectly.

Although many scientists rubbish this idea, no less an authority than Nobel Laureate Steven Weinberg (who wrote the seminal book on the early Universe, The First Three Minutes) believes that quantum cosmology provides a context in which the anthropic principle becomes simple common sense. The most probable universe is the one that we're in! As Voltaire's absurd philosopher Pangloss keeps telling Candide, "We live in the best of all possible worlds."



PRINCIPLE).

QUANTUM

FLUCTUATIONS.

#### **Hawking's Nobel Prize**

Stephen Hawking has received just about every award and honour which can be given to a scientist. Naturally, the question arises whether he will be awarded the most famous of all – an invitation to the Royal Academy of Sciences in Stockholm to receive the Nobel Prize in Physics.



There are complications. First of all, the award is only rarely given for work in astronomy or cosmology rather than pure physics. The second obstacle is more serious. Alfred Nobel was a very practical man (he made his fortune from patents on the explosive TNT) and insisted that to be eligible, theoretical discoveries must be verified by experiment.

For cosmologists like Hawking, whose laboratory extends to the most remote regions of the Universe, experimental verification may never be possible or, at best, take decades.

Let's review Hawking's major theoretical discoveries which might win him the Nobel Prize.

- **1.** Using General Relativity, Hawking and Penrose showed that the classical concept of time must have begun with a singularity at the Big Bang and thus the Universe existed at one time in a hot, dense state.
- **2.** In 1974, he discovered that black holes radiate like thermodynamic bodies (now called **Hawking Radiation**) and possess a temperature (proportional to their surface gravity) and an entropy (proportional to their surface area).
- **3.** He presented a model for the early Universe called the **No Boundary Proposal** with Jim Hartle which predicts density variations in the early Universe due to quantum fluctuations of the vacuum.

Ironically, **Hawking Radiation**, his most significant work, seems an unlikely candidate for the Nobel award as it seems impossible to detect.

However, both the Big Bang singularity (hot, dense state of the Universe) and quantum fluctuations (seeds for galaxy formation) could be proved if very accurate **absolute** and extremely sensitive **differential** measurements were made of the cosmic background radiation.

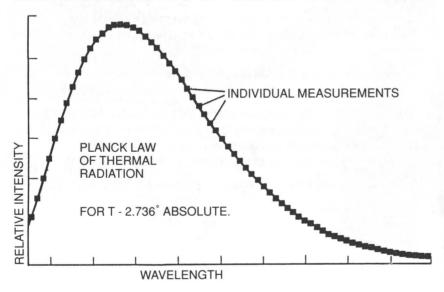
That is exactly what the COBE project did between 1989 and 1992.

## **COBE:** the Greatest Discovery of All Time (?)

COBE took twelve years to design and carry out, but the results were nothing short of spectacular. Launched in 1989, the instruments took only 8 minutes to verify the conclusions based on the 1964 measurements of Penzias and Wilson, but this time at many different wavelengths. The data traced out a near perfect thermal radiation curve (see page 99) for a background temperature of 2.736 degrees C above absolute zero.

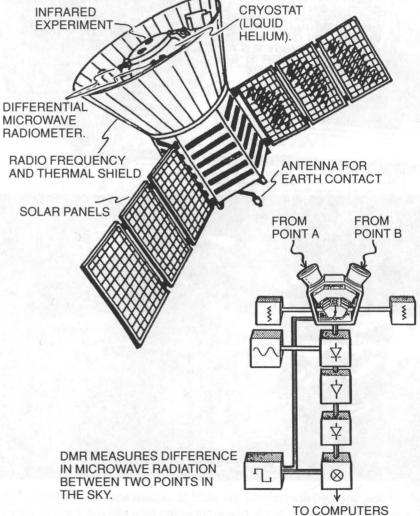
This was COBE I which used an *absolute* microwave radiometer calibrated by a bath of liquid helium on board the satellite. The results proved without a doubt that the detectors were looking at the remnant of the hot, dense state of the early Universe which we call the big bang. Such a curve would have thrilled Max Planck, as it did the American Astronomical Society when first presented in 1990.

#### COBE MEASUREMENTS OF BACKGROUND RADIATION.



But the big news was still to come. COBE II used a sensitive differential microwave radiometer (DMR) which doesn't measure the absolute temperature of the radiation at a given point in the sky; rather, it measures the **difference** in temperature between two points. The COBE I single antenna gives the answer: "The temperature at point A is 2.725 degrees." But the COBE II dual-antenna differential radiometer gives the answer: "The temperature difference between point A and point B is 0.002 degrees."

## THE COBE SPACECRAFT

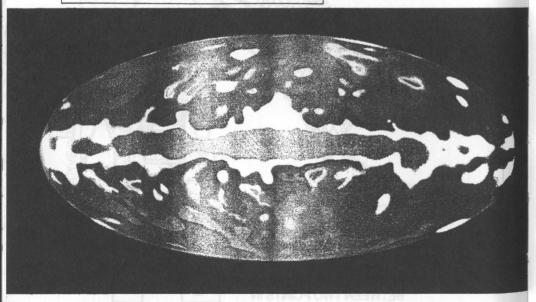


This was George Smoot's project – to look for evidence of ripples in the space–time of the 300,000-year-old Universe. In April 1992, after more than two years of data collecting and analysis, Smoot and his team made a dramatic announcement. The COBE satellite had detected tiny temperature variations of the order of about one-hundred-thousandth of a degree in the background radiation.

ACCORDING
TO COMPUTER
GENERATED PLOTS
OF THE ENTIRE SKY,
THE TEMPERATURE WAS
MINUTELY HIGHER IN THE
DIRECTION OF THE LARGE
GALACTIC CLUSTERS AND
SLIGHTLY LOWER IN THE
GREAT COSMIC
VOIDS.



COBE MAP OF THE MICROWAVE SKY SHOWING OUR GALAXY AND COSMIC RIPPLES.



It now seemed possible for theorists to explain some of the structures seen in today's Universe in terms of events which took place billions of years ago.

The report was greeted with an enthusiastic media response all over the world



Science and wal-

"It's the greatest discovery of the century – if not of all time"

IF YOU'RE REUGIOUS, IT'S LIKE SEEING GOD.

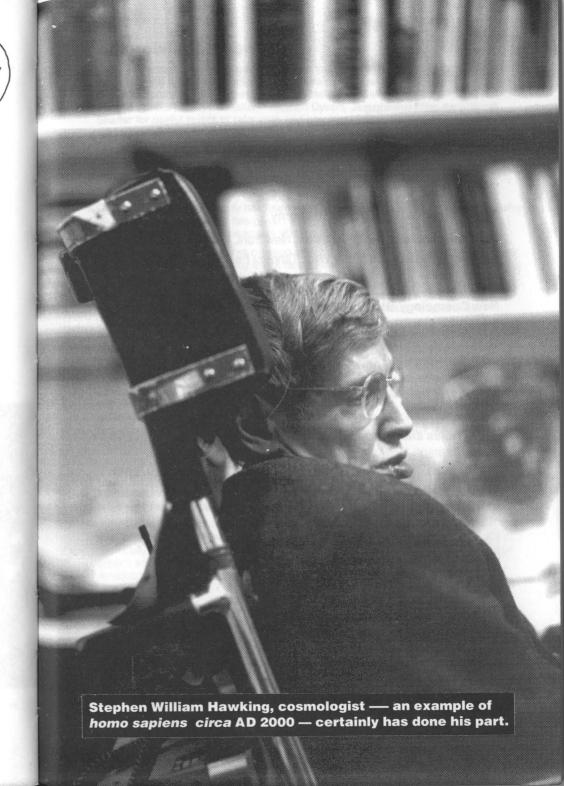


Both Hawking and Smoot made statements which together just about covered the two ends of the emotional spectrum. Smoot is a religious man and has accepted the big bang as a creation event. COBE's results moved him emotionally.

Hawking sees things differently. To him, the variations in the background radiation seen by COBE are simply evidence for the presence of quantum fluctuations in an inflationary Universe consistent with his No Boundary Proposal. Any wonder he's smiling.

COBE's success is seen by most scientists to be a stunning confirmation of big bang cosmology. But the game is not yet up. The final solution to the mysteries of the beginning and structure of the Universe may be much more complicated.

The Earth-centred cosmos of Aristotle and Ptolemy, the Sun-centred system of Copernicus, Le Maître's Cosmic Egg and Hawking's No Boundary Proposal are just steps along the way to deeper understanding of the Universe and our place in it. The journey is everyone's to contemplate, to understand, to enjoy.



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